

# **PERFORMANCE ANALYSIS OF CASCADE REFRIGERATION SYSTEM**

*A Major Thesis Submitted in  
Partial fulfillment of the requirements for the award of the degree of*

***MASTER OF ENGINEERING***

**in**

**THERMAL ENGINEERING**



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## **CANDIDATE'S DECLARATION**

I hereby declare that the work which being present in the major thesis entitled “**Performance Analysis of Cascade Refrigeration System**” in the partial fulfillment for the award of degree of MASTER of ENGINEERING with specialization in “THERMAL ENGINEERING” submitted to Delhi College of Engineering, University of Delhi, is an authentic record of my own work carried out under the supervisions of Dr. R. S. MISHRA and Mr. A. ARORA, Department of Mechanical Engineering Delhi College of Engineering, University of Delhi. I have not submitted the matter in this dissertation for the award of any other Degree or Diploma or any other purpose what so ever.

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## **CERTIFICATE**

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*“If brain is the nucleus of thoughts, teacher is the source of energy to run the operation of solving cross puzzles of doubts that often poise the mind of students.”*

It is a great pleasure to have the opportunity to extend my heartiest felt gratitude to everybody who helped me throughout the project.

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## **ABSTRACT**

Ammonia/CO<sub>2</sub> mixture is presently considered to be the best for cascade refrigeration up to 216.58°K. However to approach temperatures lower than 216.58°K the mixture of CO<sub>2</sub> with other refrigerants are required. The aim of present work was to study the possibility of using carbon dioxide mixtures in those applications where temperatures below CO<sub>2</sub> triple point (216.58 K) are needed. The blends considered for analysis purpose are R744/R125, R744/R41, R744/R32, and R744/R23. The analysis of cascade refrigeration cycle has been carried out with the help of a computer program developed using Engineering Equation Solver (EES). The composition of CO<sub>2</sub> is varied from a mole fraction of 0.1 to 0.8 along with R23, R32, R41 and R125. The mixtures properties of the investigated blends (R744/R125, R744/R41, R744/R32, and R744/R23) were calculated by Ref Prop 7.0 and used in EES program. Ammonia is used as refrigerant in high-temperature-circuit.

Blend of CO<sub>2</sub> with R125 having a mole fraction ratio of 0.3/0.7 is the best among all the blends considered as it offers highest COP values. Up to mole fraction ratio 0.5/0.5, CO<sub>2</sub>/R125 blend is better than other blends for same mole fraction ratio. At mole fraction ratio of 0.8/0.2, the blends R744/R125, R744/R41 and R744/R32 have almost same values of COP and that of R744/ R32 blend is lowest. Hence R744 blends are an attractive option for the low-temperature circuit of cascade systems operating at temperatures approaching 200 K.



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# NOMENCLATURE

COP	Coefficient of performance (non dimensional)
$h$	Specific enthalpy (kJ/kg)
HTC	High temperature circuit
LTC	Low temperature circuit
$m$	Mass flow rate (kg/s)
$P$	Pressure (kPa)
$Q$	Heat exchange per unit mass (kw)
$s$	Specific entropy (kJ/kg k)
$T$	Temperature ( $^{\circ}\text{C}/^{\circ}\text{K}$ )
VCC	Volumetric cooling capacity (kJ/m <sup>3</sup> )
$V_s$	Specific volume at inlet to the compressor (m <sup>3</sup> /kg)
$W$	Specific work (kJ/kg)

## Subscript/superscript

C	Condenser
comp1	Low temperature circuit Compressor
comp2	High temperature circuit Compressor
E	Evaporator
in	inlet
MC	Cascade condenser
out	outlet
r	Refrigerant
s	Isentropic

## Greek symbol

$\eta$	Efficiency
$\Sigma$	Summation of

Refrigeration is defined as “the transfer of heat from a lower temperature region to a higher temperature one.” Refrigeration devices that produce refrigeration are heat pumps, refrigerators, automotive air-conditioners, and residential/commercial air-conditioners. All of these devices have one thing in common, to reduce the temperature of an enclosed environment.

Vapour compression cycle can be used in temperature range  $-10$  to  $-30^{\circ}\text{C}$  easily. And low-temperature refrigeration systems are typically required in the temperature range from  $-30^{\circ}\text{C}$  to  $-100^{\circ}\text{C}$  for applications in food, pharmaceutical, chemical, and other industries, e.g., blast freezing, cold storages, liquefaction of gases such as natural gas, etc. At such low temperatures, single-stage compression systems with reciprocating compressors are generally not feasible due to high pressure ratios. A high pressure ratio implies high discharge and oil temperatures and low volumetric efficiencies and, hence, low COP values. Screw and scroll compressors have relatively flat volumetric efficiency curves and have been reported to achieve temperatures as low as  $-40^{\circ}\text{C}$  to  $-50^{\circ}\text{C}$  in single-stage systems (Stegmann, 2000). Further, the use of a single refrigerant over such a wide range of temperature results in either extremely low pressures in the evaporator and large suction volumes or extremely high pressures in the condenser. To increase volumetric efficiency and refrigerating effect and to reduce power consumption, multistaging with intercooling is often employed (Bansal and Jain, 2006).

Cascade refrigeration cycle can be used to achieve low temperatures, where series of single-stage units are used that are thermally coupled through evaporator/condenser cascades, as shown in Figure 1 for a two-circuit cascade unit. Each circuit has a different refrigerant suitable for that temperature, the lower temperature units progressively using lower boiling point refrigerants. Generally, two-circuit and rarely three-circuit cascade systems are used. In general, if the desired temperature can easily be achieved in a single-stage machine, it will be more efficient than a cascade system due to irreversibility and losses associated with a large number of components.

A commonly used refrigerant pair in the past has been R12 and R13 for the high pressure and low-pressure stages respectively in cascade system. But these refrigerants contained

chlorine which is ozone depleting. So eco-friendly refrigerants are most suitable for industrial applications related to food preservation, such as in supermarkets, cold storages, blast freezing, etc., where refrigeration to temperatures down to  $-80^{\circ}\text{C}$  is required (Bansal and Jain 2006). The conventional two-stage ammonia systems that were mostly used to cater to these applications are coming under cloud due to stricter safety regulations, particularly for human access facilities such as supermarkets, and the need for higher energy efficiencies.

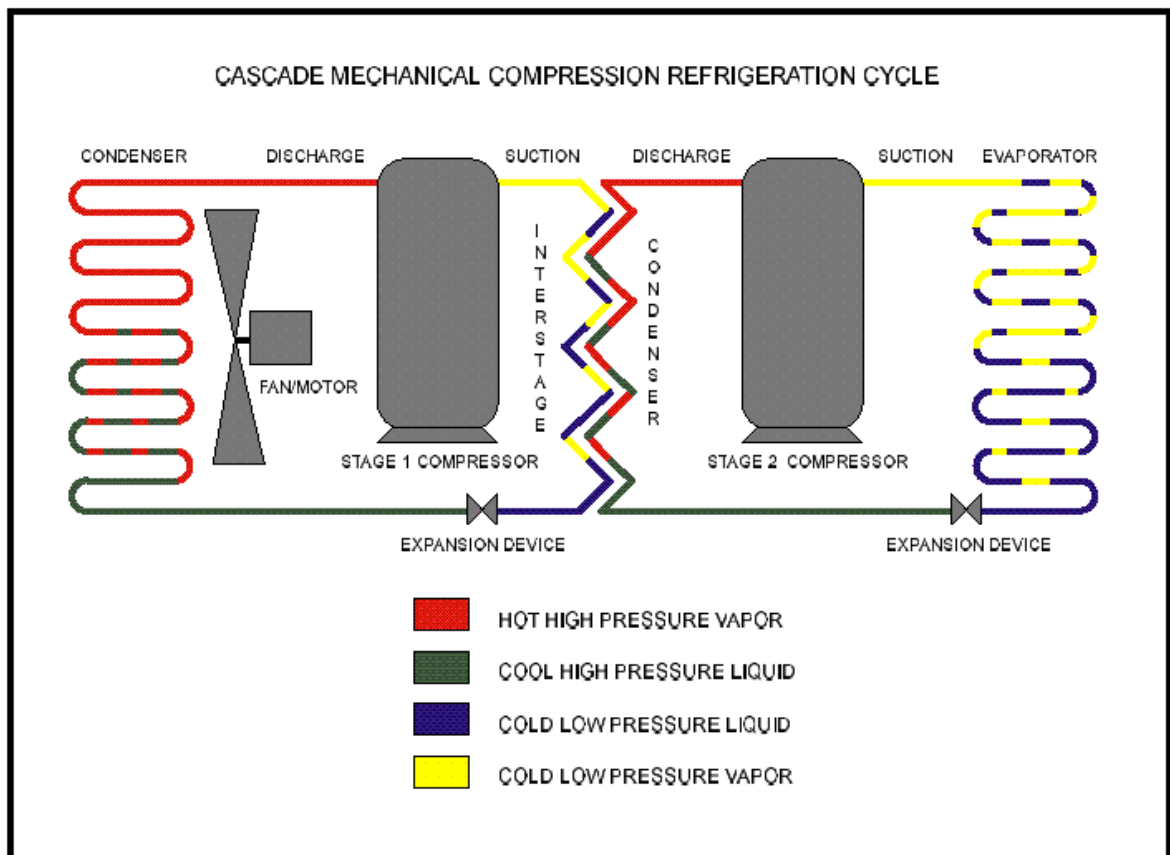


Fig.1 Two stage cascade refrigeration cycle

The continuous depletion of the ozone layer, which shields the earth's surface from UV radiation, has resulted in a series of international treaties demanding a gradual phase out of halogenated fluids. The chlorofluorocarbons (CFCs) have been banned since 1996, and also the partially halogenated hydro chlorofluorocarbons (HCFCs) are bound to be prohibited in the near future. The HFCs (chlorofluorocarbons) are candidate for the definite substitution of both CFCs and HCFCs, as they do not contain chlorine.



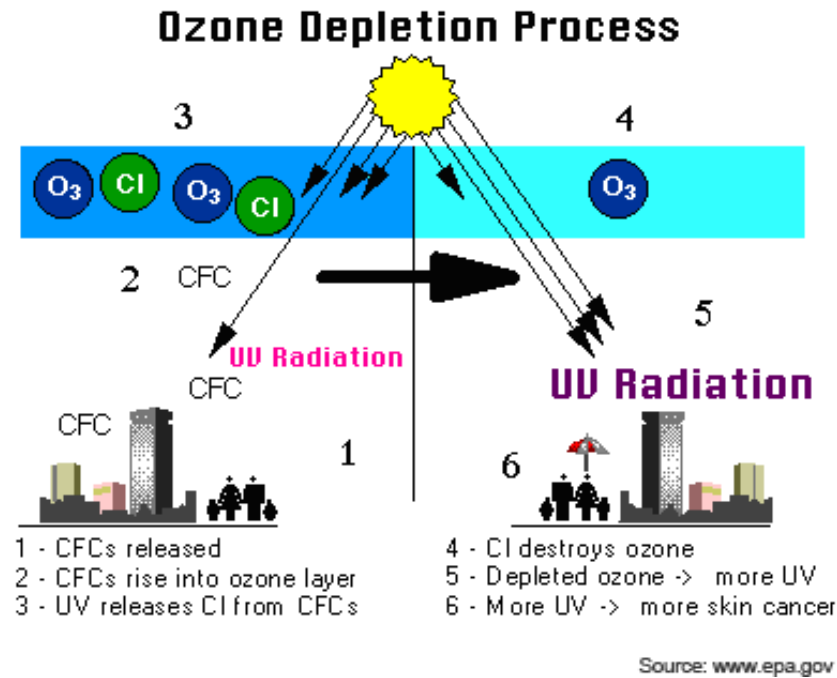


Fig.2 ozone depletion process

A further problem is the green house effect, stemming from the infrared radiation capture by some component of the atmosphere. Human activities have considerably increased the concentration of greenhouse gases (CFC, HCFCs, carbon dioxide, methane, nitrous oxide) that determine the earth's surface and atmosphere warming that might adversely affect the natural ecosystem. Over the last hundred years, the mean temperature have increased by 0.3°C to 0.6°C, and doubling the amount of carbon dioxide in the atmosphere is likely to yield a further temperature increase from 1.5°C to 4.5°C in particular, it is well known that the green house effect resulting from an operating plant is not a secondary matter. Recent estimate indicate that the overall contribution, both direct and indirect, to the green house effect of HCFCs and CFCs exceeds 24% (Houghton, 1995). So, the choice of the working fluid in the vapour compression plant must depend on both the absence of chlorine atoms in the molecule (ozone depletion potential (ODP) equal to 0) and their low contribution to the green house effect (low global warming potential (GWP) and high energy efficiency). The phase out of fully halogenated CFCs and partially halogenated HCFCs in an irreversible process in the industrialized world, but the problem of their replacement has been partially solved.

In present days, we should look non ozone depleting refrigerant which do not cause global warming. With respect to global environmental protection, the use of natural refrigerant in cascade refrigeration system helps to satisfy the obligations of

environmental treaties (Lee et al., 2006). Normally now a day's no. of pair are used in cascade refrigeration cycle like R-717 and R-508b, R-717 and R-744 etc.

R-717 in high temperature circuit and R-744 in low temperature circuit is a very interesting application for the food industry, where evaporating temperatures between 30 and  $-40^{\circ}\text{C}$  are needed but due to triple point of R-744 it cannot be uses beyond  $-56.57^{\circ}\text{C}$ . In present work, usages of carbon dioxide blends with HFCs (R-23, R-32, R-41 and R-125) have been examined in low temperature circuit of cascade refrigeration cycle to achieve low temperatures up to 200°K i.e. below triple point of R-744.

In this chapter, it is intended to give a brief literature review of the work being carried out on cascade refrigeration system during last decade.

Getu and Bansal (2008) have analysed of carbon dioxide–ammonia (R744–R717) cascade refrigeration system to optimize the design and operating parameters of the system. A multi linear regression analysis was employed in terms of subcooling, superheating, evaporating, condensing, and cascade heat exchanger temperature difference in order to develop mathematical expressions for maximum COP, an optimum evaporating temperature of R717 and an optimum mass flow ratio of R717 to that of R744 in the cascade system

Wilson and Maier (2006) have analysed that cascade refrigeration systems is the initial installation cost being 10% higher than the traditional direct expansion systems. But this cost can be negated with less refrigerant charge requirements and the environmental advantage of the cascade system due to less direct emissions as compared to single-stage system.

Jain and Bansal (2006) reviewed two circuit cascade refrigeration systems. The high-temperature circuit uses high boiling point refrigerants such as R-22, R-134a, ammonia, propane, propylene etc. The low-temperature circuit uses low boiling refrigerants such as carbon dioxide, HFC-23, and R-508B etc. CO<sub>2</sub> differs from other common refrigerants in many aspects, and has some unique properties. CO<sub>2</sub> is most commonly applied in cascade or hybrid system designs in industrial refrigeration, because its pressure can be limited to such extent that commercially available components like compressors, controls and valves can be used. It has been found that ammonia is the best high-temperature refrigerant among propane, propylene, and R-404A considered in their study. It gives a theoretical optimum COP.

Lee et al. (2006) analyzed a carbon dioxide–ammonia (R744– R717) cascade system thermodynamically and determined the optimum condensing temperature of R744 in the low-temperature circuit. They have reported that the optimum condensing temperature of a cascade condenser increases by increasing evaporator and condenser temperature,

whereas the maximum COP increases with only evaporator temperature, but decreases as condenser temperature decreases.

Russmann and Kruse (2006) have performed analysis of cascade refrigerating systems using  $\text{N}_2\text{O}$  as refrigerant for the low temperature cascade stage and various natural refrigerants like ammonia, propane, propene, carbon dioxide and nitrous oxide itself for the high temperature stage and the basis of the comparison was a conventional R23/R134a-cascade refrigerating system. This  $\text{N}_2\text{O}$  system has nearly equal COP as a conventional R23/R134a-cascade refrigerating system

Tagung (2005) has reported that  $\text{CO}_2$  may be applied as a refrigerant in a number of different system types, including both subcritical and supercritical systems. The classic refrigeration cycle is subcritical, i.e. the entire range of temperatures and pressures are below the critical point and above the triple point. A single stage subcritical  $\text{CO}_2$  system is simple, but it has some disadvantages, because of its limited temperature range and high pressure.

Sawalha (2005) have been observed the cascade systems with the same fluid in both circuits. By reducing amount of superheat in the discharge temperature of the high-temperature circuit that result in a reduced capacity of the high-temperature condenser and increased refrigeration effect. High-temperature circuit condenser, cascade condenser and evaporator losses can also be reduced if the sizes of the heat exchangers are properly optimized. Several types of cascade condensers such as plate, shell-and-plate or shell-and-tube heat exchangers can be employed for cascade systems to couple the low- and high-temperature circuits.

Bhattacharyya et al. (2005) have been presented the optimization analysis for a  $\text{C}_3\text{H}_8$ – $\text{CO}_2$  based cascade system for simultaneous refrigeration and heating applications. The COP of this cascaded system increases with rising refrigerated space temperature and decreases with rising heating outlet temperature.

Agnew and Ameli (2004) demonstrated optimising of a cascade refrigeration system with multi staging on the high temperature side and single staging on the low temperature side. The alternative ozone friendly pair R717 and R508b has been chosen as a replacement of R12 and R13 respectively. R717 is more commonly known as ammonia, a well tried and tested refrigerant and R508b is a relatively new formulation consisting of 46% of R23 with the remainder being R116. It has no ozone depleting

potential and non-flammable. The chosen combination of R717 and R508b exhibited an improved performance over an original combination of R12 and R13.

Nicola et al. (2005) have presented a comparative analysis on the performance of a cascade refrigeration cycle operated with blends of carbon dioxide (R744) and HFCs (R23, R32, R41 and R125) as the low-temperature working fluid and R717 as the high temperature working fluid. They reported that R744 blends are an attractive option for the low-temperature circuit of cascade systems operating at temperatures approaching 200°K i.e. below CO<sub>2</sub> triple point 216.58°K. The mixtures (R744 blends) were modelled using the Carnahan–Starling–De Santis (CSD) Equation of state (EOS) taken as the thermal EOS from which the necessary vapour–liquid equilibrium and volumetric properties were derived to give the pressure–volume–temperature–composition (PVTx) parameters. The PVTx parameters were supplemented with the ideal gas heat capacity and described all the thermodynamic functions at each point in the cycle. The properties of the investigated blends (R744/R125, R744/R41, R744/R32, and R744/R23) were used to simulate the behaviour of a cascade cycle. They fixed evaporator temperature as 203°K, condenser temperature as 313°K and varying cascade condenser temperature as 213 to 283°K. They have taken 0°K approach and considered 5°K subcooling and 10°K superheating. They have not considered effect of varying the condenser temperature, effect of approach and cascade refrigeration system without superheating and subcooling. They performed each set of calculations for three compositions 0.1, 0.3 and 0.5 in mole fractions of R744 with HFCs (R23, R32, R41 and R125) and COP is presented as a function of cascade condenser temperature in the former and as a function of mixture composition in the latter. They reported that the COPs for all systems and compositions reach the maximum value at temperatures between 240 and 250°K. COP values are plotted in relation to mole fraction; they show a small negative departure from linearity.

Use of a liquid vapour heat exchanger in the low-temperature side was also investigated HFC/CO<sub>2</sub>. They reported that the liquid vapour heat exchanger cannot be recommended for R717 and the use of a heat exchanger in low temperature circuit improves the COP values substantially for the R-125/CO<sub>2</sub> blend and marginally for others. It also shifts the optimum cascade temperature toward higher values. This implies higher operating pressures in the cascade condenser that do not seem to be very desirable unless the gains are substantial, as in the case of the R-125/CO<sub>2</sub> blend.

Klein et al. (2001) have used liquid vapour heat exchanger. Subcooling the liquid leaving the condenser with the vapour before it enters the compressor is known to be able to improve a cycle's COP considerably. They have also reported that improvement only applies to refrigerants that have important exergy losses in the throttling process.

Missimer (1997) have analysed the auto refrigerating (or mixed refrigerant) cascades, to achieve temperatures to  $-180^{\circ}\text{C}$ . Moderate sized (less than 14 kW power input) auto refrigerating cascade (ARC) systems have been successfully converted from the use of CFC components to completely CFC-free refrigerant mixtures with successful operation. New zeotropic mixtures have overall ODP levels below 0.02 with nearly identical Carnot efficiencies, as well as requiring no hardware or lubricant changes. Present efforts have reduced the ODP by a ratio of 20 to 30 times compared to pre conversion mixes. Additional efforts show promise of obtaining an ODP of less than 0.01 and eventually down to zero when more acceptable zero ODP substances become available. However, their use is limited to special applications only.

Ratts and Brown (2000) have reported that the optimum temperature distribution for a cascade system was determined by minimizing entropy generation at each stage of the system. The equations for entropy generation were developed in terms of a single independent variable, the intermediate temperature ratio, and in terms of specific heats. Through the inter-mediate temperature ratio and through equations for the specific heats, the optimum temperature distribution was found. The development in terms of a single independent variable also provided a way to characterize the distribution of the losses.

Pearson and Cable (2003) reported the use of a plate-and-shell type cascade condenser instead of shell-and-tube type cascade condenser that is bulky. Plate-and-shell type condenser is expensive but compact and minimizes the leakage of carbon dioxide into the ammonia system.

## **2.1 CONCLUSION AND GAPS**

Cascade refrigeration systems are used to achieve low-temperatures. Using carbon dioxide in low temperature circuit and ammonia in high temperature circuit in cascade system is a very interesting application for refrigeration, where evaporating temperatures between  $-30$  and  $-40^{\circ}\text{C}$  are needed. But where lower temperatures are needed, this is no longer a feasible solution, due to the triple-point temperature of carbon dioxide ( $216.58$

K, -56.57 °C), which prevents its use in vapour compression cycles intended for use at lower temperatures. An obvious solution to overcome this drawback blends of carbon dioxide as mentioned by Nicola et al. (2005).

Most of the researchers used pure refrigerant except Nicola et al. (2005). They have done analysis of cascade system using carbon dioxide blend with HFCs. But they have not taken some parameters in their analysis such as approach (temperature difference between low temperature circuit condenser and high temperature circuit evaporator), effect of varying the condenser temperature on the performance parameters. They have considered the effect of superheating and subcooling in their model. Consideration of superheating and subcooling is natural but analysis of cascade system without superheating and subcooling is also necessary.

## **2.2 Problem formulation**

In the present study, analysis of cascade refrigeration system has been carried out by taking R717 in low temperature circuit and R-744 mixture with HFCs (R23, R32, R41 and R125) to achieve low temperatures down to 200°K.

It is proposed to examine the effect of following parameters on the performance of cascade refrigeration system and evaluation of optimum cascade condenser temperature in the present work.

- Effect of approach
- Analysis with and without superheating and subcooling
- Effect of varying the condenser temperature
- Varying the mole fraction of R-744
- Effect of using LVHE in low temperature circuit

In this chapter, it is intended to give thermodynamic analysis of the present work, which has been carried out on cascade refrigeration system.

### 3.1 SYSTEM DESCRIPTION

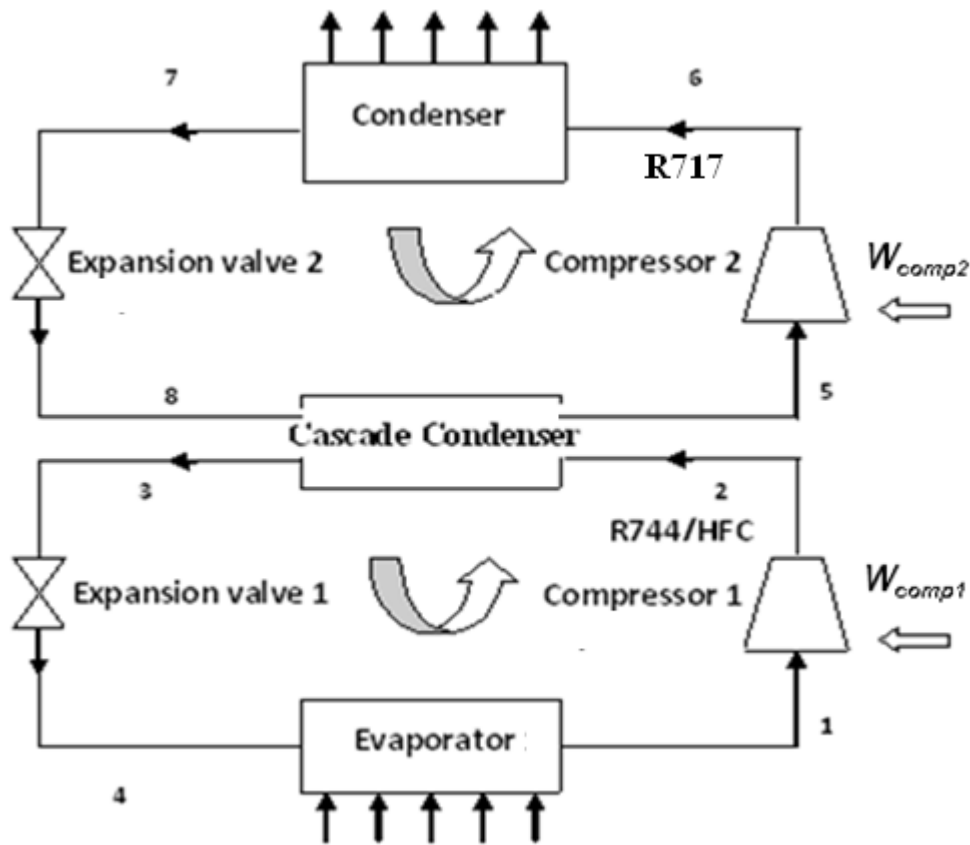


Fig.3 Schematic representation of two stage cascade refrigeration cycle

Fig.3 schematically represents a cascade refrigeration system. Fig.4 represents the corresponding pressure enthalpy diagrams. This refrigeration system comprises two separate refrigeration circuits- the high-temperature circuit (HTC) and the low-temperature circuit (LTC). Ammonia is the refrigerant in HTC, whereas carbon dioxide blend with HFCs (R-23, R-32, R-41 and R-125) are the refrigerants in LTC. The circuits



are thermally connected to each other through a cascade-condenser, which acts as an evaporator for the HTC and a condenser for the LTC.

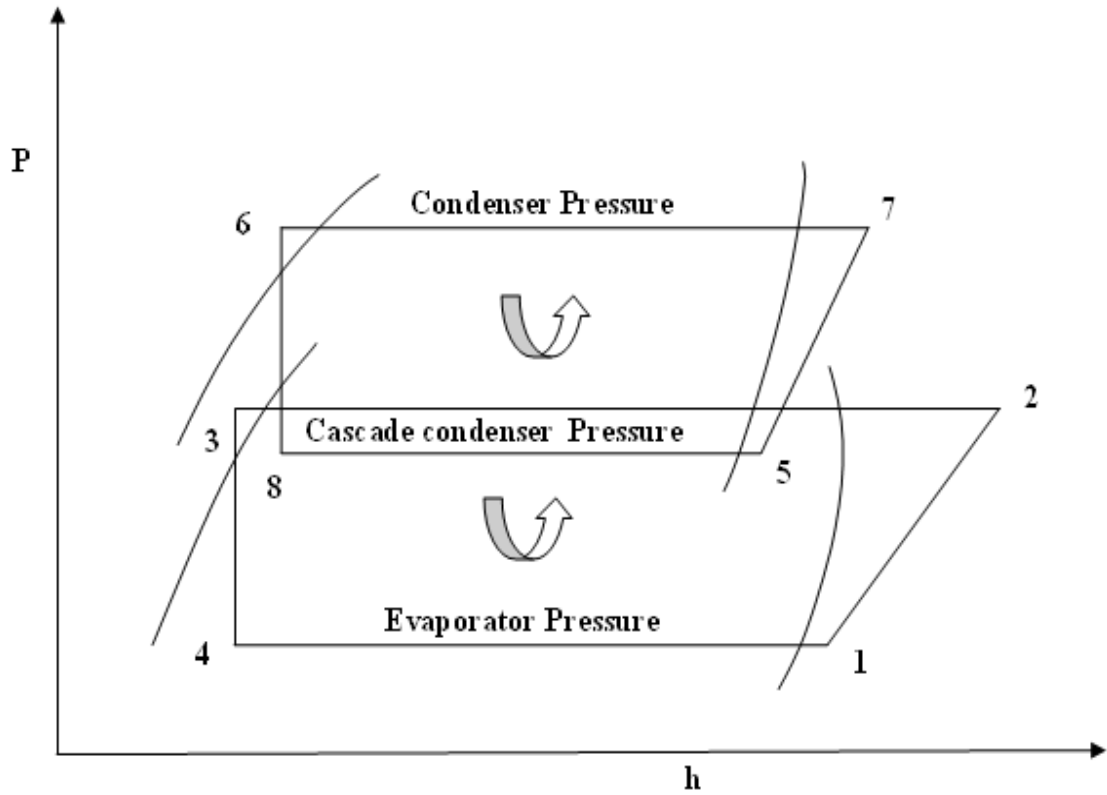


Fig.4 P-h diagram of cascade refrigeration system

The condenser in this cascade refrigeration system rejects a heat of  $Q_C$  from the condenser at condensing temperature of  $T_C$ , to its warm coolant or environment at temperature of  $T_0$ . The evaporator of this cascade system absorbs a refrigerated load  $Q_E$  from the cold refrigerated space at evaporating temperature  $T_E$ . The heat rejected by condenser of LTC equals the heat absorbed by the evaporator of the HTC.  $T_{MC}$  and  $T_{ME}$  represent the condensing and evaporating temperatures of the cascade condenser, respectively.

Approach represents the difference between the condensing temperature of LTC and the evaporating temperature of HTC. The evaporating temperature  $T_E$ , the condensing temperature  $T_C$ , and the temperature difference in the cascade-condenser are three important design parameters of a cascade refrigeration system.

### 3.2 THERMODYNAMIC ANALYSIS

In the present work, a parametric study with fixed mass flow rate in LTC, and various condensing temperature, evaporating temperature and approach in the cascade-condenser have been conducted to determine the optimum condensing temperature of the cascade-condenser.

The following assumptions are made to simplify the thermodynamic analysis, including energy analysis.

1. All components are assumed to be a steady-state and steady-flow process. The changes in the potential and the kinetic energy of the components are negligible.
2. The high and low-temperature circuit compressors are non-isentropic.
3. The heat loss and pressure drops in the piping connecting the components are negligible.
4. All throttling devices are isenthalpic.

Based on the assumptions mentioned above, the equations for mass and energy balance are written for each component. Each component in the cascade refrigeration system, shown in Fig.7 considered as a control volume.

Mass balance

$$\sum_{in} m_r = \sum_{out} m_r \quad (1)$$

Energy balance

$$Q - W + \sum_{in} m_r h - \sum_{out} m_r h = 0 \quad (2)$$

Energy changes in each component of cascade refrigeration cycle are as follows:

**Evaporator:** evaporator is a heat exchanger which abstract heat from the cold room and this heat is called refrigeration effect, which is given by

$$Q_E = m_{r1} (h_1 - h_4) \quad (3)$$

**Compressor:** compressor is a work absorbing device in which, the isentropic work input to the compressor is expressed as

In compressor1:

$$W_{comp1s} = m_{r1} (h_{2s} - h_1) \quad (4)$$

Actual compressor work is specified by

$$W_{comp1} = \frac{m_{r1} (h_{2s} - h_1)}{\eta_{c1}}$$

$$W_{comp1} = m_{r1} (h_2 - h_1) \quad (5)$$

In compressor2

$$W_{comp2s} = m_{r2} (h_{6s} - h_5) \quad (6)$$

Actual compressor work is specified by

$$W_{comp2} = \frac{m_{r2} (h_{6s} - h_5)}{\eta_{c2}}$$

$$W_{comp2} = m_{r2} (h_6 - h_5) \quad (7)$$

**Condenser:** condenser is a heat exchanger in which heat rejected by the condenser to the environment or warm coolant is given as

$$Q_c = m_{r2} (h_6 - h_7) \quad (8)$$

**Expansion valve:** expansion valve is a device in which expansion of refrigerant occurred and enthalpy remains constant.

In expansion valve 1:

$$h_3 = h_4 \quad (9)$$

In expansion valve 2:

$$h_7 = h_8 \quad (10)$$

**Cascade condenser:** it acts as an evaporator in the high-temperature stage and as a condenser in the low-temperature stage. Cascade condenser is a heat exchanger in which all the heat released by the low-temperature-circuit condenser is rejected to the high-temperature-circuit evaporator.

Energy balance in cascade condenser

$$m_{r1} (h_2 - h_3) = m_{r2} (h_5 - h_8) \quad (11)$$

Where  $m_{r1}$  = mass flow rate in low temperature circuit

$m_{r2}$  = mass flow rate in low temperature circuit

### Coefficient of performance

The performance parameter, COP of a cascade system is defined as the ratio of the refrigerating effect produced in the evaporator to the total work input to all compressors in the system. It can be express by following expression.

$$COP = \frac{Q_E}{W_{comp1} + W_{comp2}} \quad (12)$$

### Volumetric cooling capacity

The volumetric cooling capacity is the cooling capacity per unit volume flow rate at the inlet to the compressor. It can be express by following expression

$$VCC = \frac{Q_E}{m_{r1} V_s} \quad (13)$$

Where  $V_s$  = specific volume at inlet of the compressor

#### 3.2.1 Cascade refrigeration system with liquid vapour heat exchanger

Energy balance in liquid vapour heat exchanger (assuming effectiveness as 1 for LVHE)

$$(h_{1s} - h_1) = (h_3 - h_{3L}) \quad (14)$$

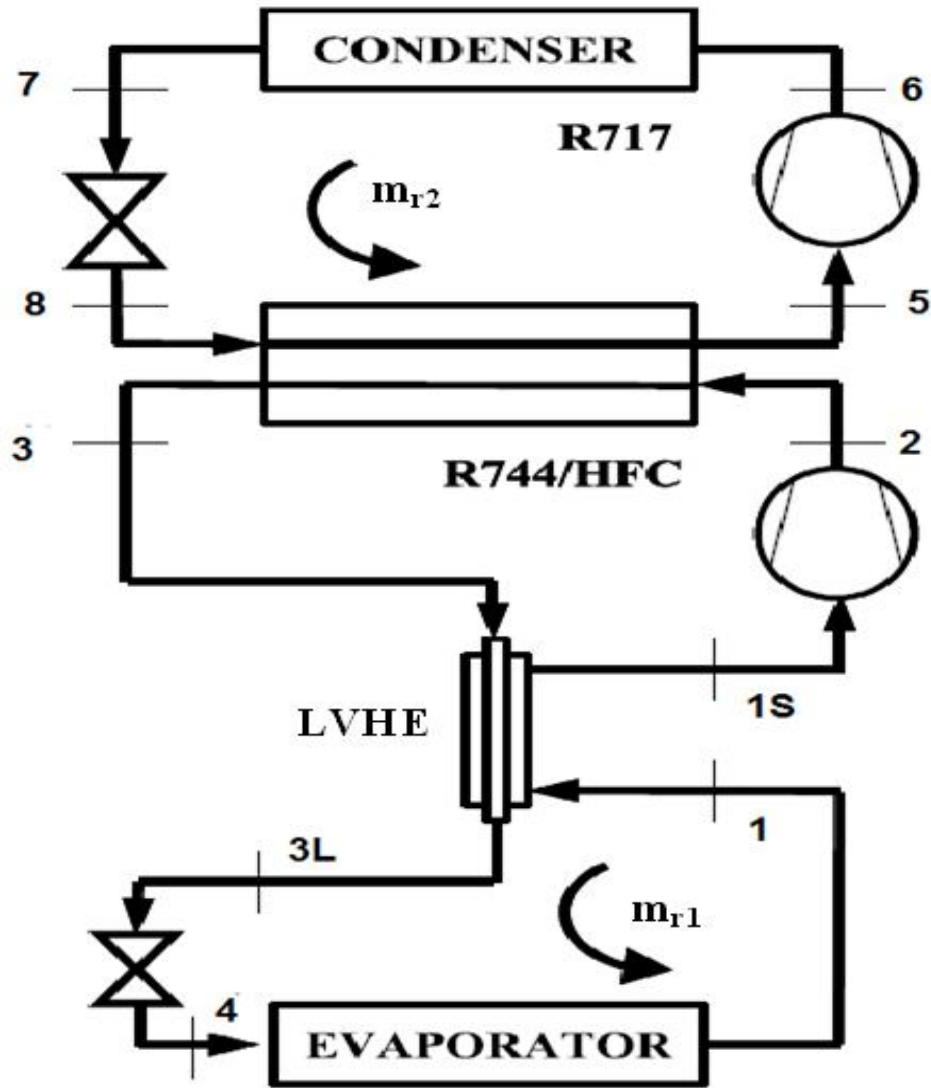


Fig.5 Schematic representation of cascade refrigeration cycle with liquid vapour heat exchanger.

### 3.3 Formulation of problem

Analysis of the cascade Refrigeration System shown in fig.3 and fig.5 has been carried out in this work.

The computer program has been developed in EES (Klein and Alvarado, 2005). The mixtures properties of the investigated blends (R744/R125, R744/R41, R744/R32, and R744/R23) were calculated by Ref Prop 7.0 (Huber et al. 2002) and used in EES program to calculate the performance parameters for a cascade refrigeration cycle.

For validation of program, results of the present work are compared with results of Nicola et al. (2005). Comparison of results for carbon dioxide (0.1 mole fraction) blend with R-125 and R-41 are shown in figure 6 and 7. The results from present work are 5% higher than that of Nicola et al. (2005).

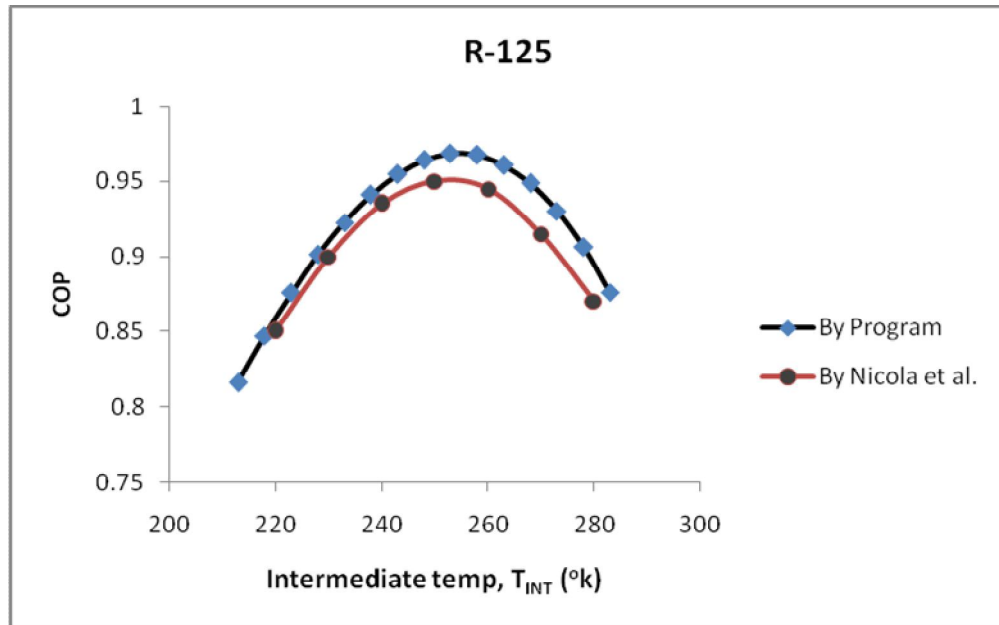


Fig.6 comparison of results with Nicola et al. results for R-125

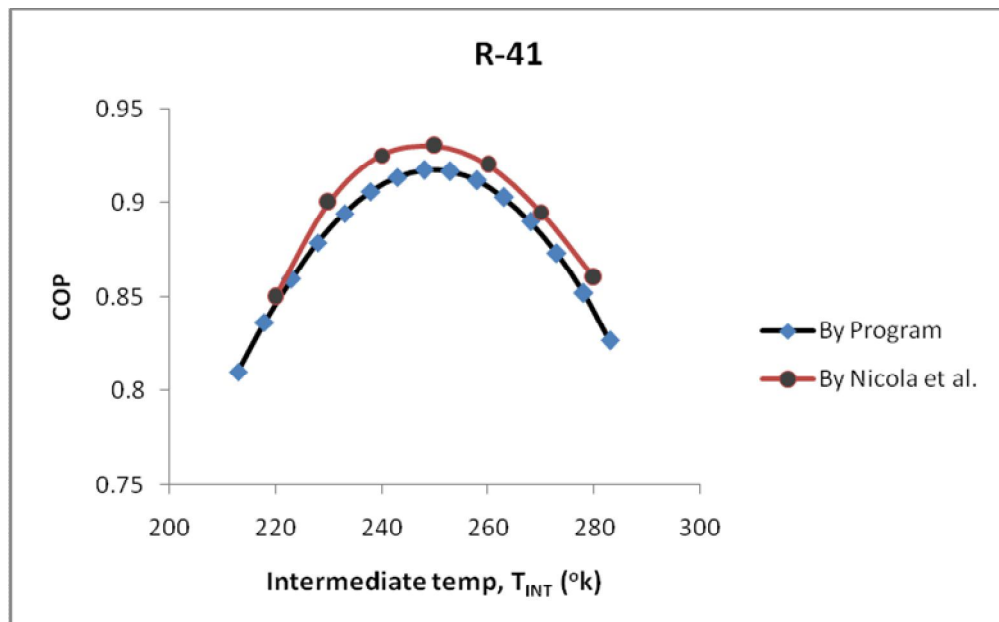


Fig.7 comparison of results with Nicola et al. results for R-41

The Input Parameters taken for computation of results are given below

Condenser Temperature	$T_c = 40 \text{ to } 50^\circ\text{C}$ in steps of $5^\circ\text{C}$
Evaporator Temperature	$T_E = -70^\circ\text{C}$
Cascade condenser temperature	$T_{MC} = 10 \text{ to } -60^\circ\text{C}$ in steps of $5^\circ\text{C}$
Approach	$A = 0, 5^\circ\text{C}$
Mass flow rate in low temperature circuit	$m_{r1} = 1 \text{ kg/sec}$
Compressor efficiency in low temperature circuit	$\eta_{c1} = 0.7$
Compressor efficiency in high temperature circuit	$\eta_{c2} = 0.7$
Refrigerant in high temperature circuit	R-717
Refrigerant in low temperature circuit	$\text{CO}_2$ blend with HFCs
HFCs used with carbon dioxide	R-23, R-32, R-41 and R-125
Subcooling (in HTC and LTC)	$0, 5^\circ\text{C}$
Superheating (in HTC and LTC)	$0, 10^\circ\text{C}$

By carrying out the thermodynamic analysis of the system for the conditions stated above the values at various state points of the cascade refrigeration cycle have been obtained. The computer program for the thermodynamic analysis of the system developed in EES has been given in Appendix A along with its flow diagram for computation procedure.

In the present work, following parameters have been computed.

- Total compressor work.
- Coefficient of performance of the cascade refrigeration cycle.
- Volumetric cooling capacity of the compressor.
- Ratio of mass flow rate in HTC and LTC.

Based on above we have computed optimal cascade condenser temperature.

In the present results computed from the compute program have been discussed.

### **4.1 MASS FLOW RATE IN HIGH TEMPERATURE CIRCUIT**

Figs 8 to 17 and Figs 22 to 31 show the variation of mass flow rate in high temp circuit for cascade refrigeration cycle with varying intermediate temperature for carbon dioxide blend with HFCs (R-23, R-32, R-41 and R-125) for different mole fraction. These figures show that the mass flow rate decreases with increase in intermediate temperature at a particular evaporator and condenser temperature for R-125 and R-23 due to decrease in load on cascade condenser. Mass flow rate increases with increase in intermediate temperature at a particular evaporator and condenser temperature for R-41 and R-32 due to increase of load on cascade condenser.

#### **4.1.1 Effect of superheating (10°C) and subcooling (5°C)**

Figs 22 to 31 show the effect of superheating of refrigerant inlet to compressor and subcooling of refrigerant outlet to condenser. By the comparison of figures with superheating and without superheating (Figs 8 to 17), mass flow rate increases around 3% by superheating and subcooling because load on cascade condenser increases due to combined effect of increase in compressor work and refrigerating effect.

#### **4.1.2 Effect of approach**

Approach is temperature difference between high temperature circuit evaporator and low temperature condenser. Figs 8 to 12 (with approach 0) and Figs 13 to 17 (with 5°C approach) show that by taking approach mass flow rate increases slightly by 0.9%.

#### **4.1.3 Effect of mole fraction of carbon dioxide**

Fig. 36 shows the variation of mole fraction of carbon dioxide in mixture with HFCs. Figure shows that by increasing mole fraction of carbon dioxide mass flow rate decreases for R-125 and R-23 and increases for R-41 and R-32.



#### **4.1.4 Effect of condenser temperature**

Figs 18 to 21 and Figs 32 to 35 present the effect of condenser temperature. By increasing condenser temperature 5°C, increase in mass flow rate in high temperature circuit is around 2%.

#### **4.1.5 Effect of liquid vapour heat exchanger**

Figs 38 and 37 show that by using liquid vapour heat exchanger in low temperature circuit, mass flow rate in high temperature circuit increases by around 3%.

### **4.2 TOTAL COMPRESSOR WORK**

Figs 39 to 48 and Figs 53 to 62 show the variation of total compressor work for cascade refrigeration cycle with varying intermediate temperature for carbon dioxide blend with HFCs (R-23, R-32, R-41 and R-125) for different mole fraction. These figures show that the total compressor work decreases with increase in intermediate temperature at a particular evaporator and condenser temperature. Total compressor work for R-41 mixture is highest among all mixtures followed by R-32, R-23 and R-125 respectively.

This happens because for a given condenser and evaporator temperature, as the intermediate temperature increases, the low temperature circuit compressor's work done ( $W_{COMP1}$ ) increases but the high temperature circuit compressor's work done ( $W_{COMP2}$ ) decreases, and the combined effect of these is to decrease work done.

#### **4.2.1 Effect of superheating (10°C) and subcooling (5°C)**

Figs 53 to 62 show the effect of superheating of refrigerant inlet to compressor and subcooling of refrigerant outlet to condenser. By the comparison of figures with superheating and without superheating (Figs 39 to 48), increase in that total compressor work is around 7% by superheating and subcooling.

#### **4.2.2 Effect of approach**

Approach is temperature difference between high temperature circuit evaporator and low temperature condenser. Figs 39 to 43 (with approach 0) and Figs 44 to 48 (with 5°C approach) show that by taking approach total compressor work increases because the low temperature circuit compressor's work done ( $W_{COMP1}$ ) decreases but the high

temperature circuit compressor's work done ( $W_{\text{COMP2}}$ ) increases, and the combined effect of these is to increase the total compressor work by around 8%.

#### **4.2.3 Effect of mole fraction of carbon dioxide**

Fig. 67 shows the variation of mole fraction of carbon dioxide in mixture with HFCs. Figure shows that by increasing mole fraction of carbon dioxide total compressor work increases for R-125 and R-23 and decreases for R-41 and R-32.

#### **4.2.4 Effect of condenser temperature**

Figs 49 to 52 and Figs 63 to 66 present the effect of condenser temperature. By increasing condenser temperature  $5^{\circ}\text{C}$ , total compressor work is increased by 8%.

#### **4.2.5 Effect of liquid vapour heat exchanger**

Figs 68 and 69 show that by using liquid vapour heat exchanger in low temperature circuit, total compressor work increases by 3%.

### **4.3 COEFFICIENT OF PERFORMANCE**

Figs 70 to 79 and Figs 84 to 93 show the variation of COP for cascade refrigeration cycle with varying intermediate temperature for carbon dioxide blend with HFCs (R-23, R-32, R-41 and R-125) for different mole fraction. These figures show that the COP increases with increase in intermediate temperature up to a temperature (optimum temperature) after this COP decreases with increase in intermediate temperature at a particular evaporator and condenser temperature. COP for R-125 mixture is highest among all mixtures followed by R-32, R-41 and R-23 respectively. Optimum temperature range for cascade refrigeration system is  $240^{\circ}\text{K}$  to  $260^{\circ}\text{K}$ .

This happens because for a given condenser and evaporator temperature, as the intermediate temperature increases, the refrigerating effect and the work done by the compressor both decreases, and combined effect of these is to increase COP up to optimum temperature but after optimum temperature COP decreases.

#### **4.3.1 Effect of superheating ( $10^{\circ}\text{C}$ ) and subcooling ( $5^{\circ}\text{C}$ )**

Figs 84 to 93 show the effect of superheating of refrigerant inlet to compressor and subcooling of refrigerant outlet to condenser. By the comparison of figures with

superheating and without superheating (Figs 70 to 79), COP increases by superheating and subcooling, this happens because by superheating work done increases and by subcooling refrigerating effect also increases, and combined effect of these is to increase COP. For R-125 mixture (with carbon dioxide) effect of superheating and subcooling on increase in COP is very high. At optimum temperature COP increased around 1% by superheating and subcooling.

#### **4.3.2 Effect of approach**

Approach is temperature difference between high temperature circuit evaporator and low temperature condenser. Figs 70 to 74 (with approach 0) and Figs 75 to 79 (with 5°C approach) show that by taking approach 5°C, COP decreases as around 8%, because of increase in compressor work. Optimum temperature is shifted 2% to higher side by taking approach.

#### **4.3.3 Effect of mole fraction of carbon dioxide**

Fig. 98 show the variation of mole fraction of carbon dioxide in mixture with HFCs. Figure show that by increasing mole fraction of carbon dioxide COP affect slightly. For R-23 and R-41, COP decreases with increase in mole fraction of carbon dioxide. For R-125, COP increases up to mole fraction 0.3 and after this decrease up to mole fraction 0.9. For R-32, COP decreases up to mole fraction 0.8 and after this COP increases.

#### **4.3.4 Effect of condenser temperature**

Figs 80 to 83 and Figs 94 to 97 present the effect of condenser temperature. By increasing condenser temperature 5°C, COP decrease by around 7%, because by increasing condenser temperature work done by compressor is increased. Optimum temperature is shifted around 1.5% to higher side by increasing condenser temperature.

#### **4.3.5 Effect of liquid vapour heat exchanger**

Figs 99 and 100 show that by using liquid vapour heat exchanger in low temperature circuit, COP decreases by 1%.

### **4.4 VOLUMETRIC COOLING CAPACITY**

Figs 101 to 110 and Figs 115 to 124 show the variation of volumetric cooling capacity for cascade refrigeration cycle with varying intermediate temperature for carbon dioxide

blend with HFCs (R-23, R-32, R-41 and R-125) for different mole fraction. These figures show that the volumetric cooling capacity decreases with increase in intermediate temperature at a particular evaporator and condenser temperature. Volumetric cooling capacity for R-23 mixture is highest among all mixtures followed by R-41, R-32 and R-125 respectively.

This happens because for a given condenser and evaporator temperature, as the intermediate temperature increases, the low temperature circuit compressor's work done ( $W_{COMP1}$ ) increases but the high temperature circuit compressor's work done ( $W_{COMP2}$ ) decreases, and combined effect of these is to decrease the total compressor work decreases and by decreasing total compressor work volumetric cooling capacity also decreases.

#### **4.4.1 Effect of superheating 10°C and subcooling 5°C**

Figs 115 to 124 show the effect of superheating of refrigerant inlet to compressor and subcooling of refrigerant outlet to condenser. By the comparison of figures with superheating and without superheating (Figs 101 to 110), volumetric cooling capacity is increased by superheating and subcooling.

#### **4.4.2 Effect of approach**

Approach is temperature difference between high temperature circuit evaporator and low temperature condenser. Figs 101 to 105 (with approach 0) and Figs 106 to 110 (with 5°C approach) show that by taking approach in cascade condenser volumetric cooling capacity does not affect.

#### **4.4.3 Effect of mole fraction of carbon dioxide**

Fig. 129 shows the variation of mole fraction of carbon dioxide in mixture with HFCs. Figure show that by increasing mole fraction of carbon dioxide volumetric cooling capacity increases.

#### **4.4.4 Effect of condenser temperature**

Figs 111 to 114 and Figs 125 to 128 present the effect of condenser temperature. By increasing condenser temperature volumetric cooling capacity does not change.

## Variation in Mass Flow Rate in high temp circuit without superheating and subcooling for cascade system

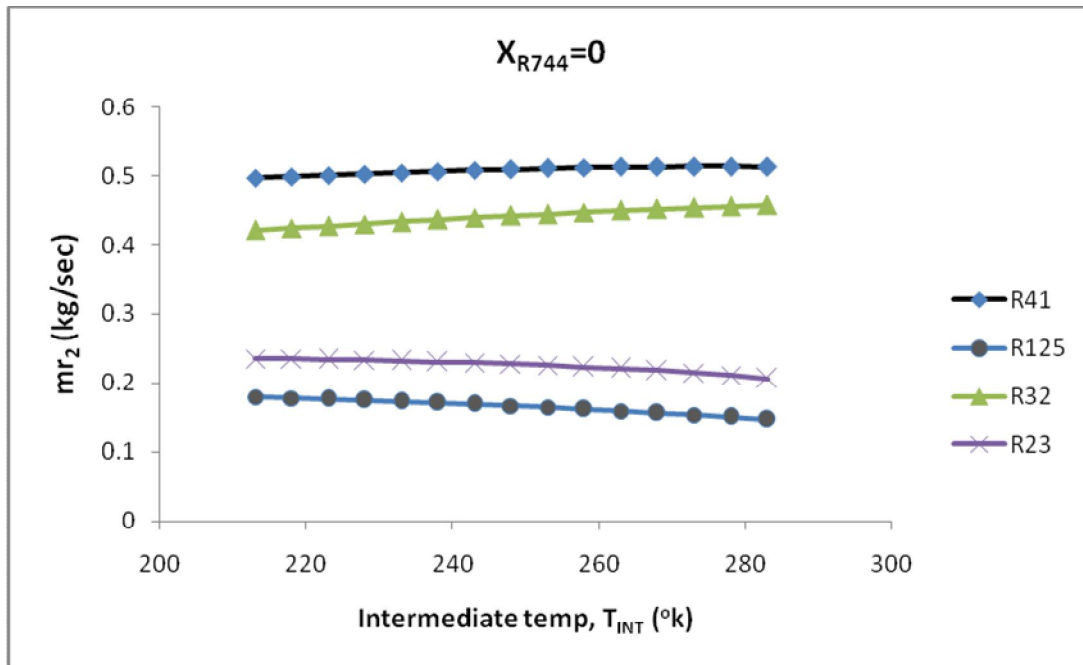


Fig.8 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.0 mole fraction as low temperature working fluid with approach 0°C.

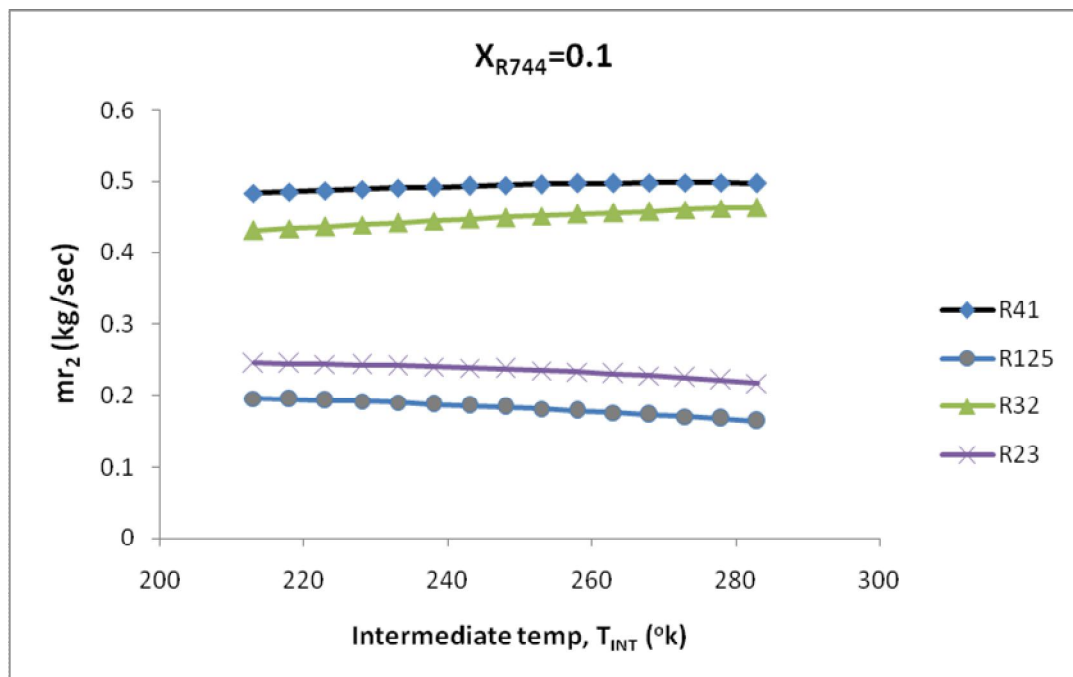


Fig.9 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

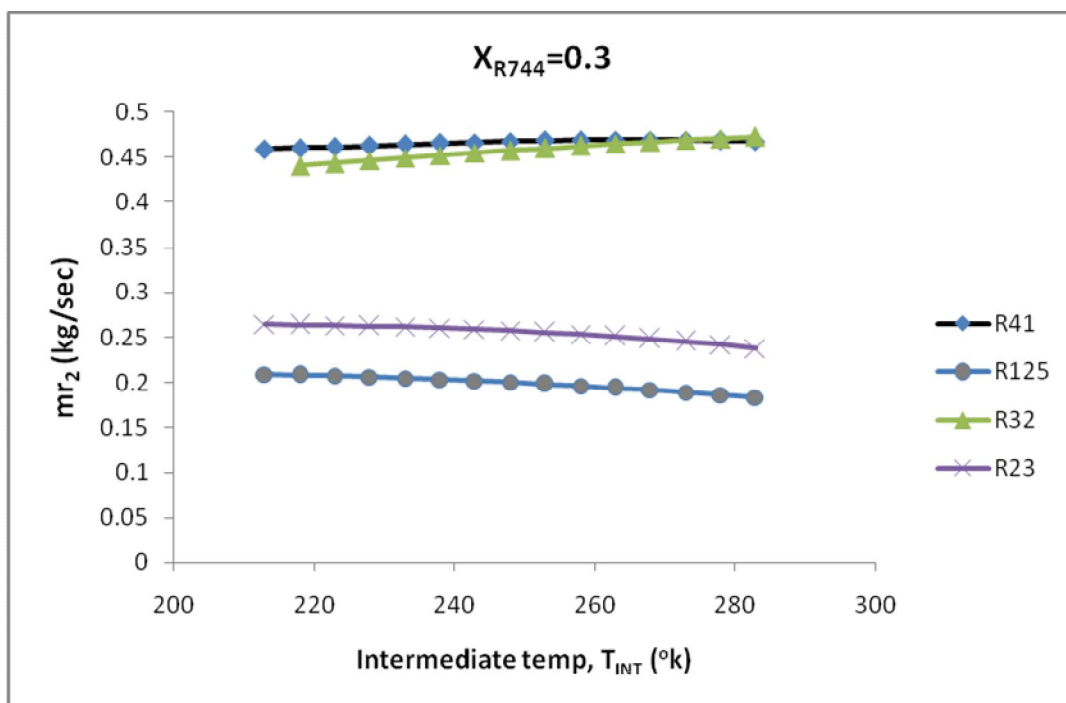


Fig.10 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

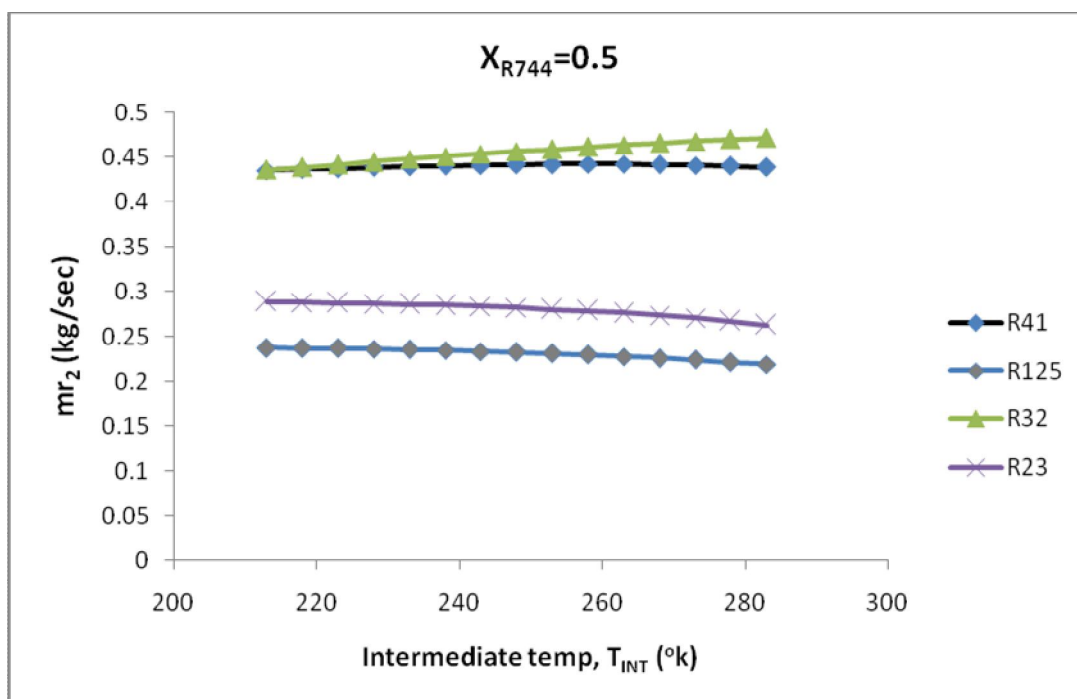


Fig.11 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

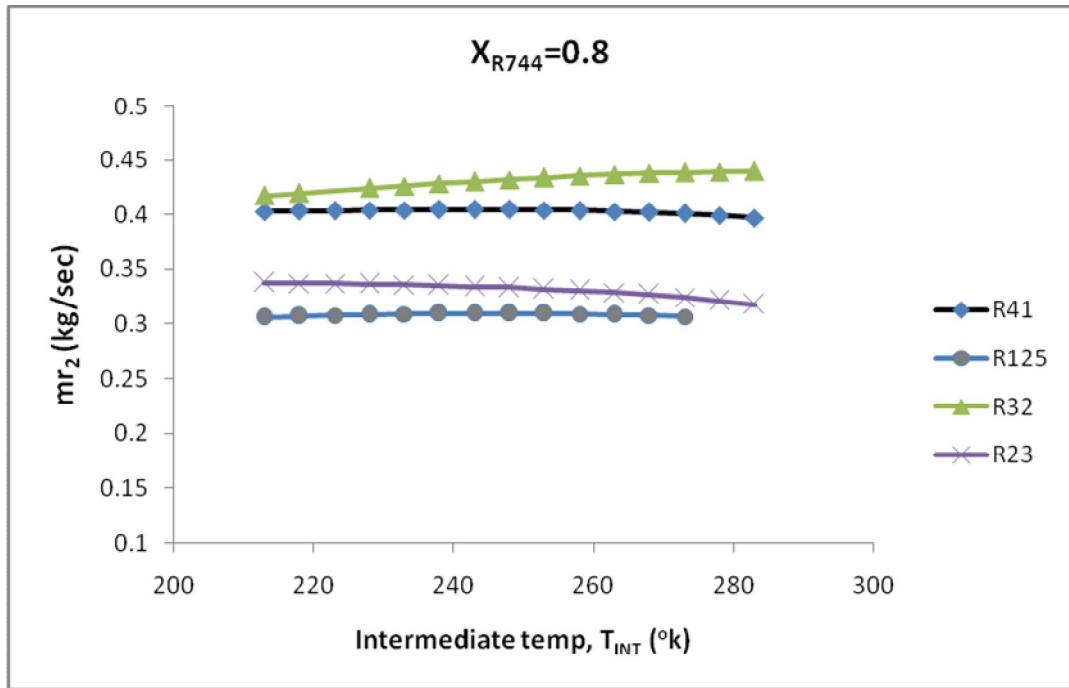


Fig.12 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

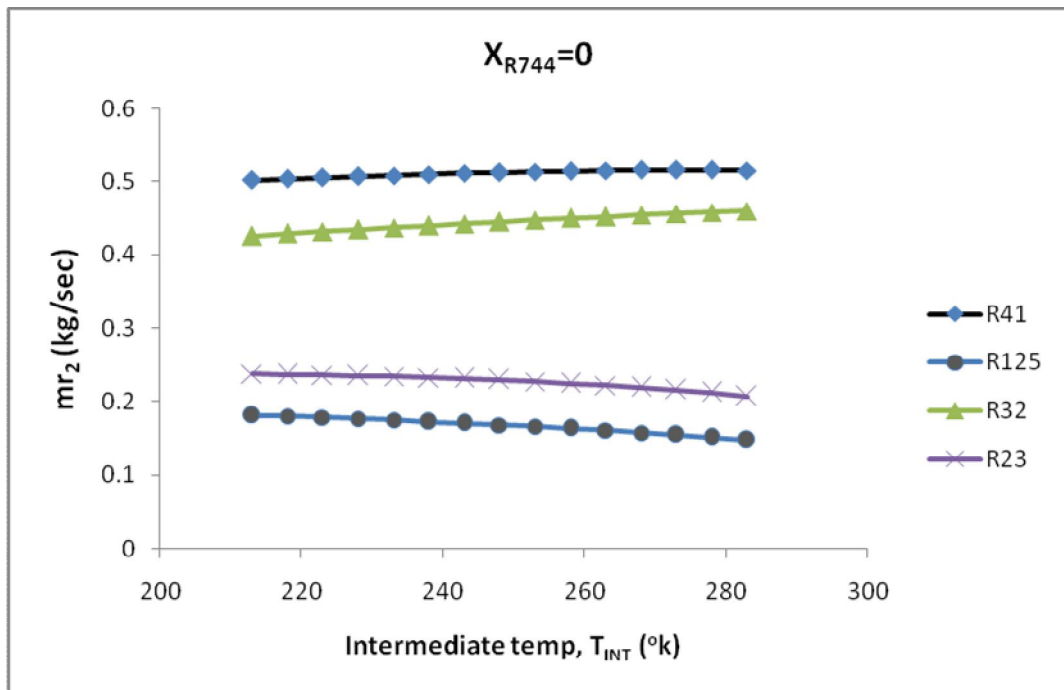


Fig.13 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.0 mole fraction as low temperature working fluid with approach 5°C.

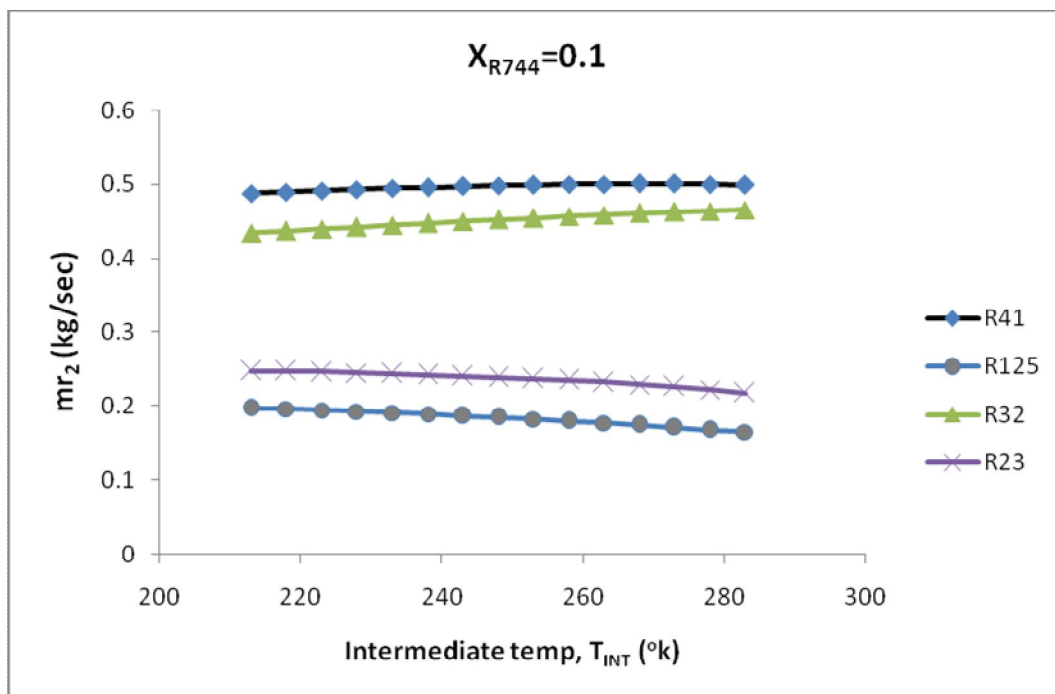


Fig.14 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

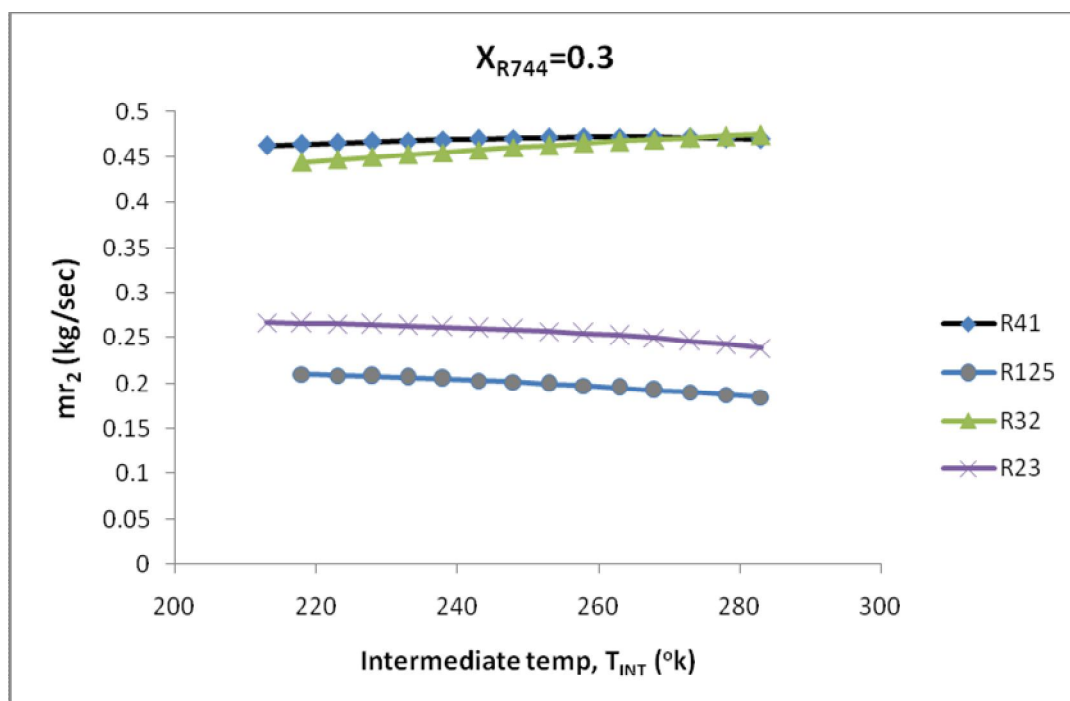


Fig.15 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.



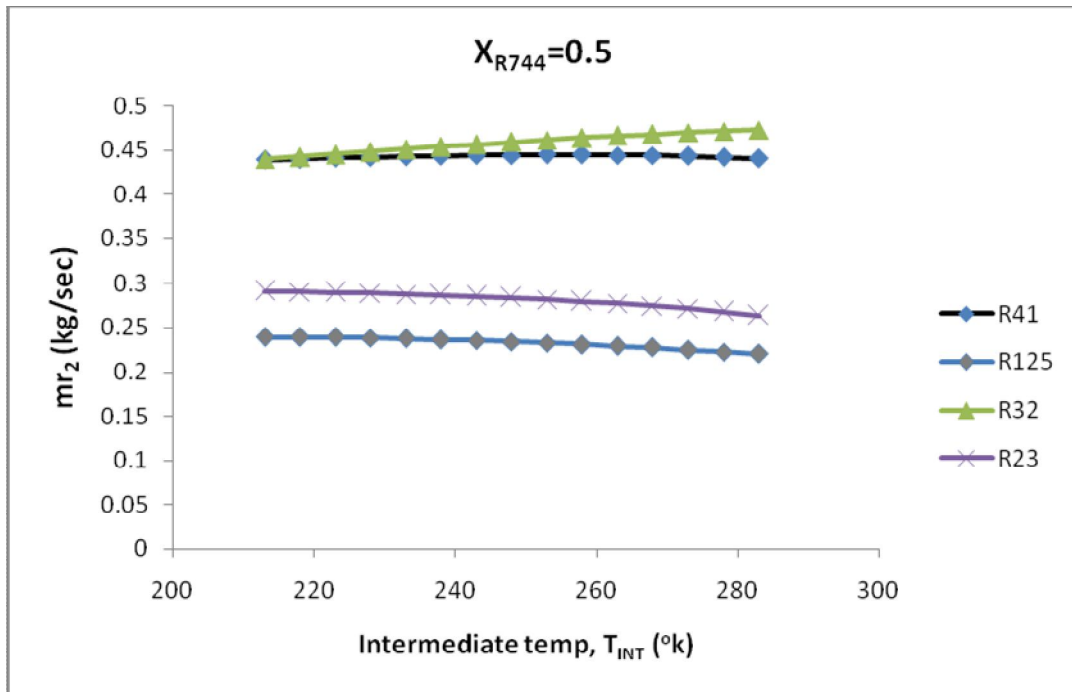


Fig.16 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

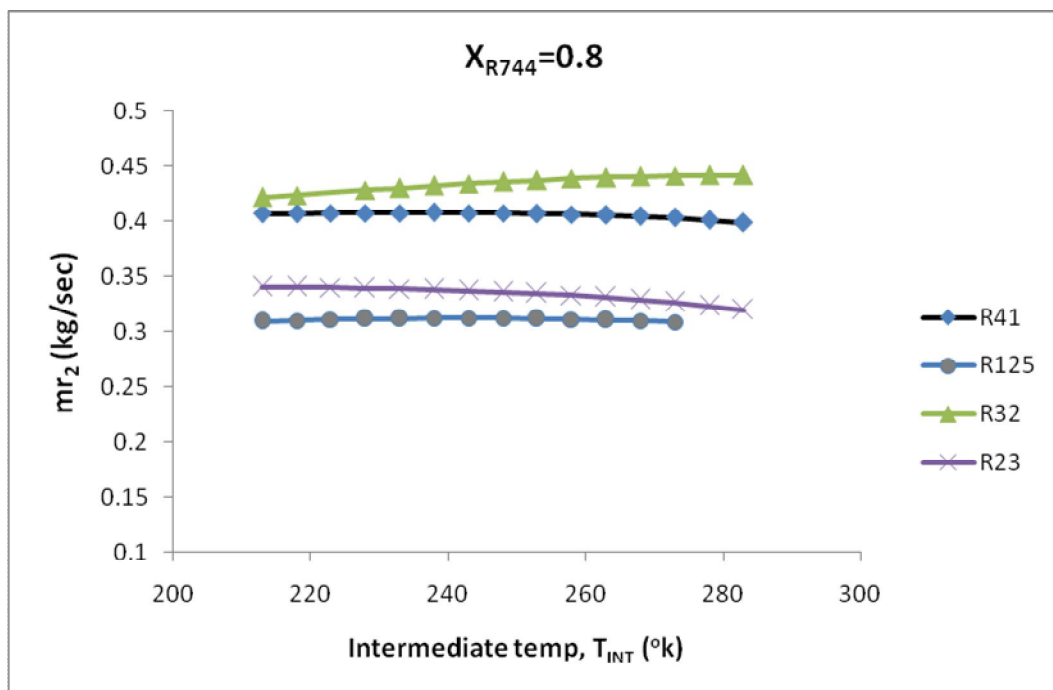


Fig.17 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.

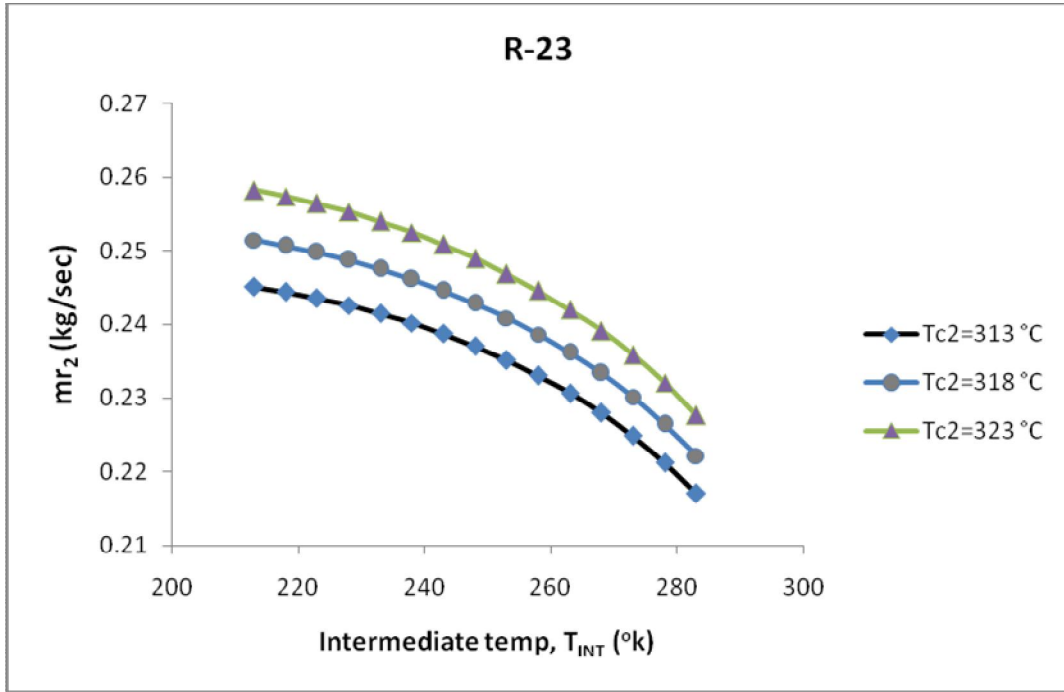


Fig.18 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

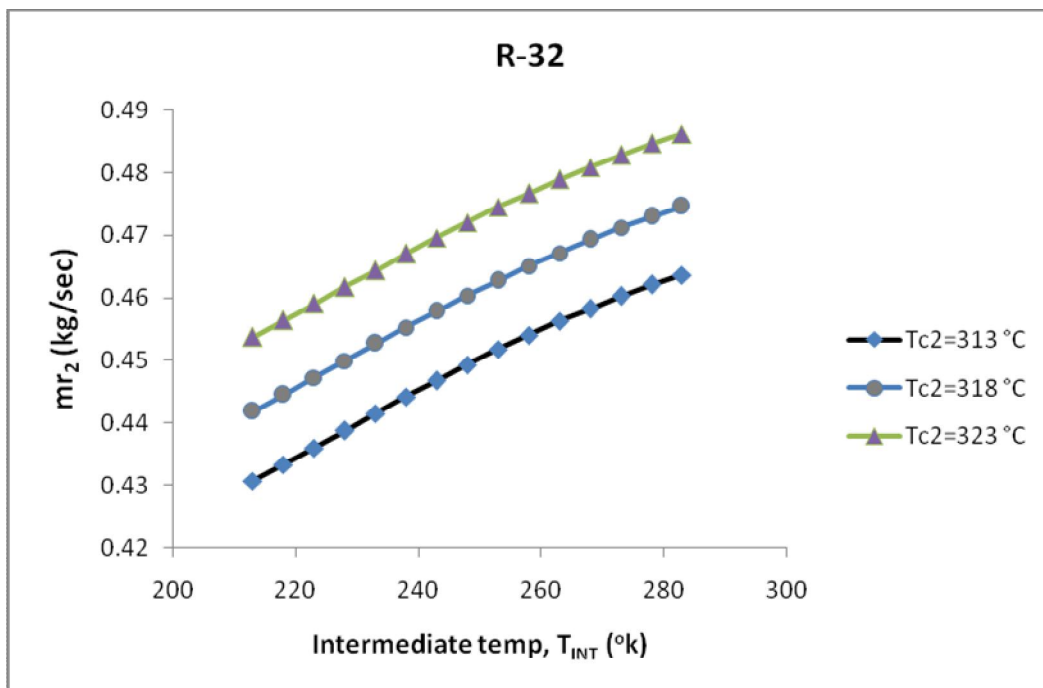


Fig.19 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

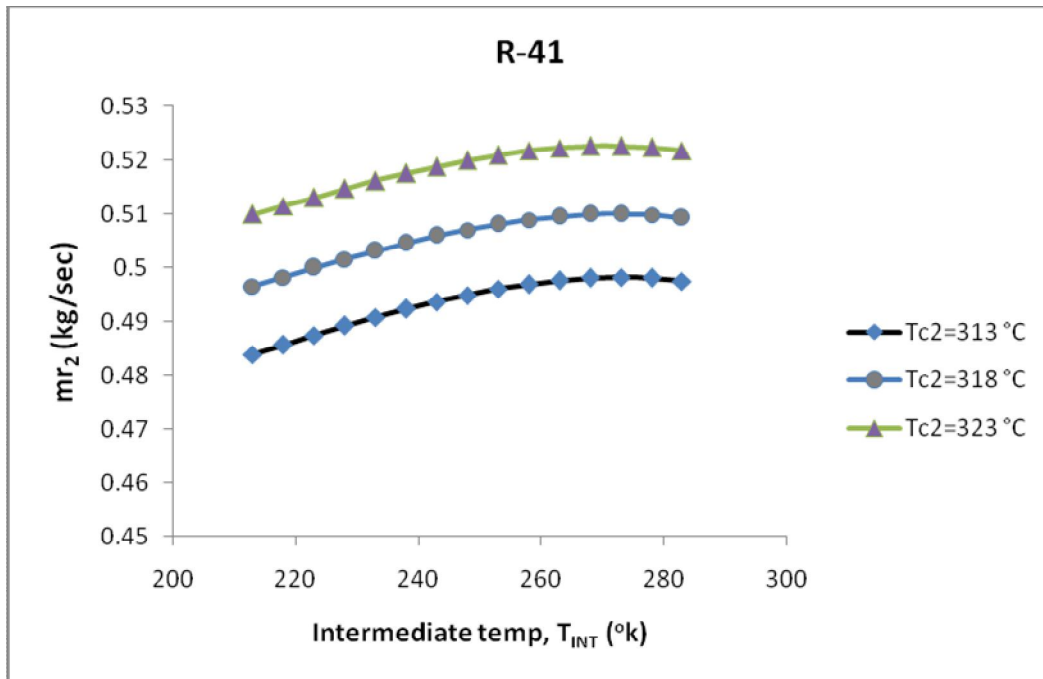


Fig.20 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

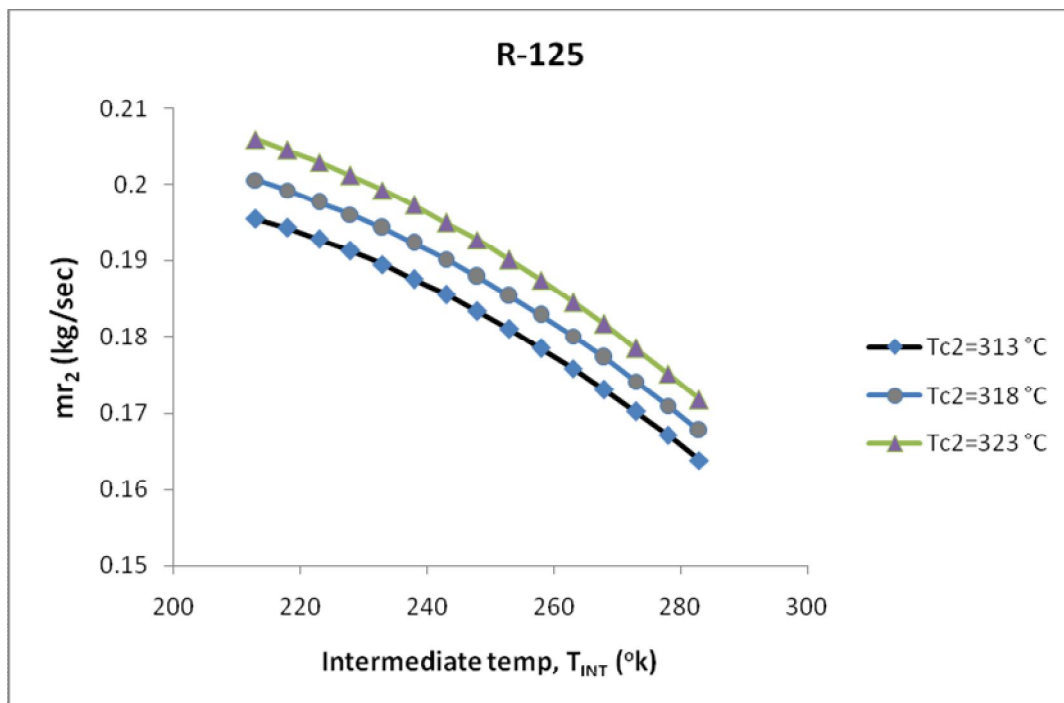


Fig.21 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

### Variation in Mass Flow Rate in high temp circuit with superheating 10°C and subcooling 5°C for cascade system

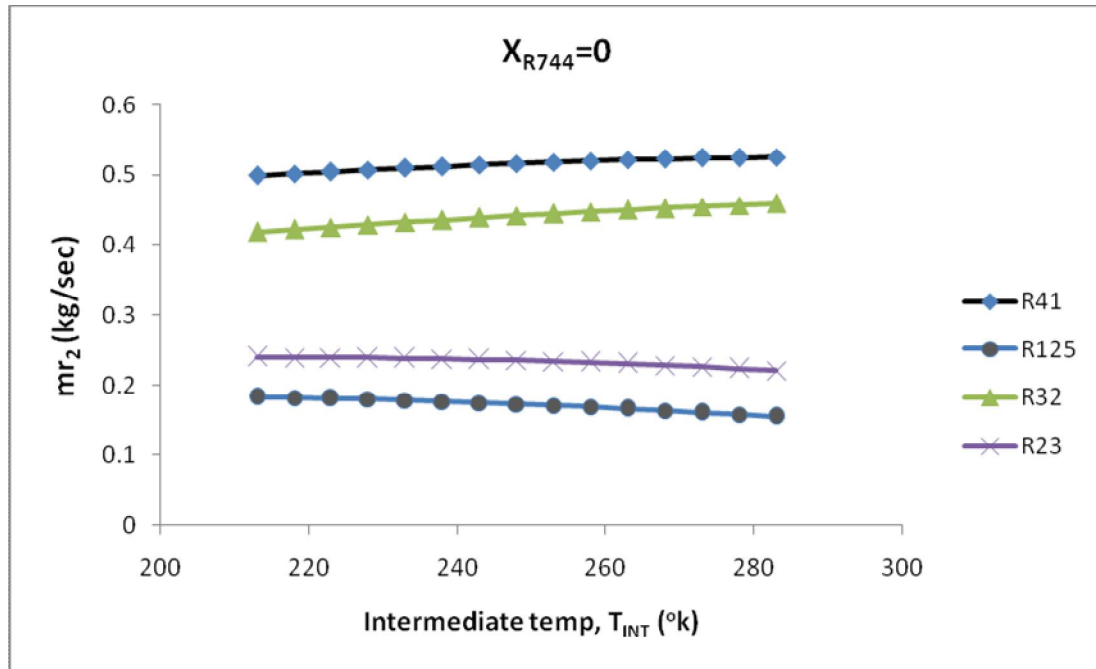


Fig.22 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.0 mole fraction as low temperature working fluid with approach 0°C.

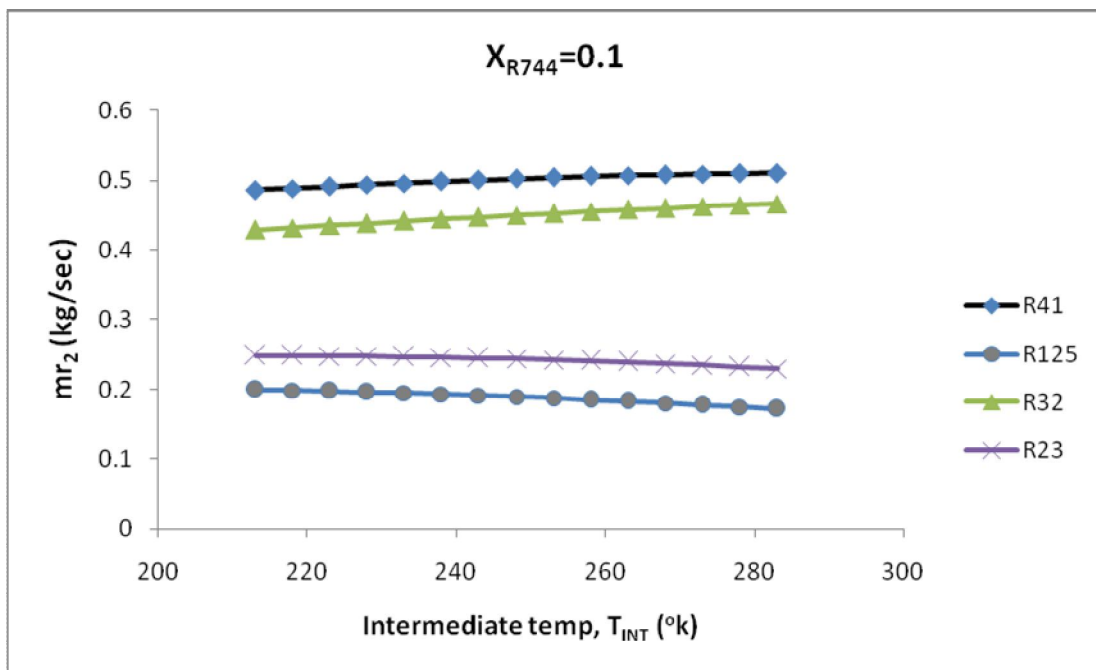


Fig.23 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

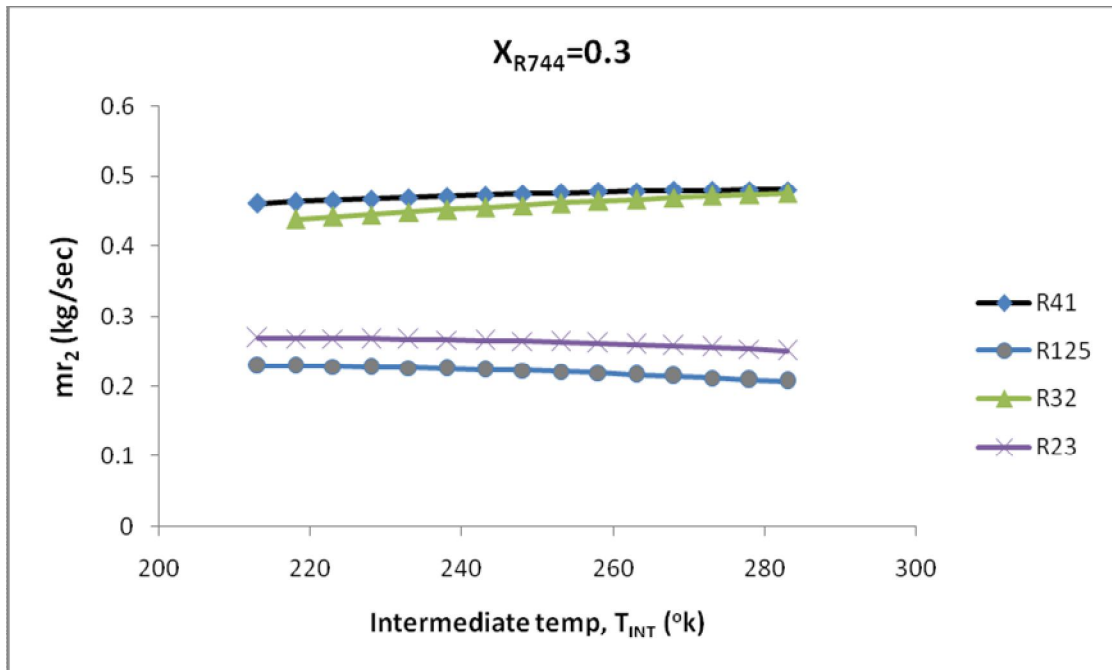


Fig.24 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach  $0^{\circ}C$ .

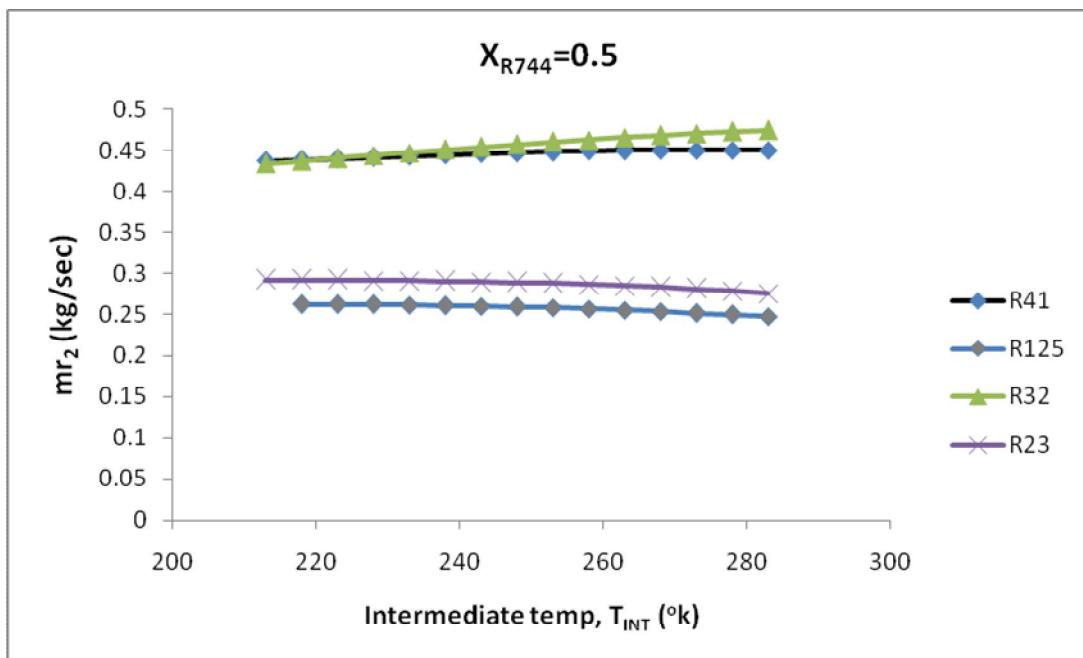


Fig.25 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach  $0^{\circ}C$ .

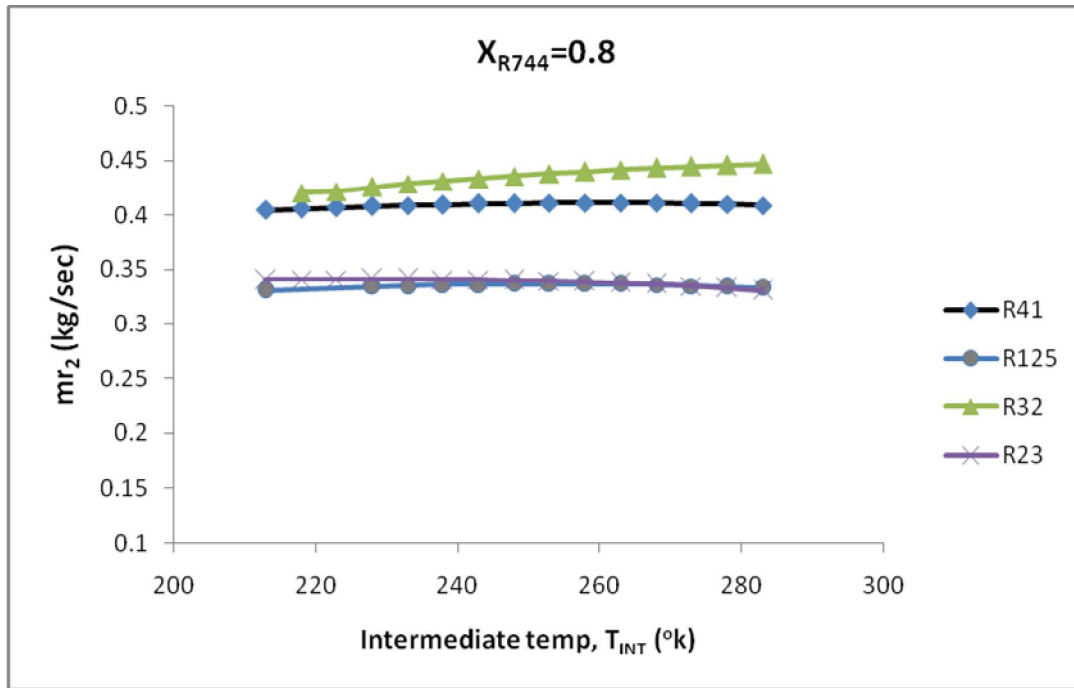


Fig.26 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

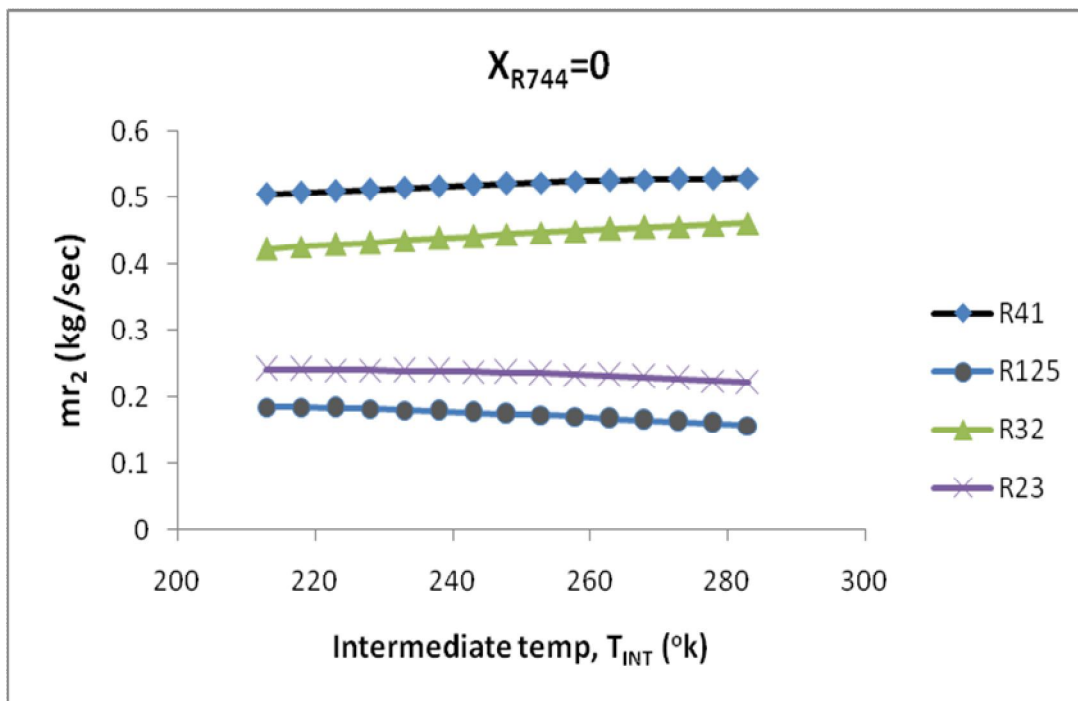


Fig.27 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

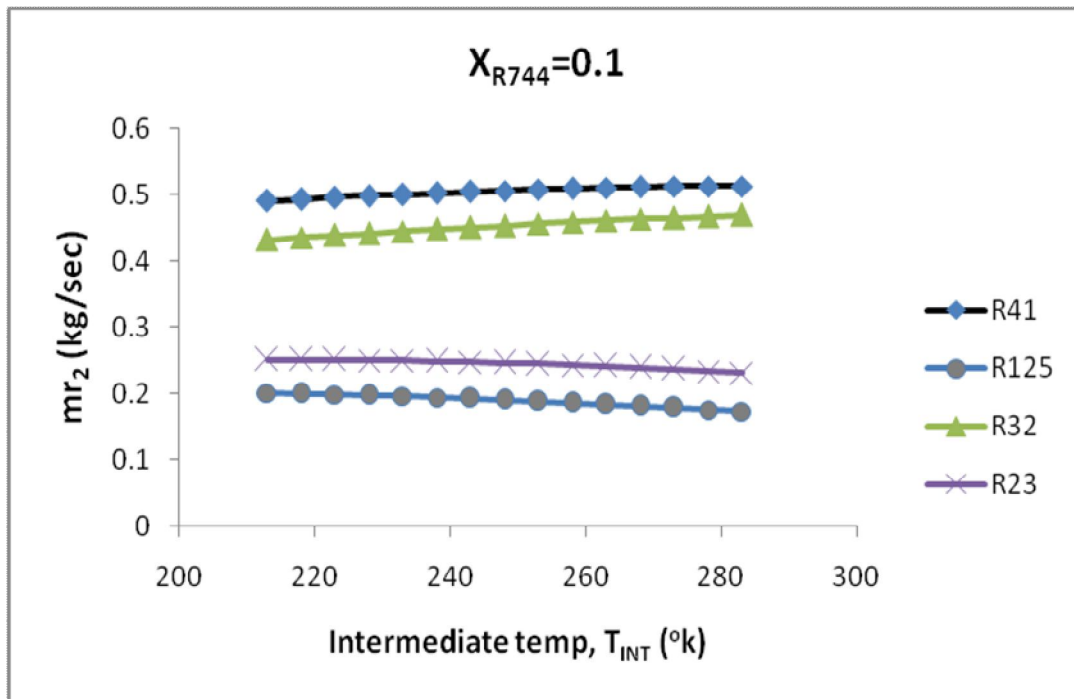


Fig.28 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

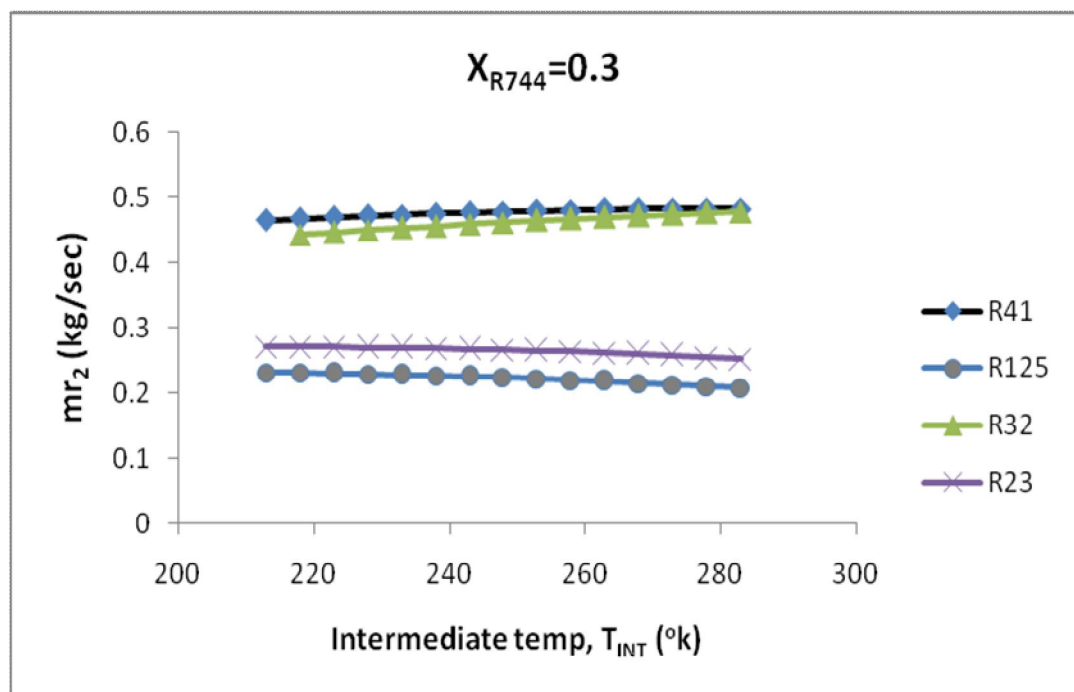


Fig.29 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.

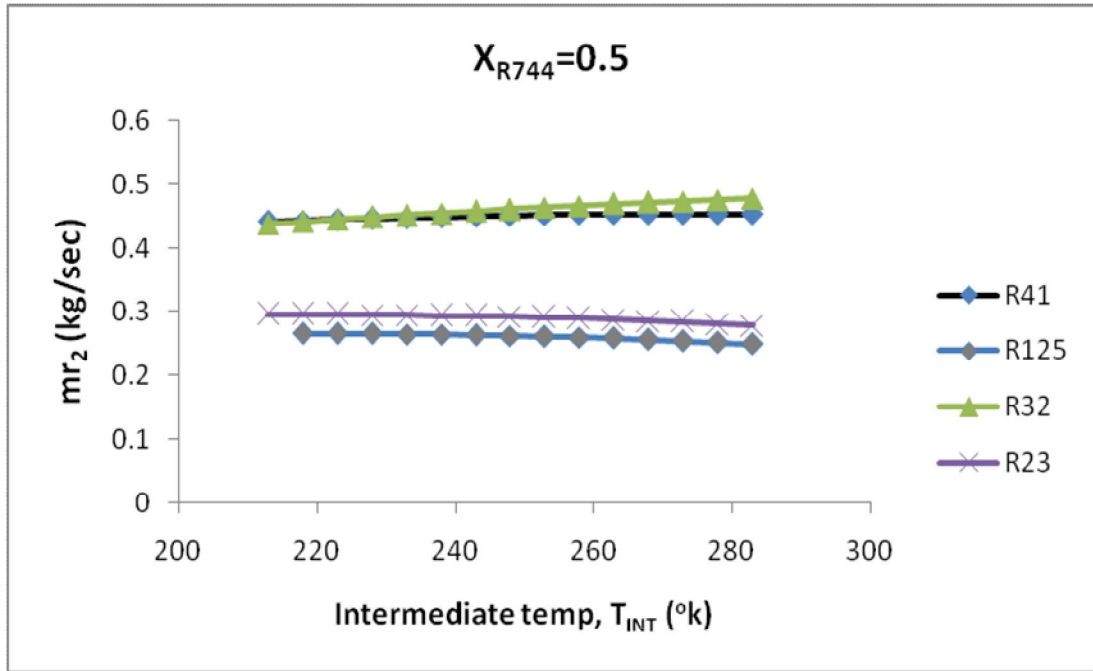


Fig.30 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

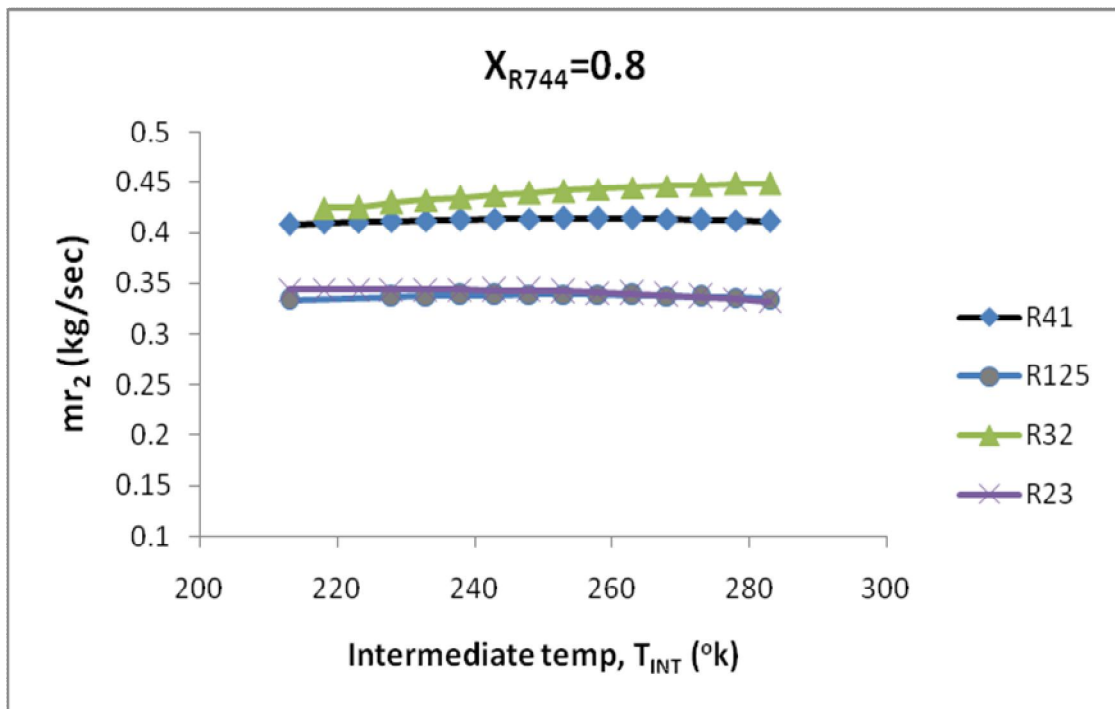


Fig.31 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.



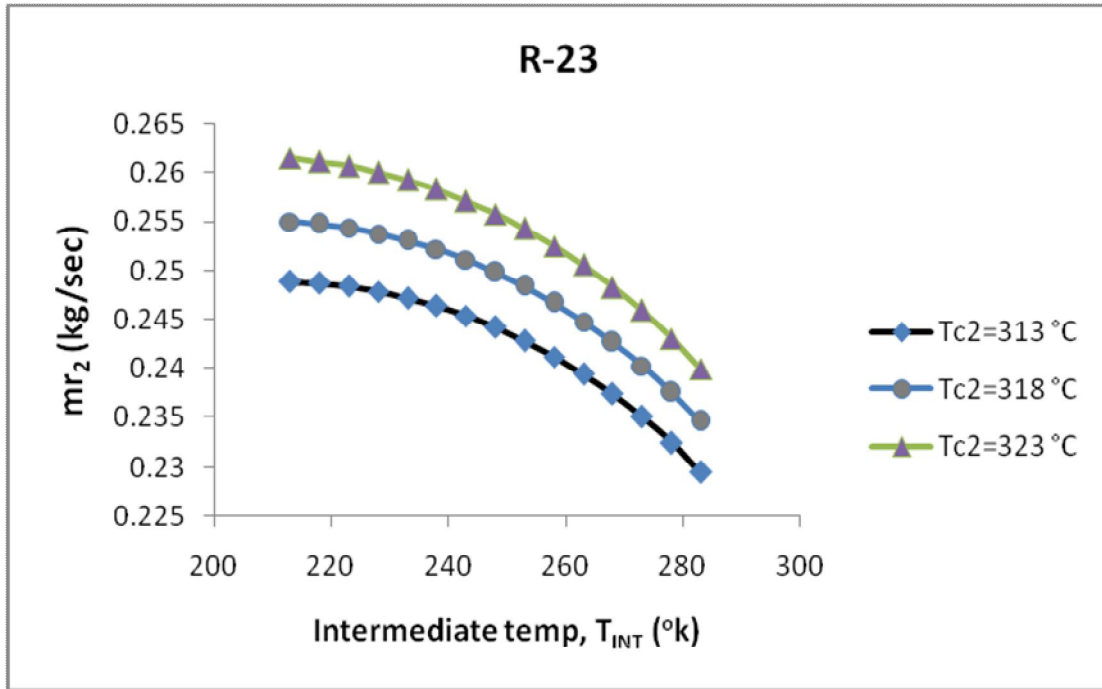


Fig.32 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

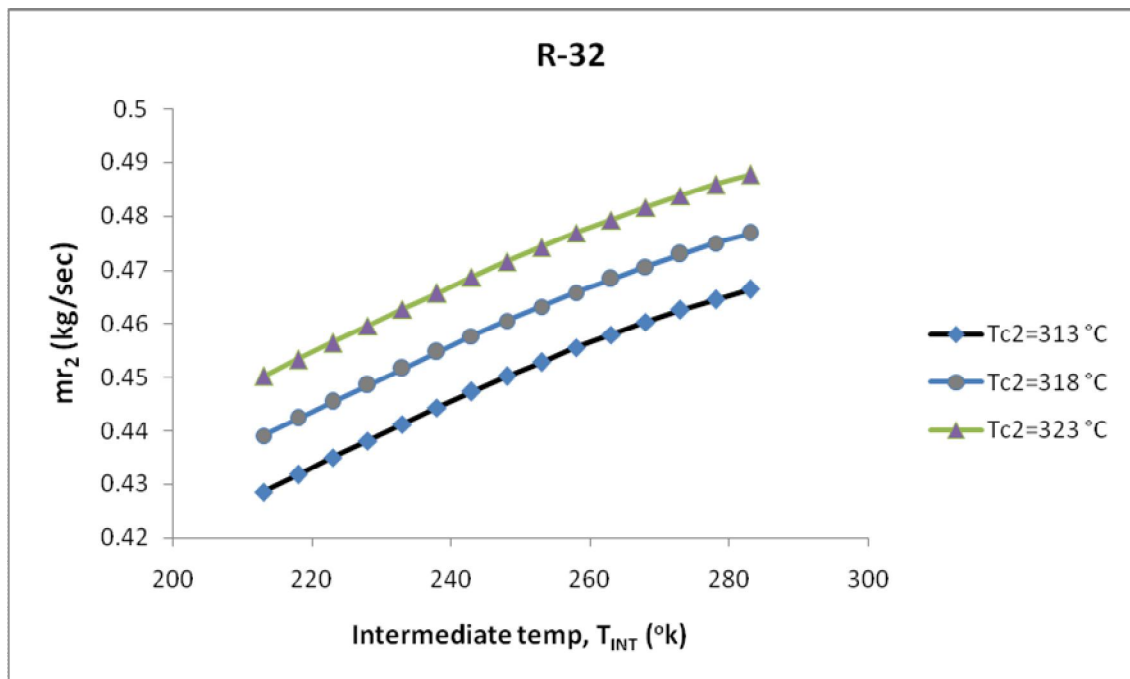


Fig.33 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

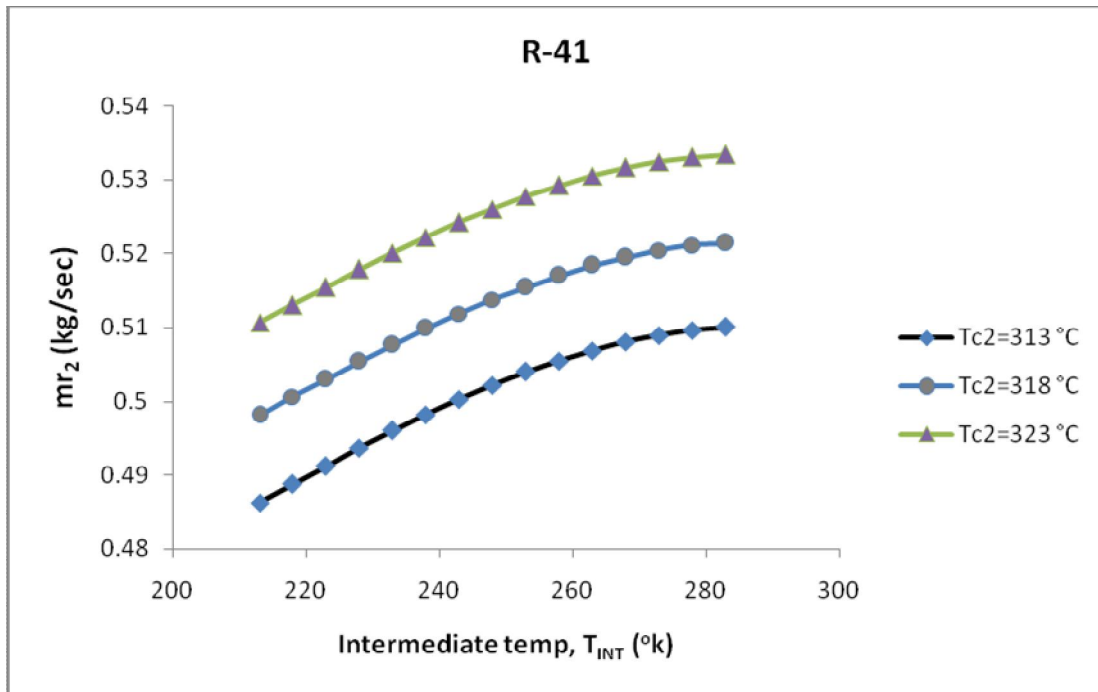


Fig.34 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

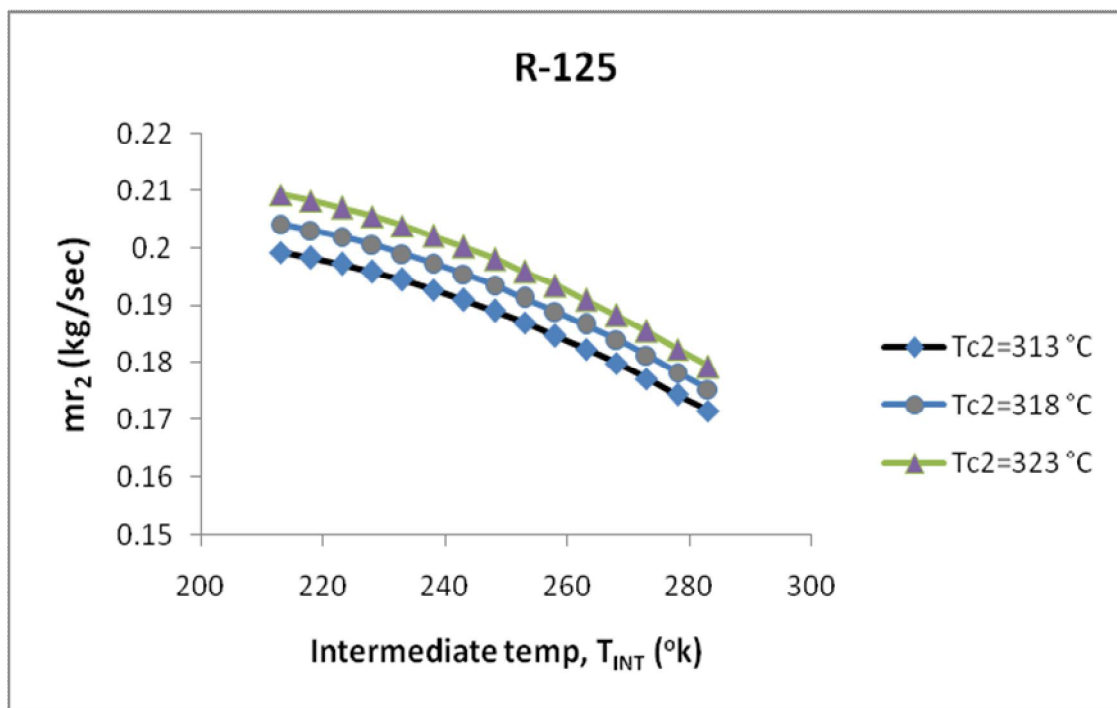


Fig.35 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

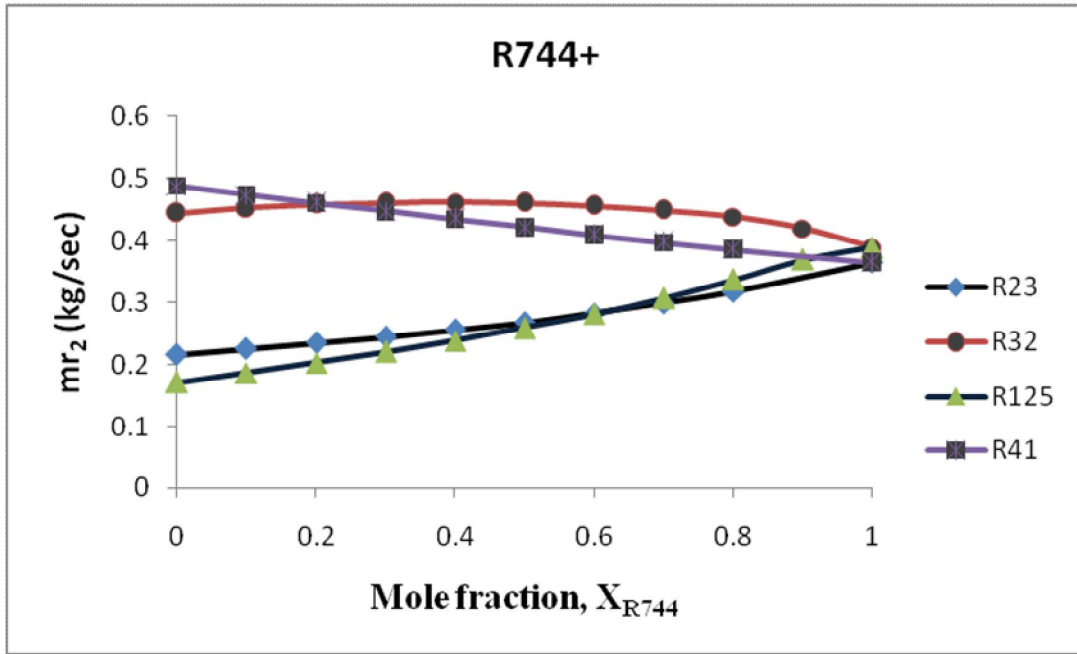


Fig.36 Variation in mass flow rate in high temp circuit with  $CO_2$  mole fraction for cascade system operating with R744 blends as low temperature working fluid.

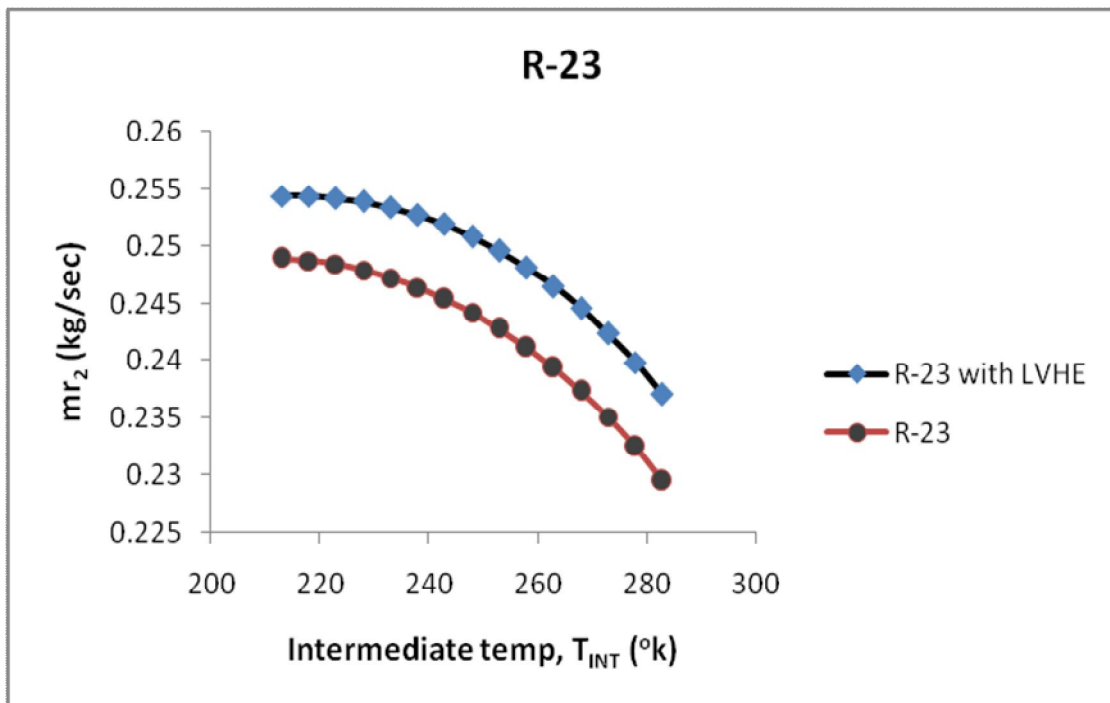


Fig.37 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 by taking LVHE effectiveness 1.

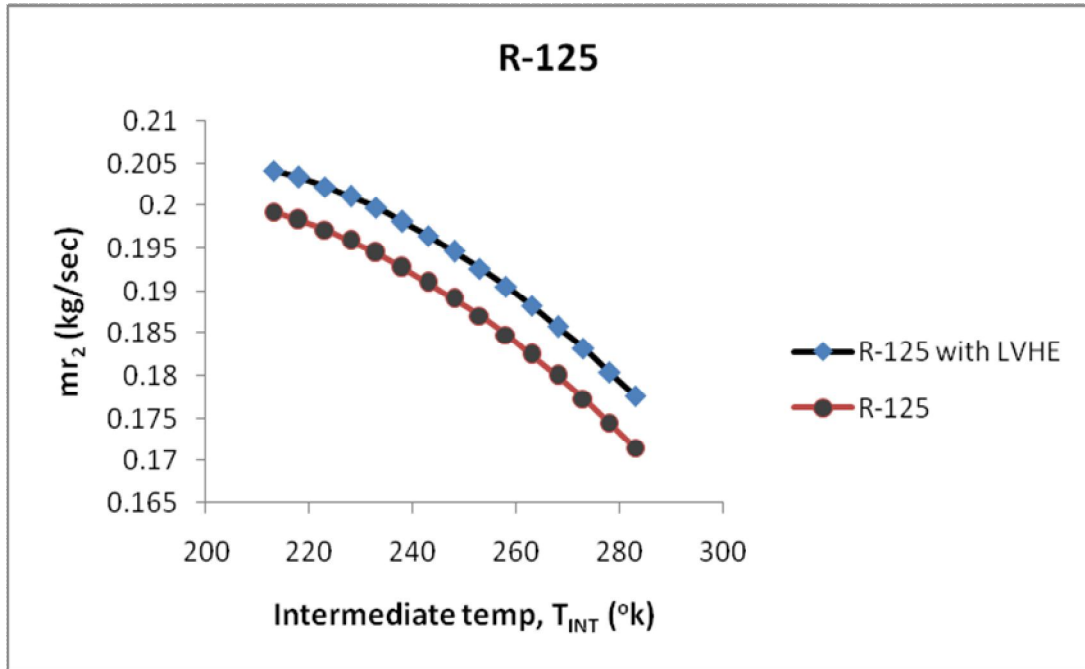


Fig.38 Variation in mass flow rate in high temp circuit with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 taking LVHE effectiveness 1.

### Variation in total compressor work without superheating and subcooling for cascade system

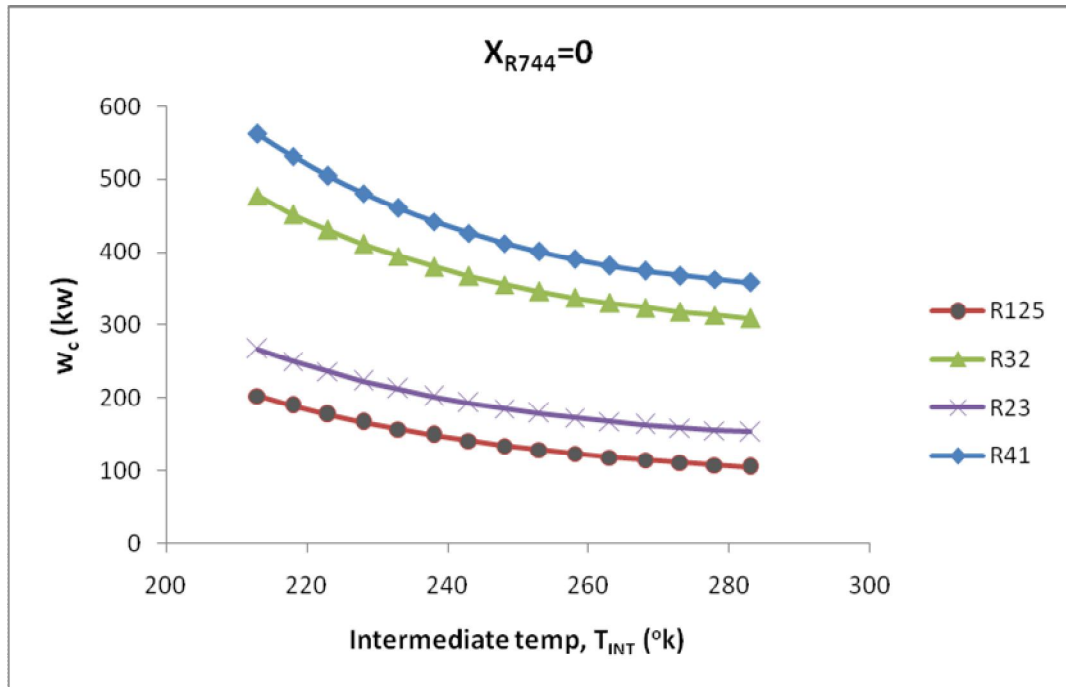


Fig.39 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 0°C.

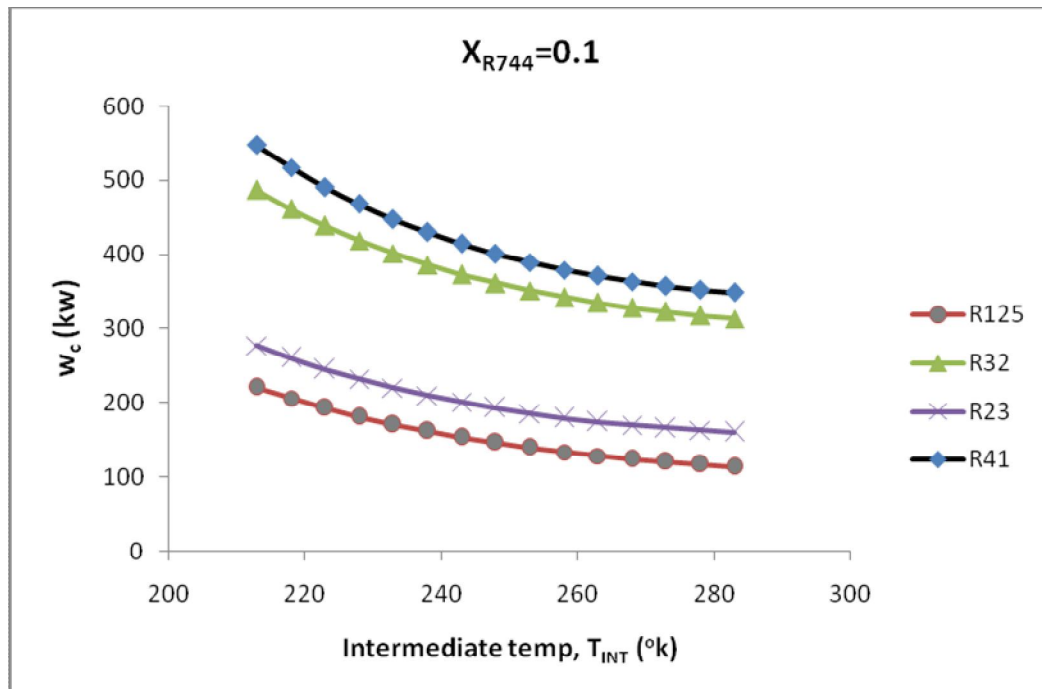


Fig.40 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

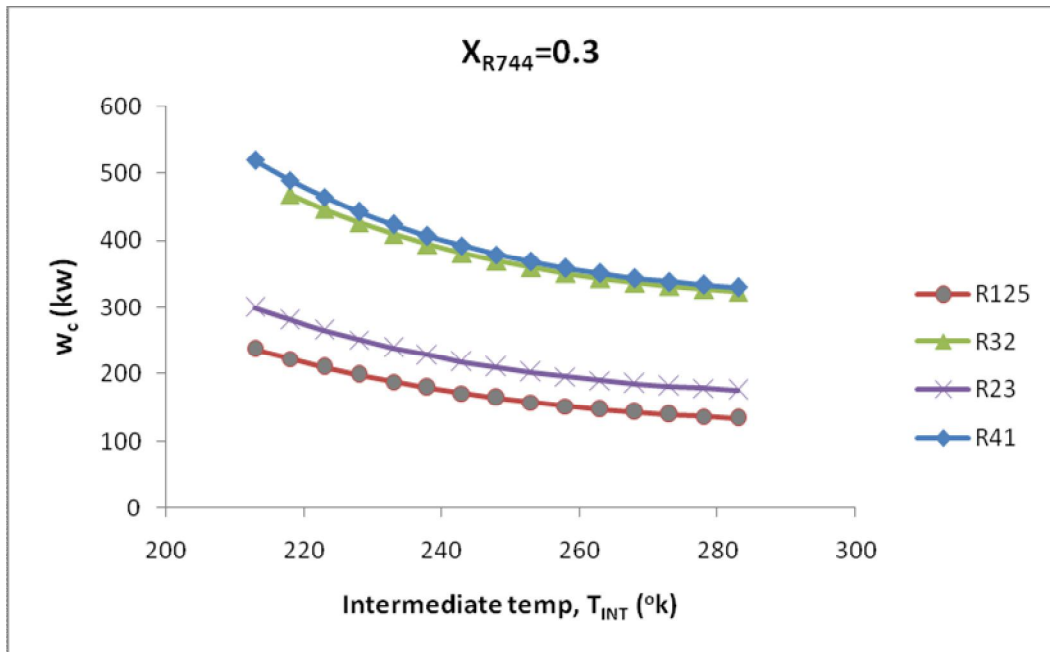


Fig.41 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

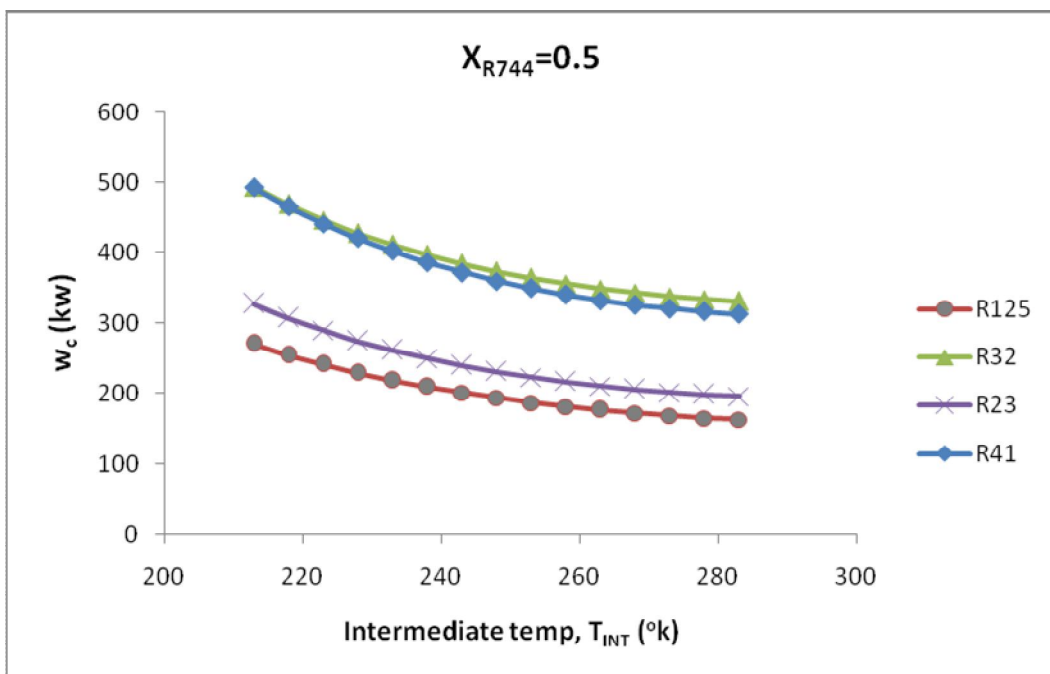


Fig.42 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

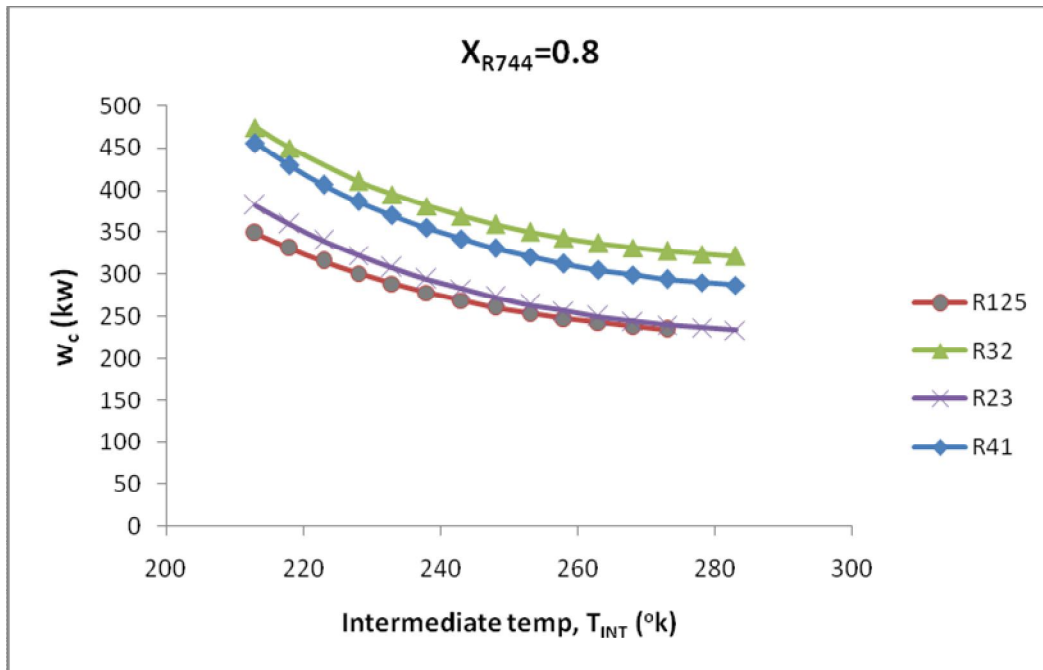


Fig.43 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

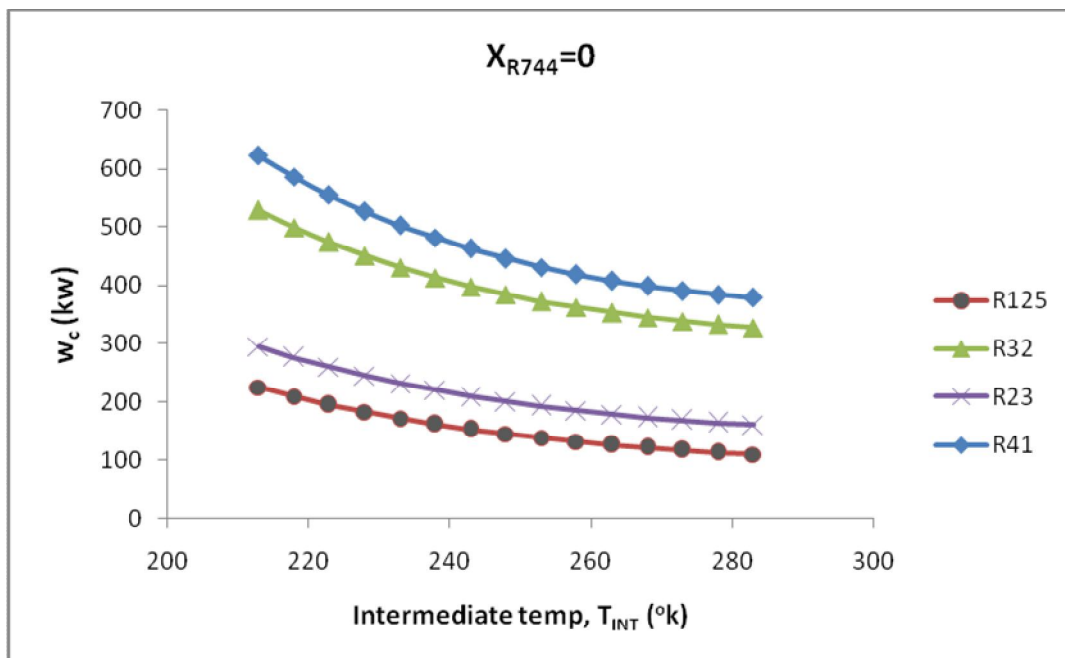


Fig.44 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

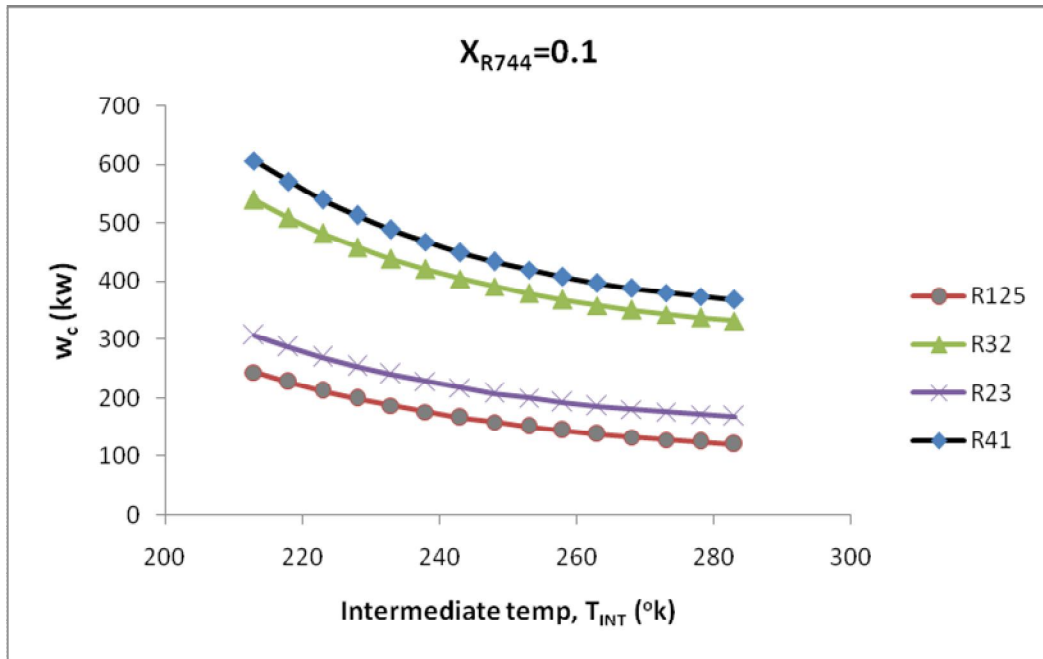


Fig.45 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

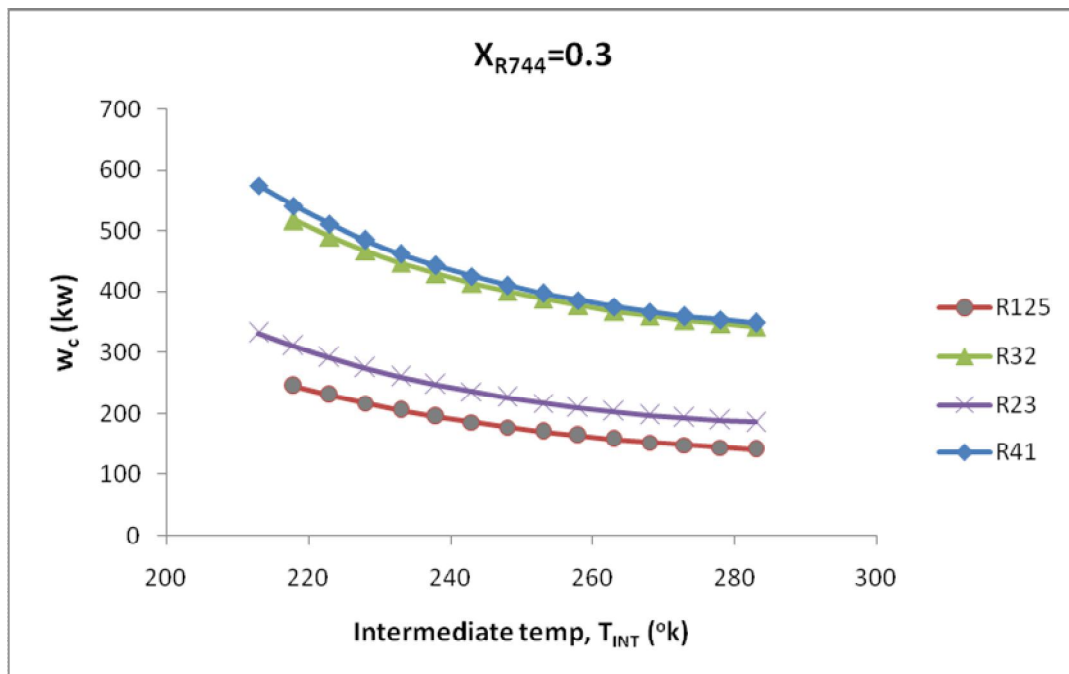


Fig.46 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.



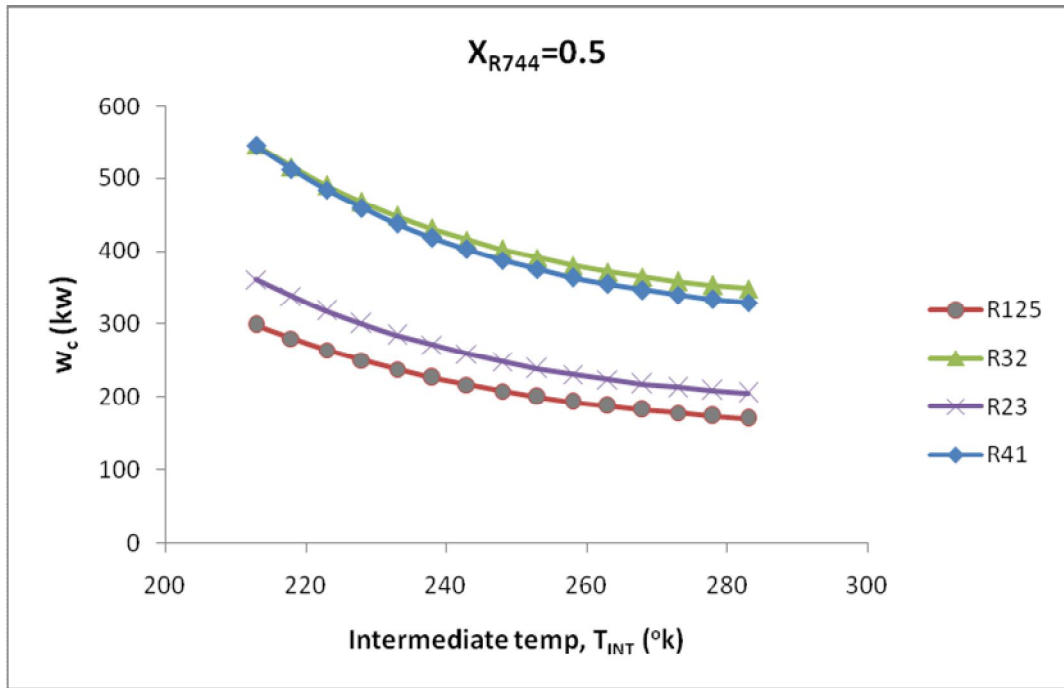


Fig.47 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

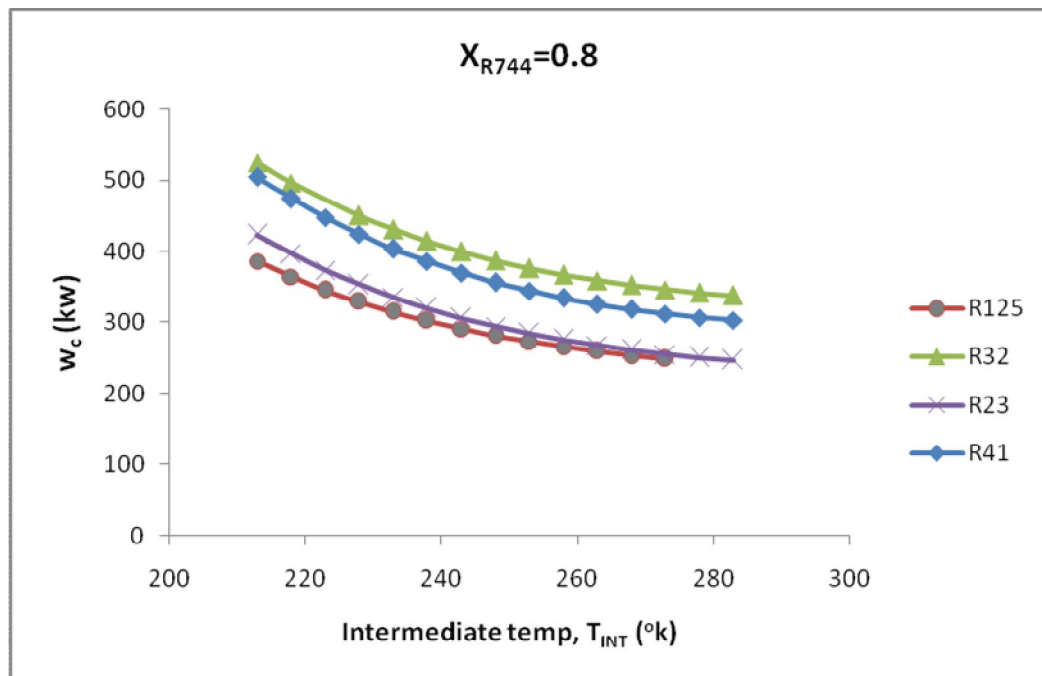


Fig.48 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.

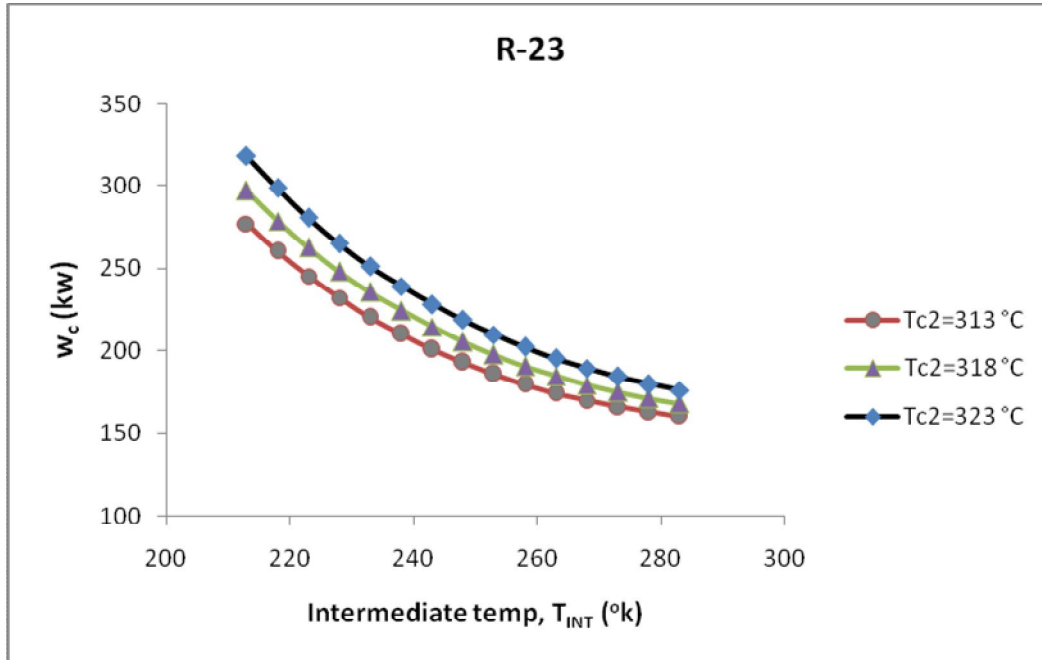


Fig.49 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

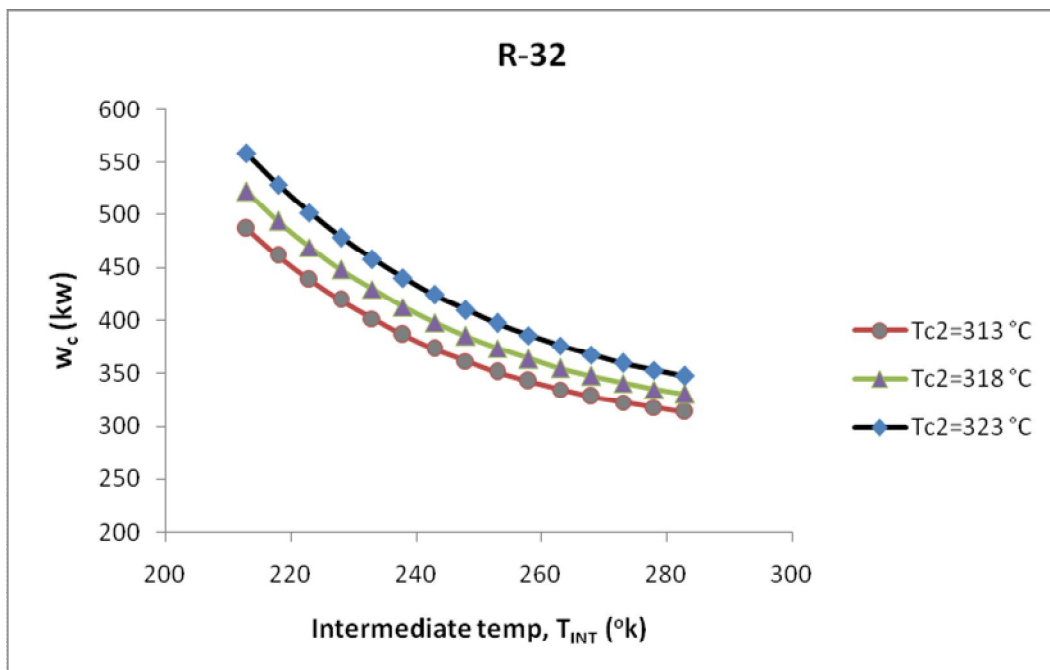


Fig.50 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

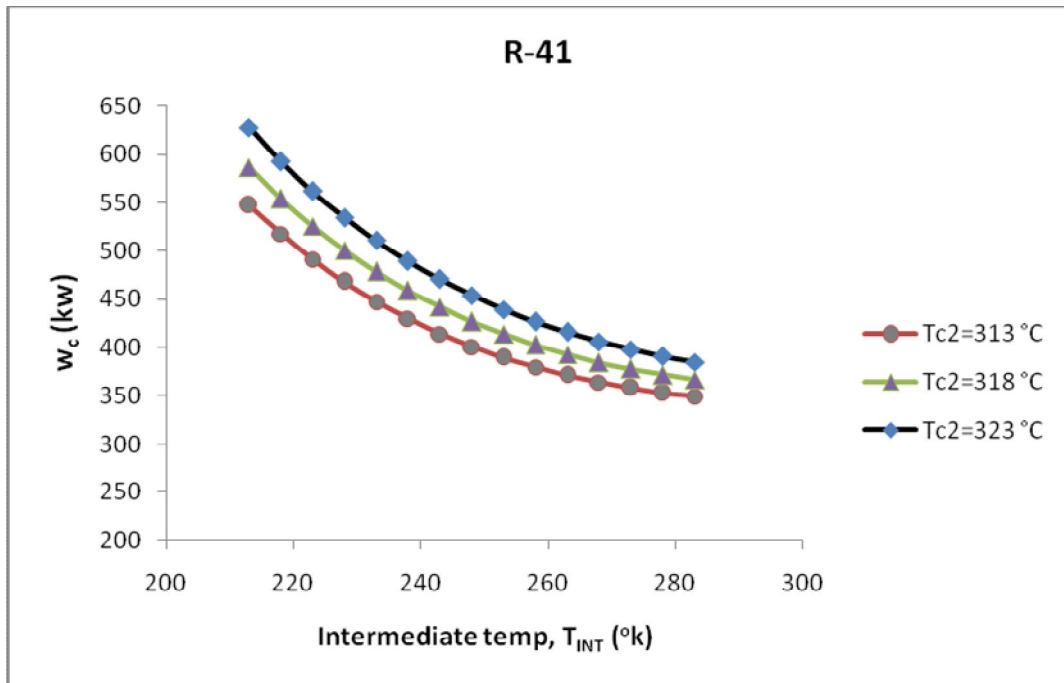


Fig.51 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

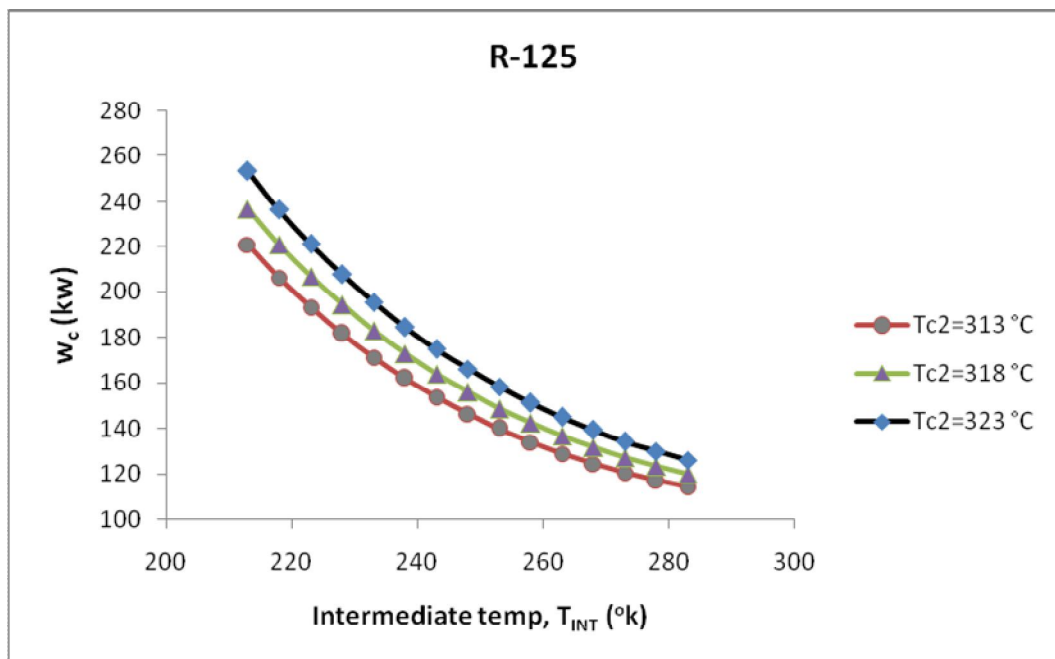


Fig.52 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

**Variation in total compressor work with superheating 10°C and subcooling 5°C for cascade system**

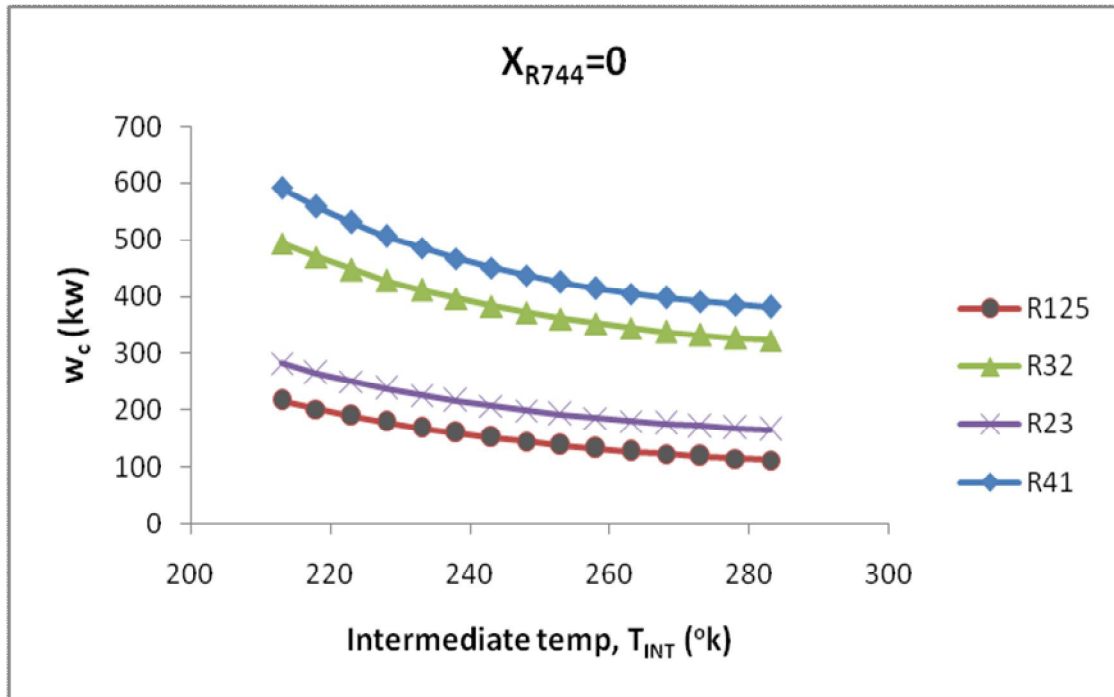


Fig.53 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 0°C.

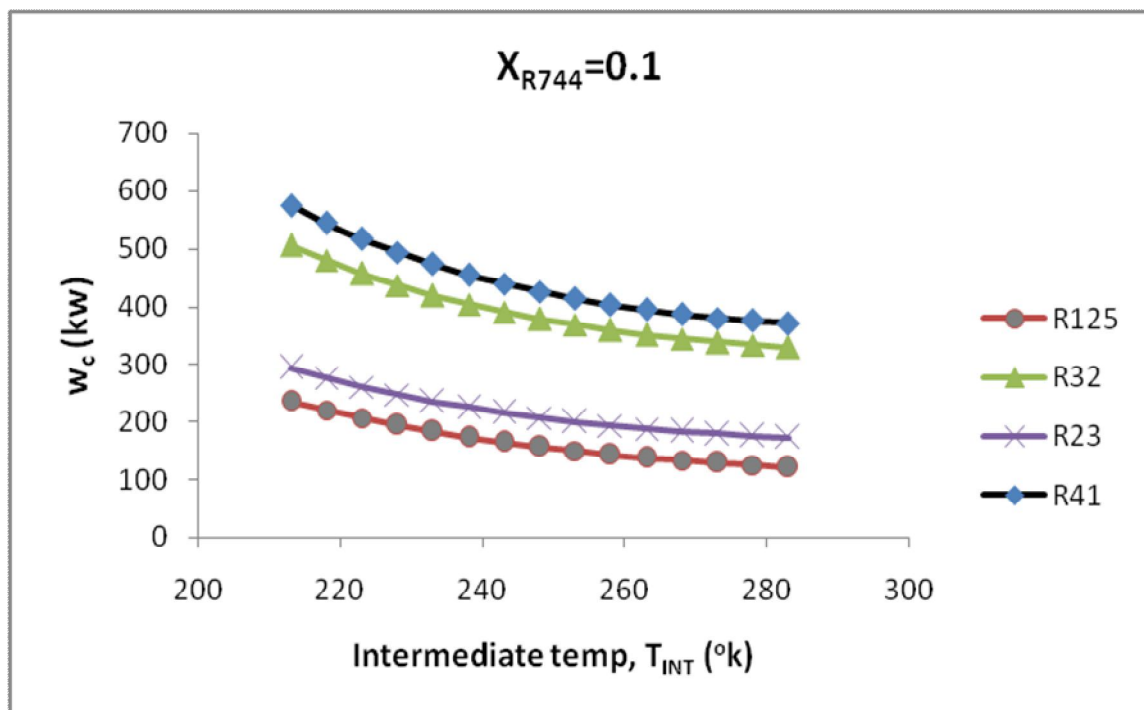


Fig.54 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

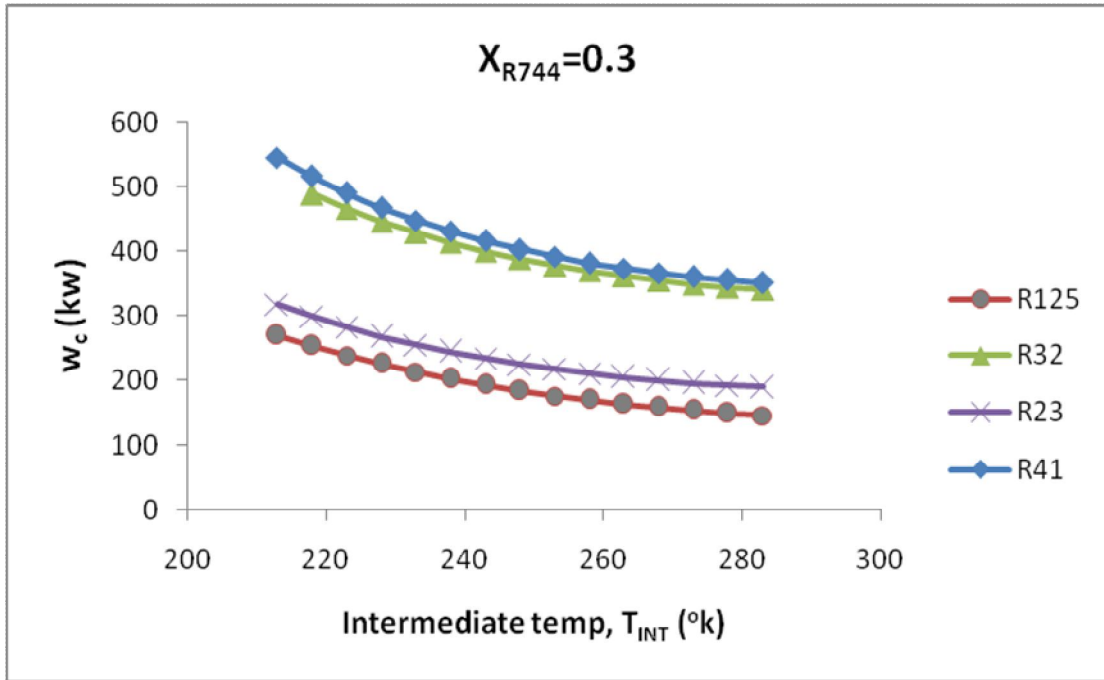


Fig.55 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

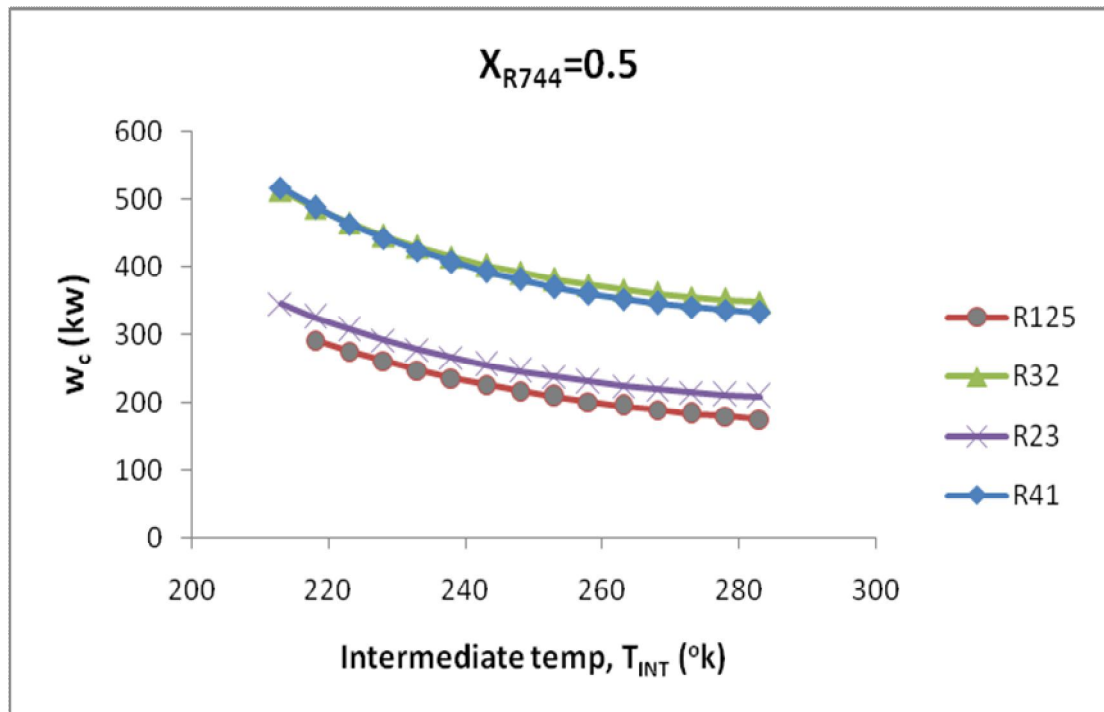


Fig.56 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

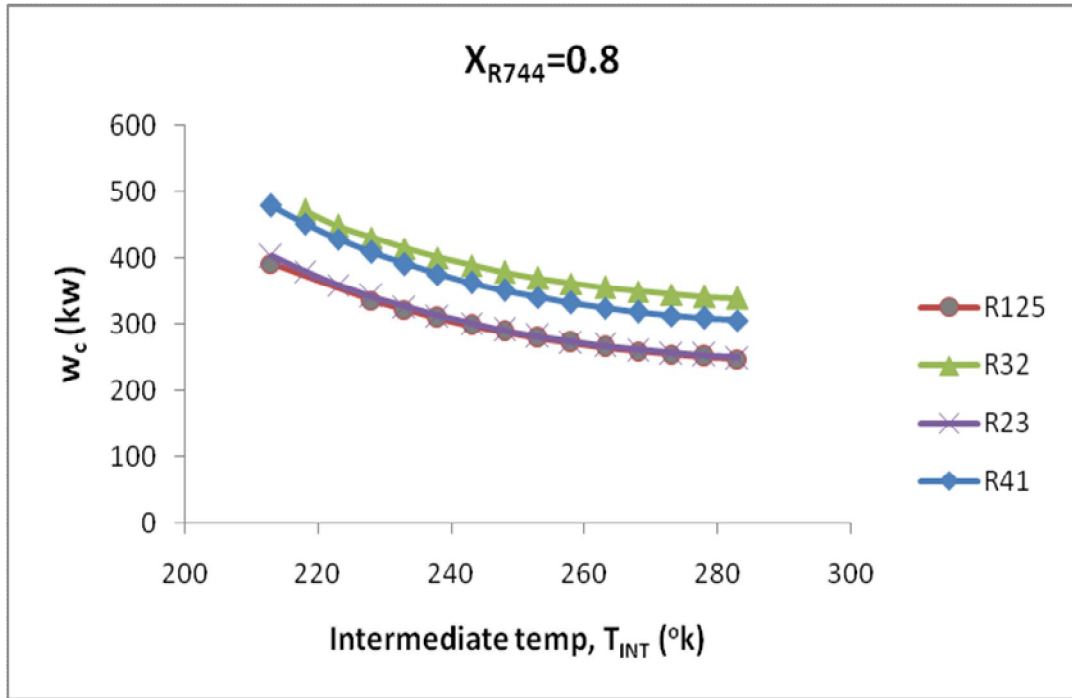


Fig.57 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

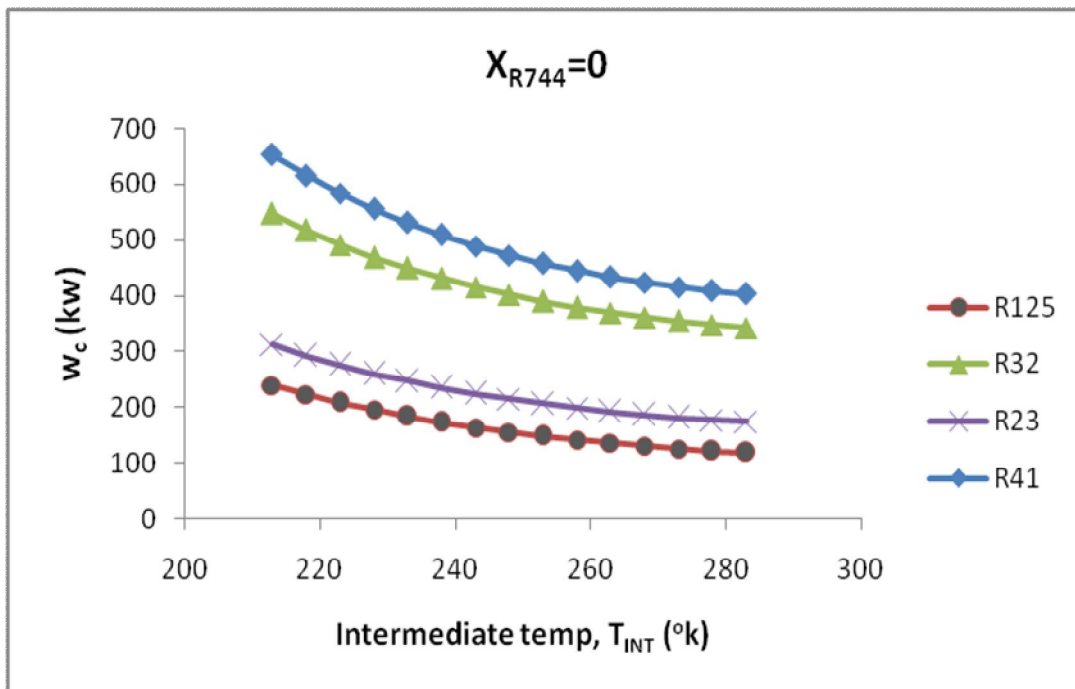


Fig.58 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

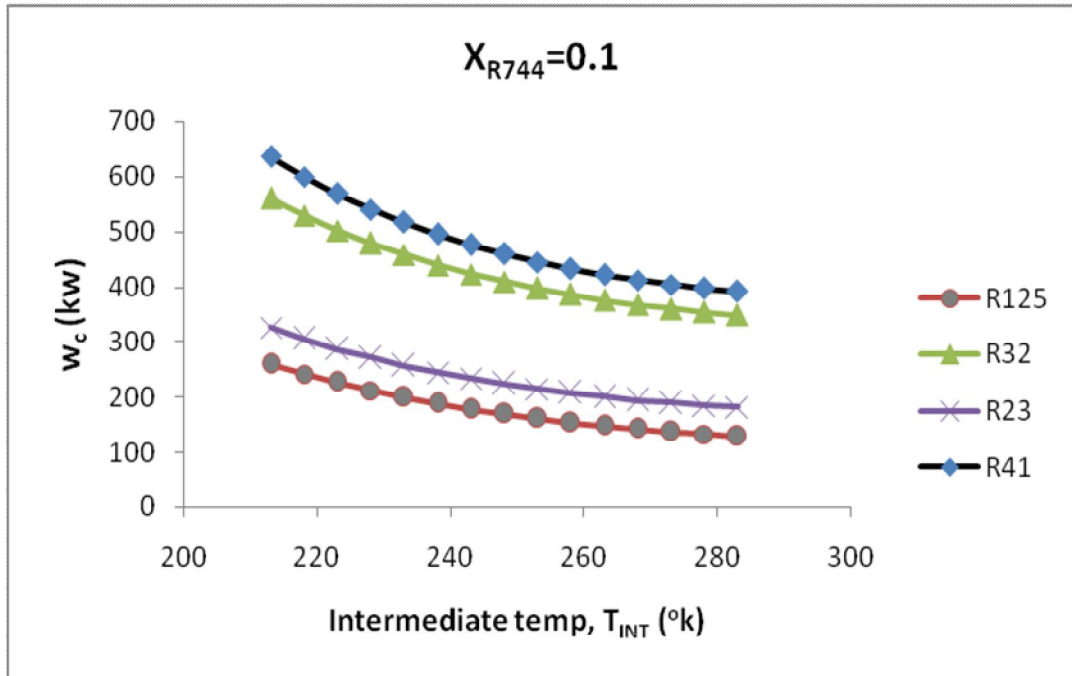


Fig.59 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

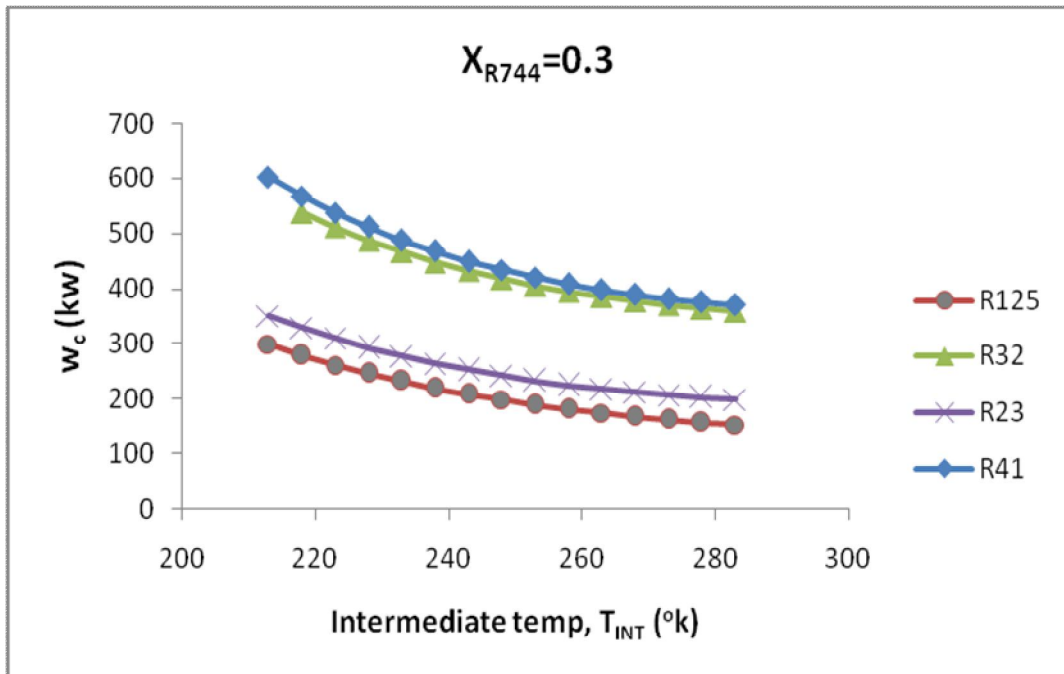


Fig.60 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.

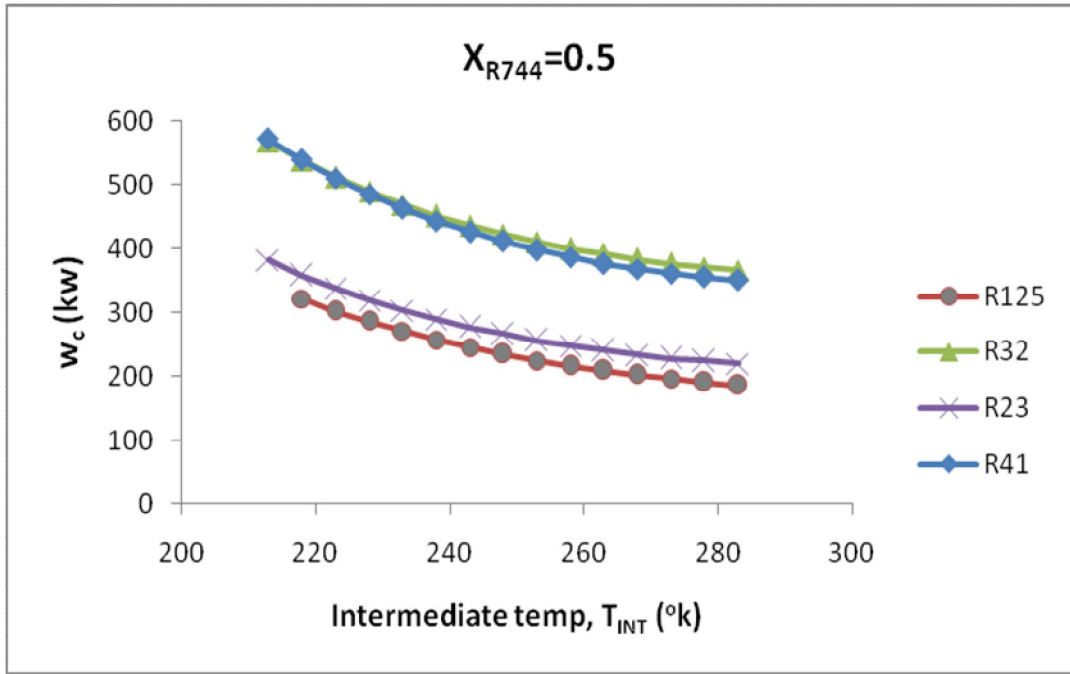


Fig.61 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

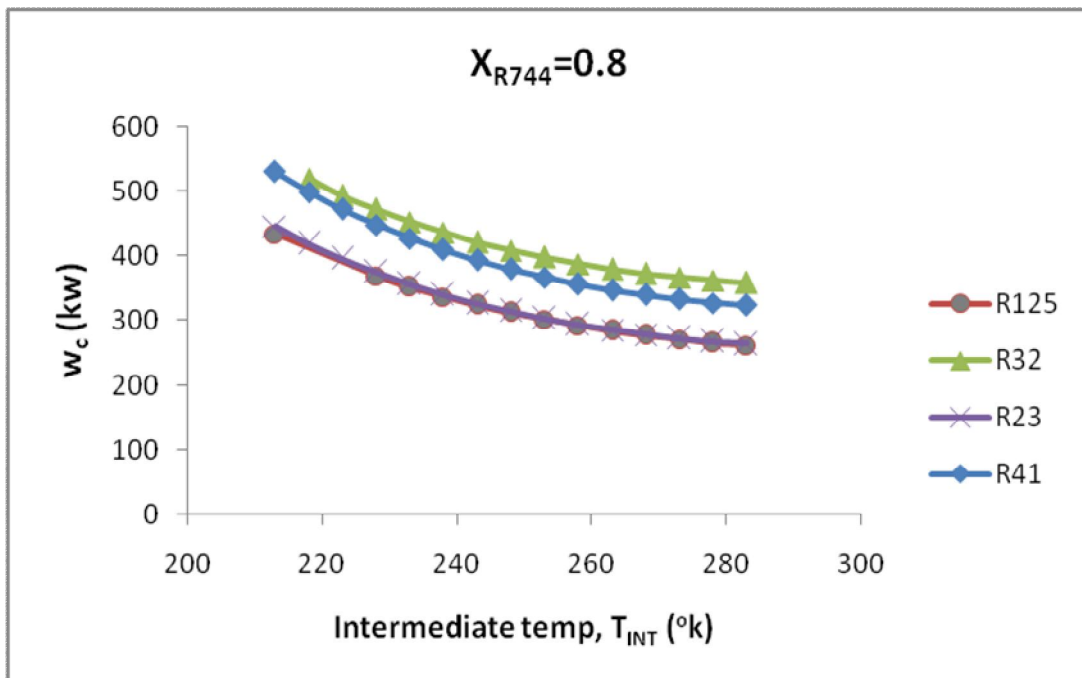


Fig.62 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.



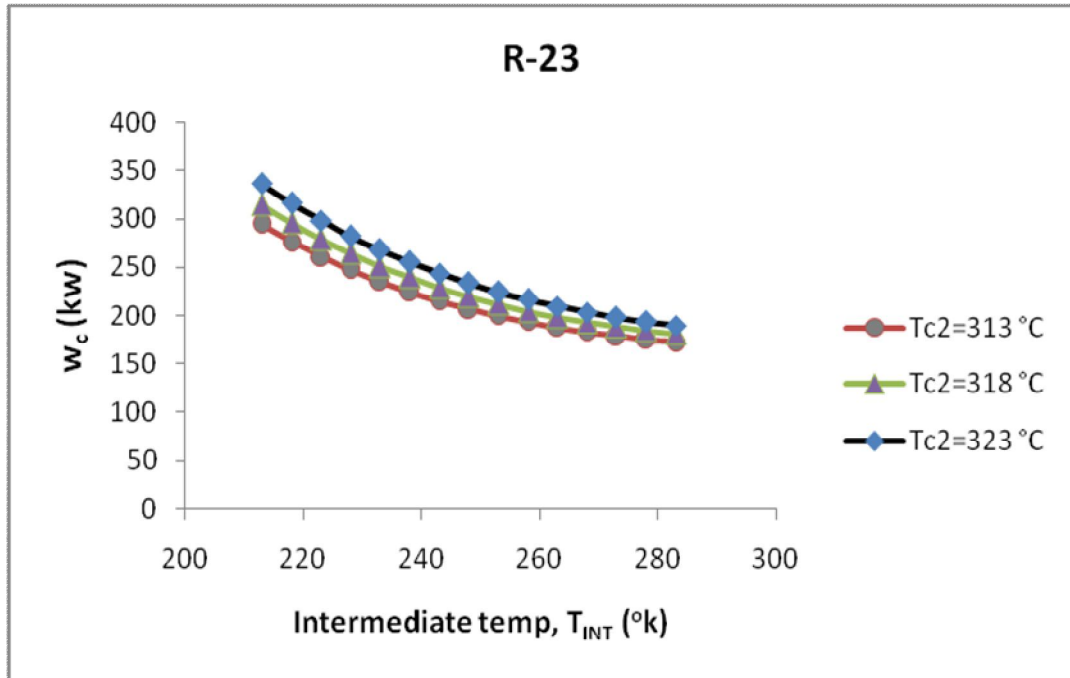


Fig.63 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

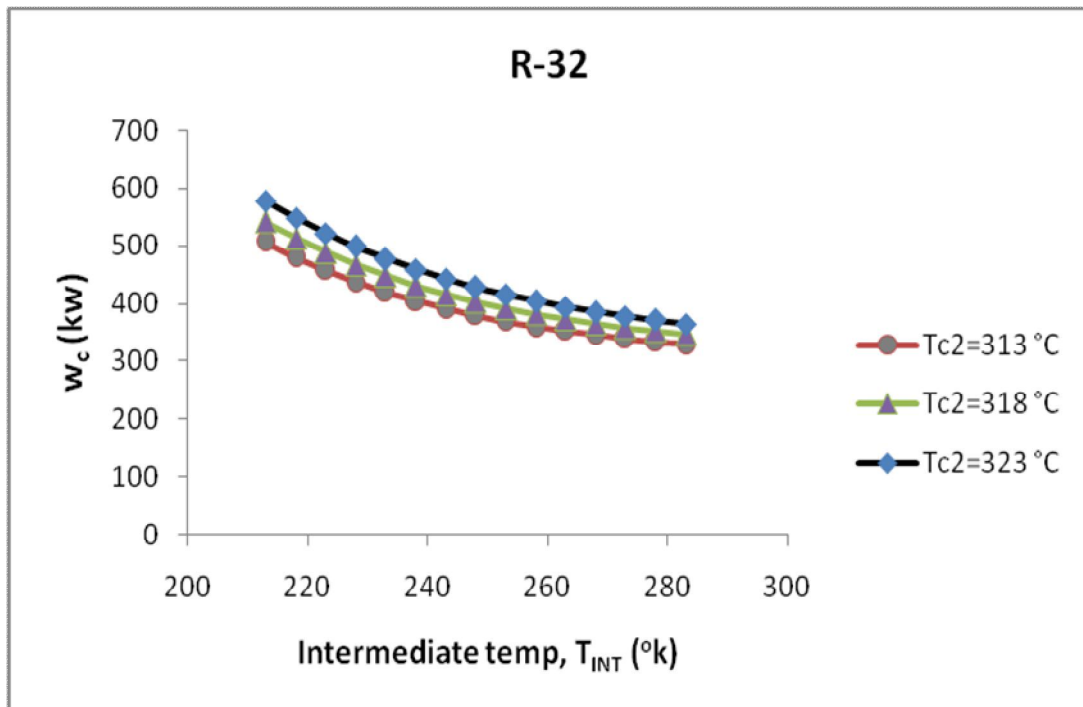


Fig.64 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

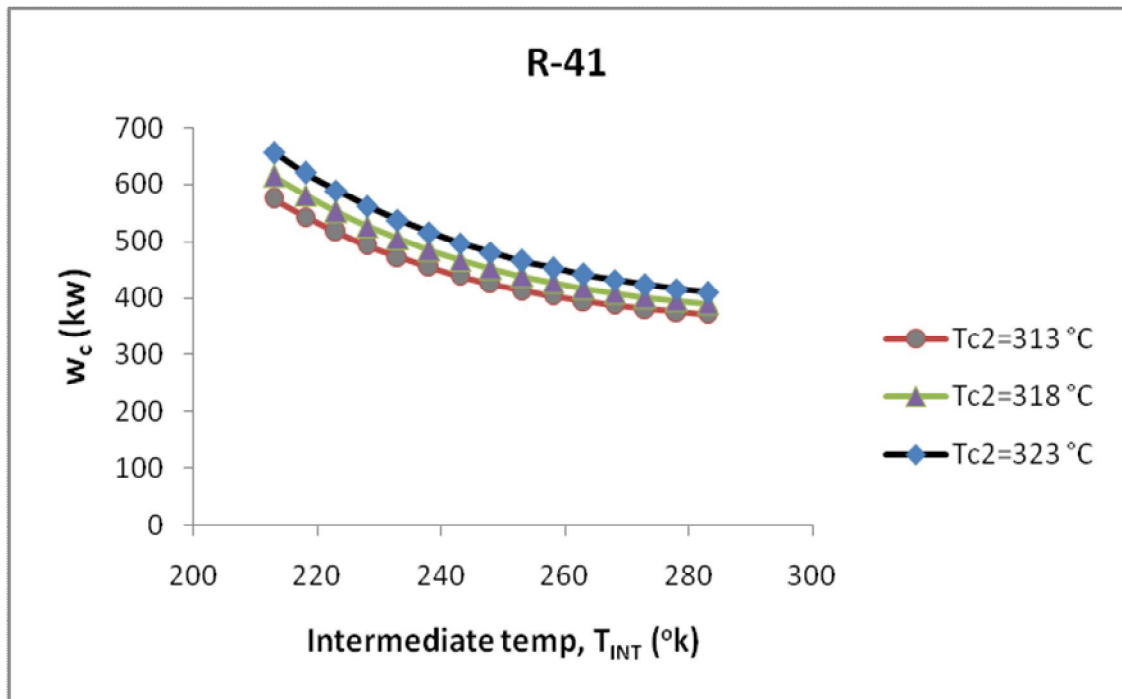


Fig.65 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

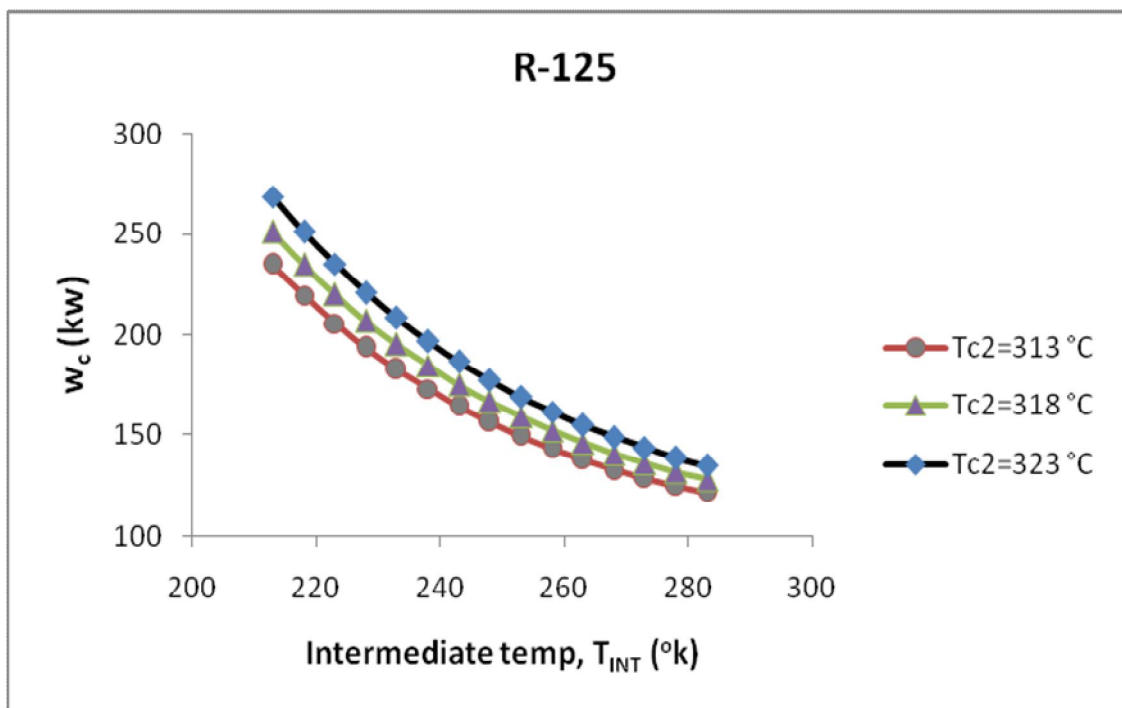


Fig.66 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

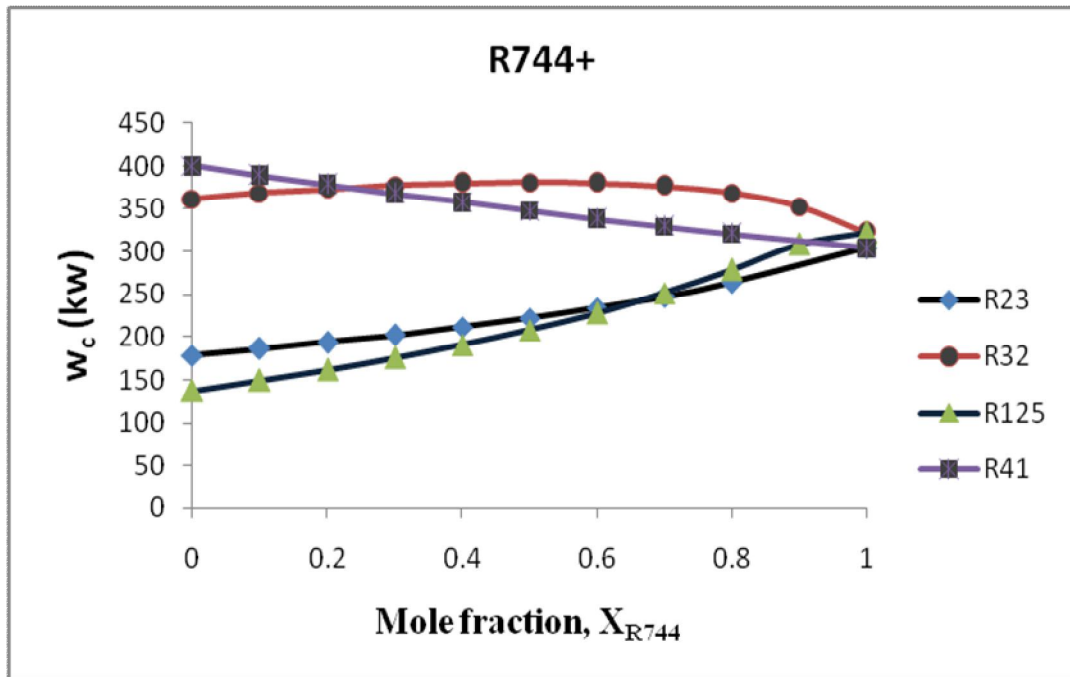


Fig.67 Variation in total compressor work with  $\text{CO}_2$  mole fraction for cascade system operating with R744 blends as low temperature working fluid.

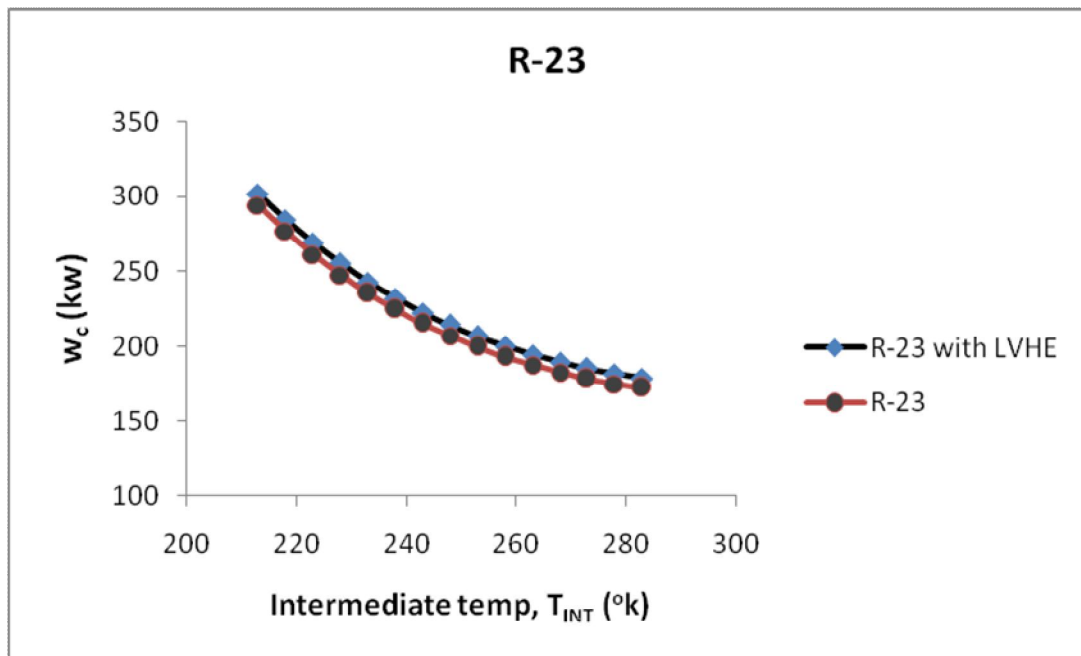


Fig.68 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 taking LVHE effectiveness 1.

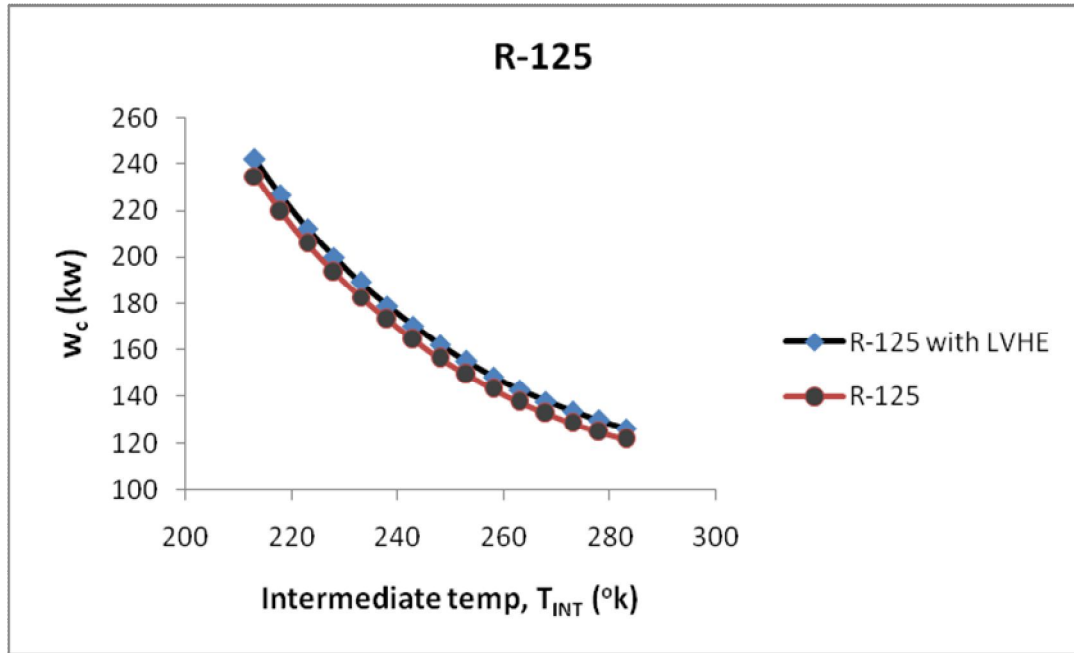


Fig.69 Variation in total compressor work with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125R-23 taking LVHE effectiveness 1.

## Variation in Coefficient of Performance without superheating and subcooling for cascade system

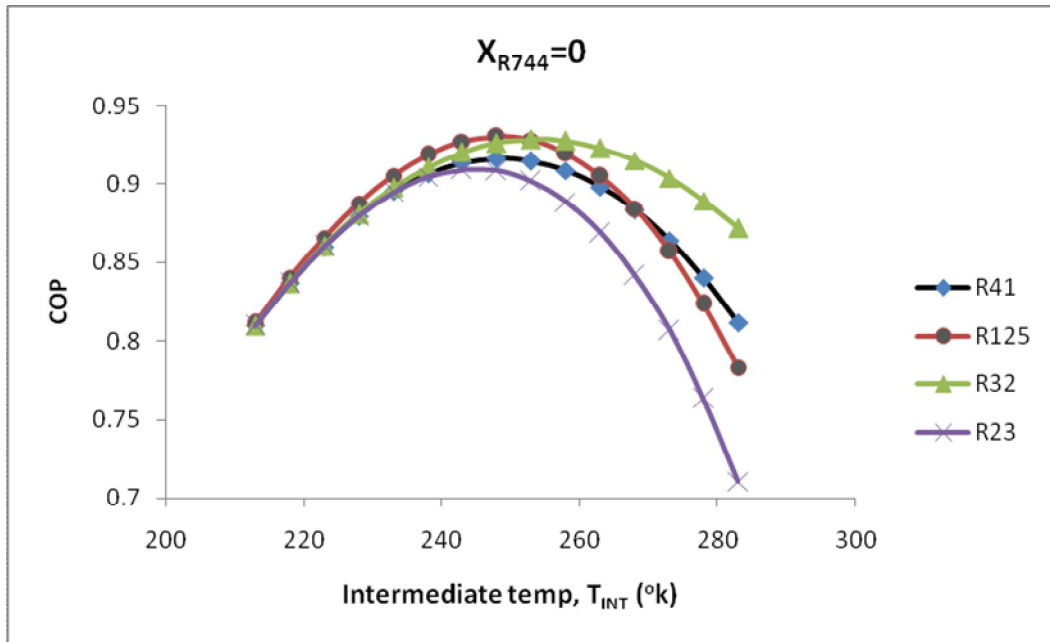


Fig.70 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 0°C.

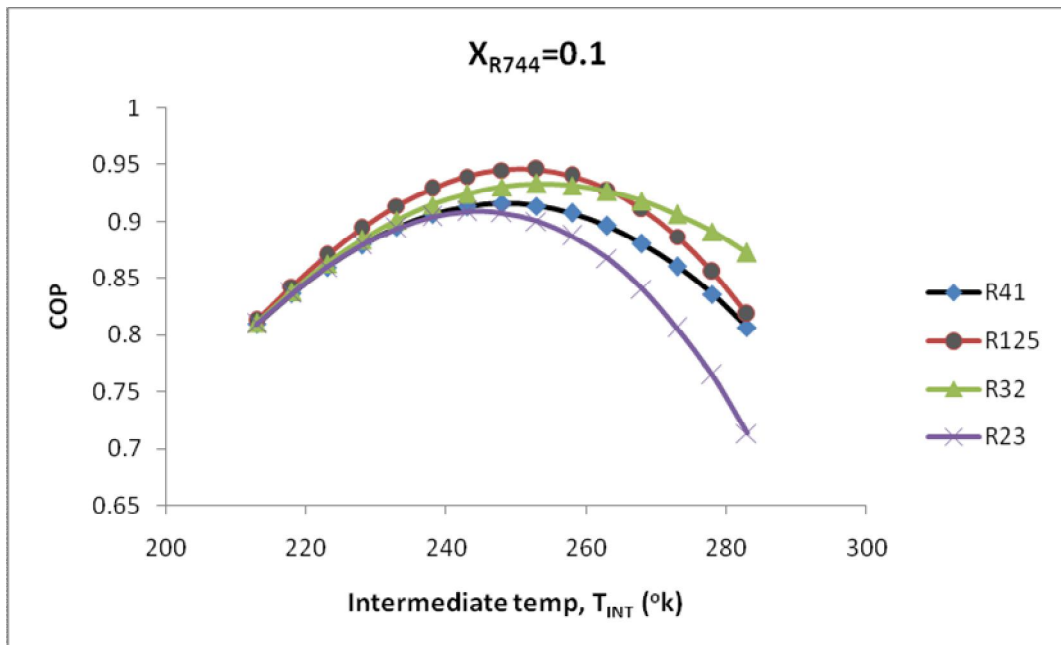


Fig.71 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

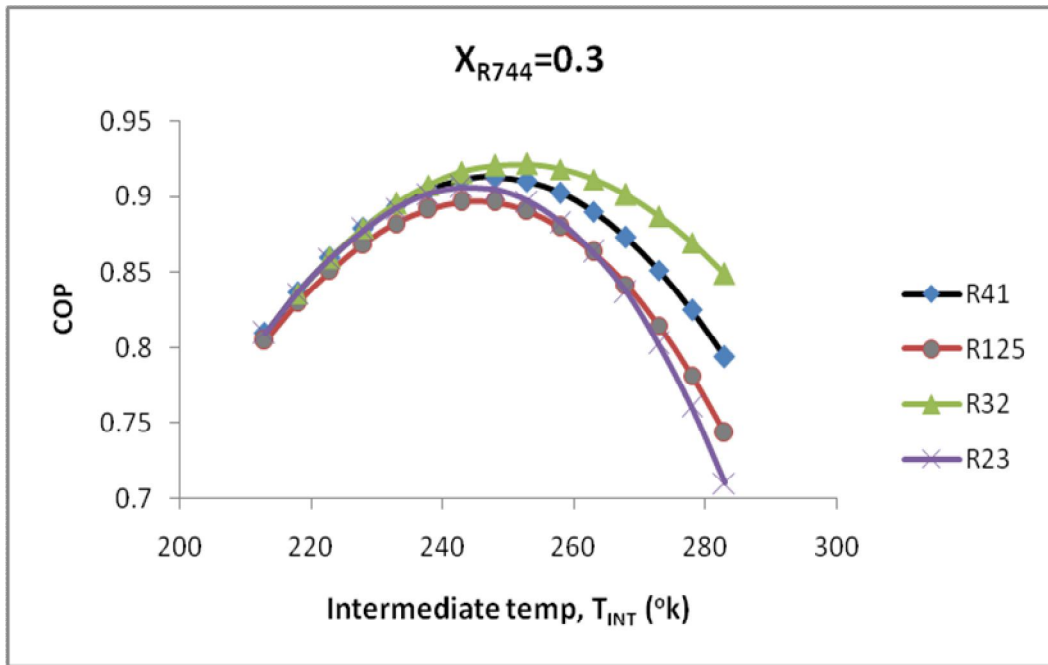


Fig.72 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

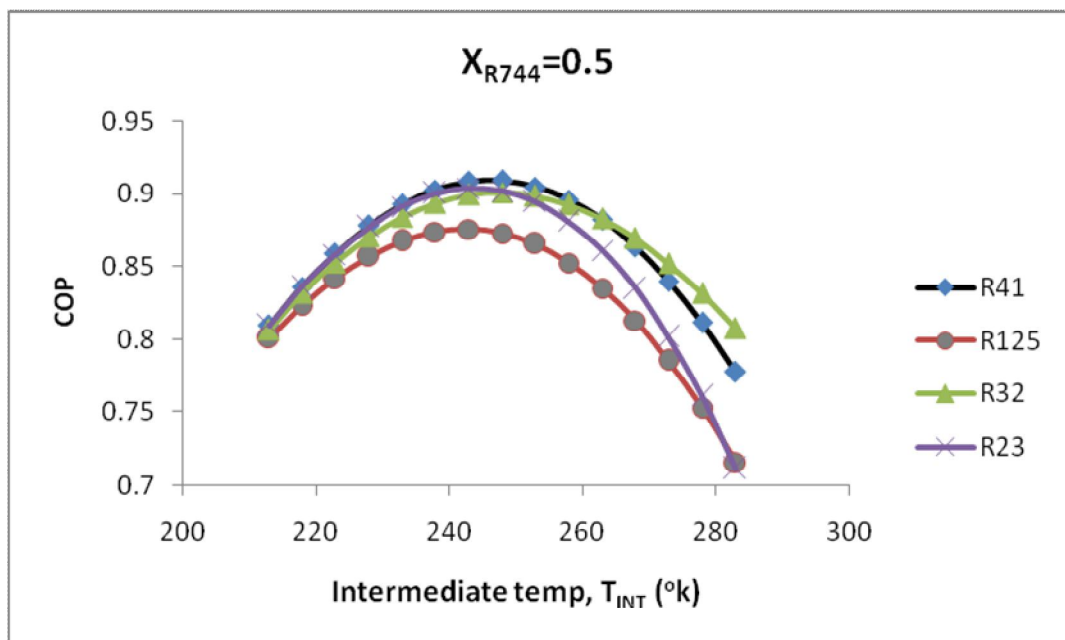


Fig.73 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

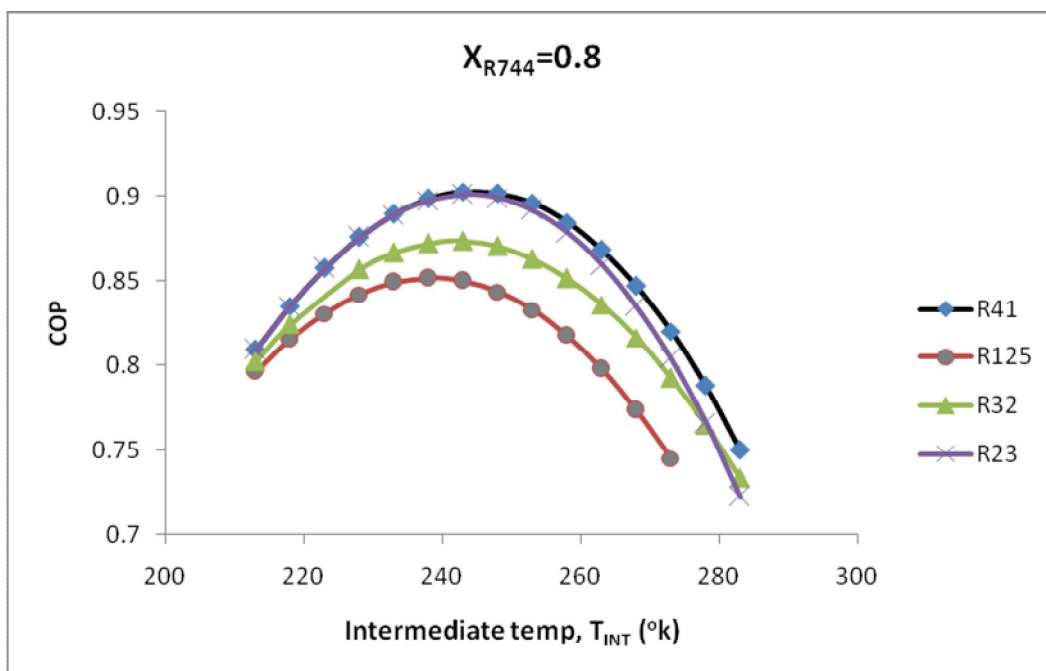


Fig.74 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

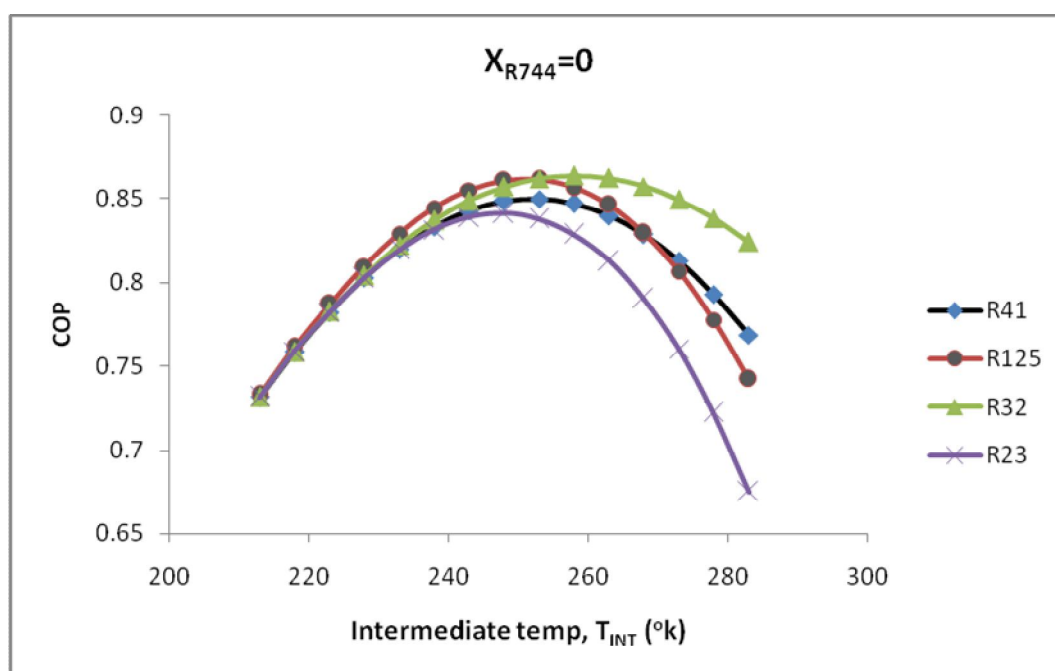


Fig.75 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

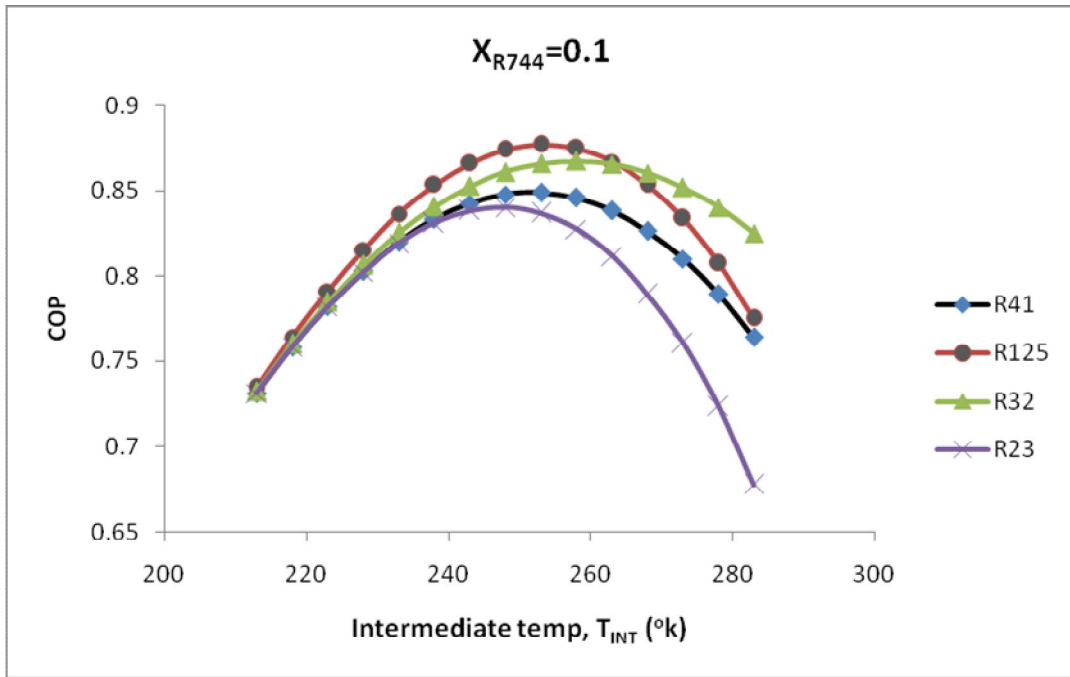


Fig.76 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

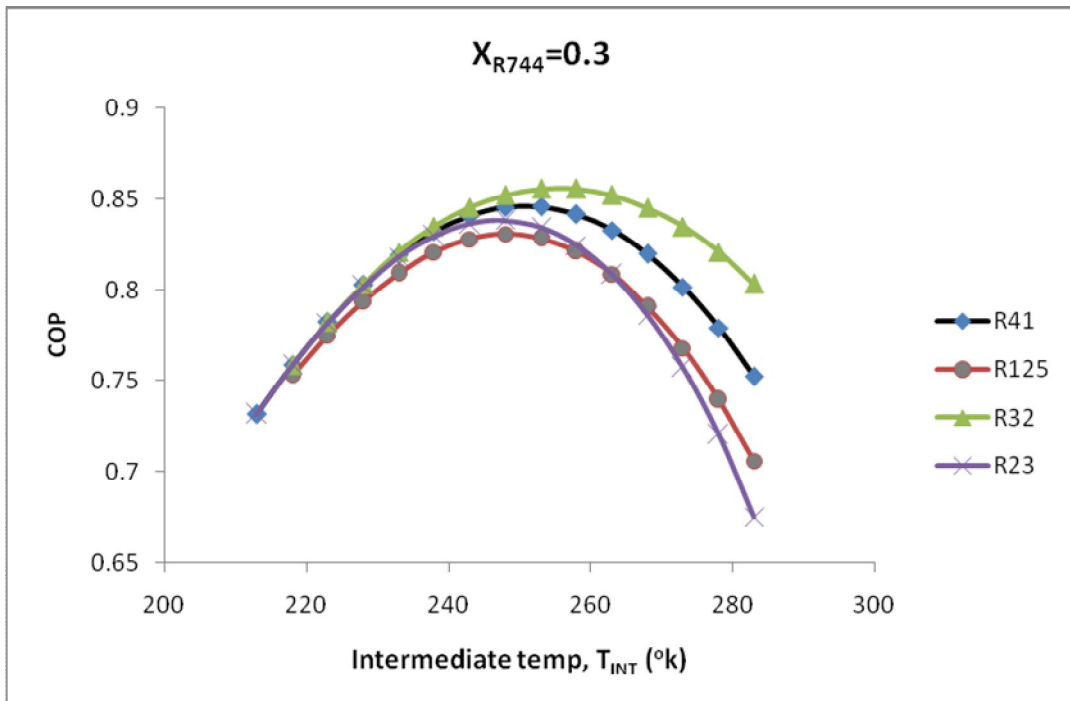


Fig.77 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.



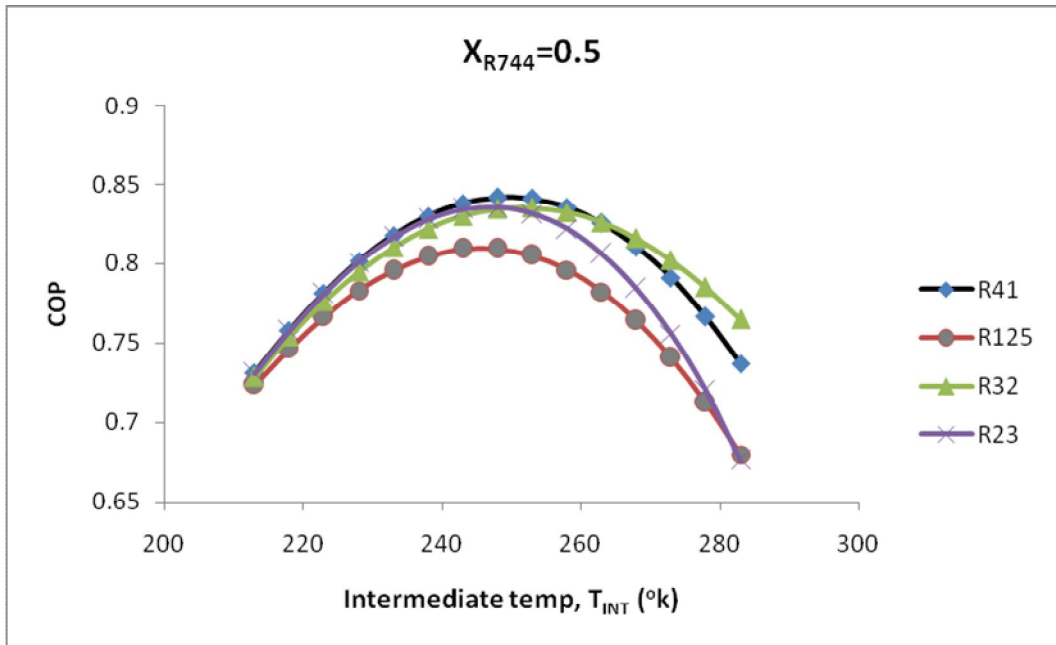


Fig.78 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

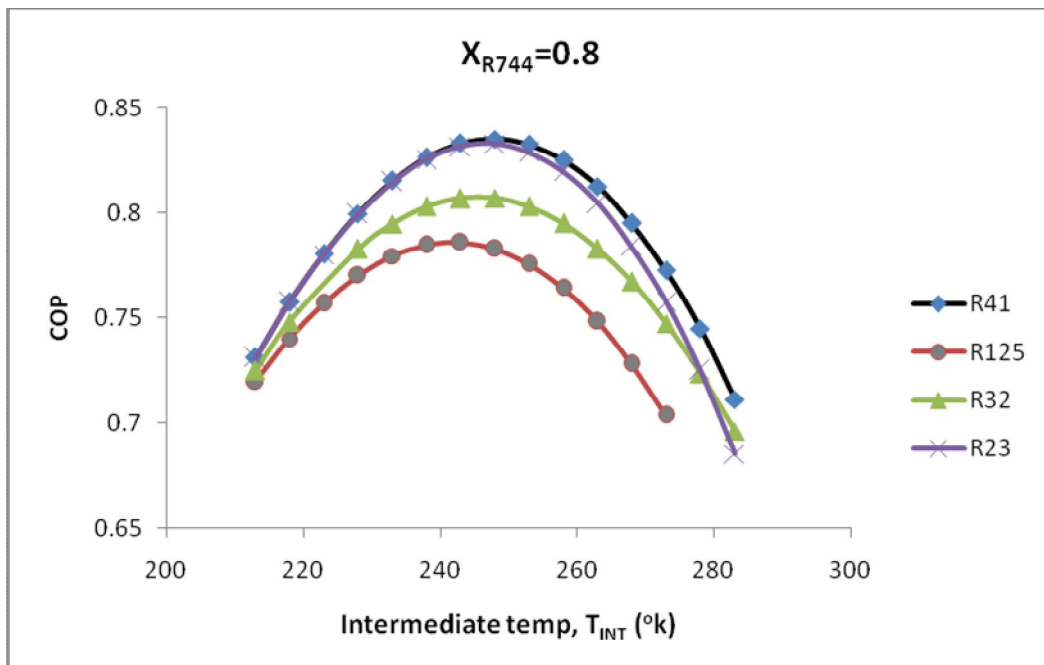


Fig.79 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.

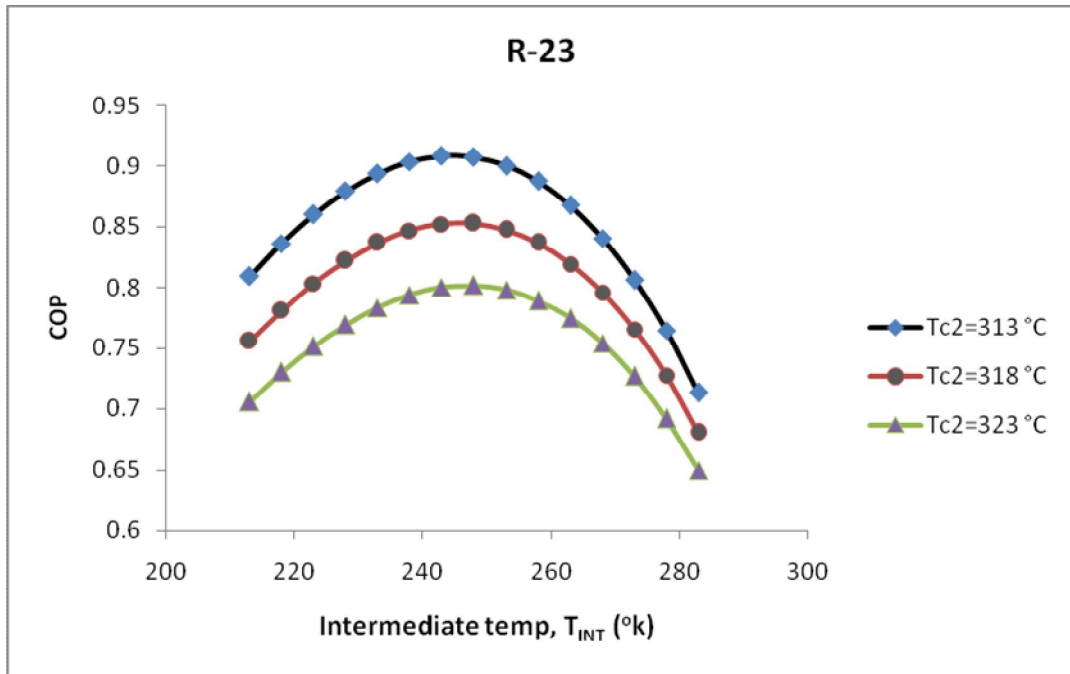


Fig.80 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

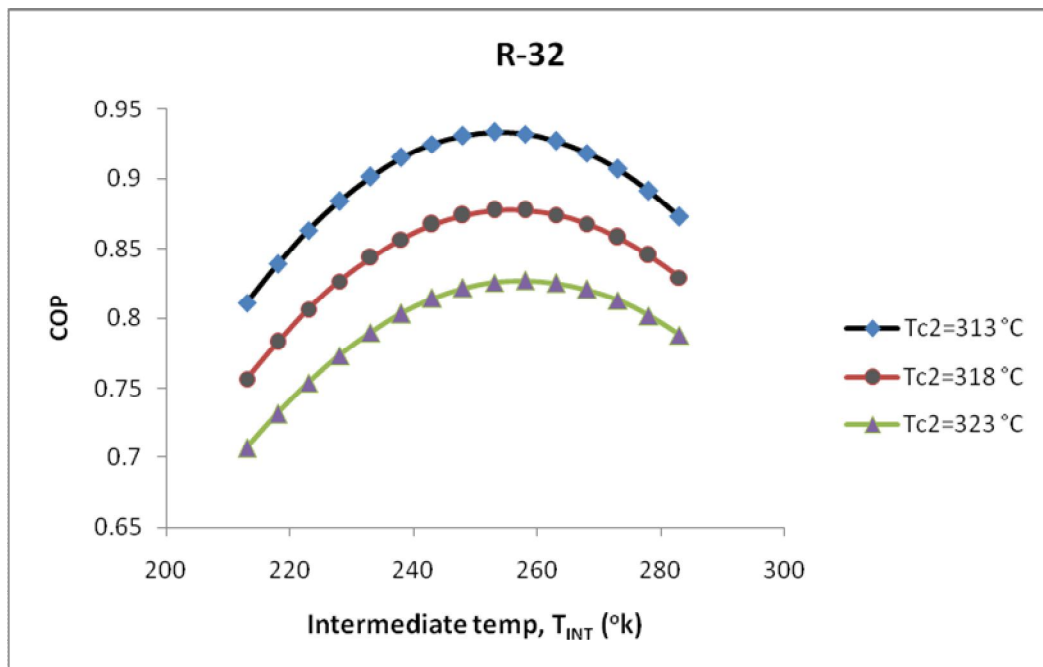


Fig.81 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

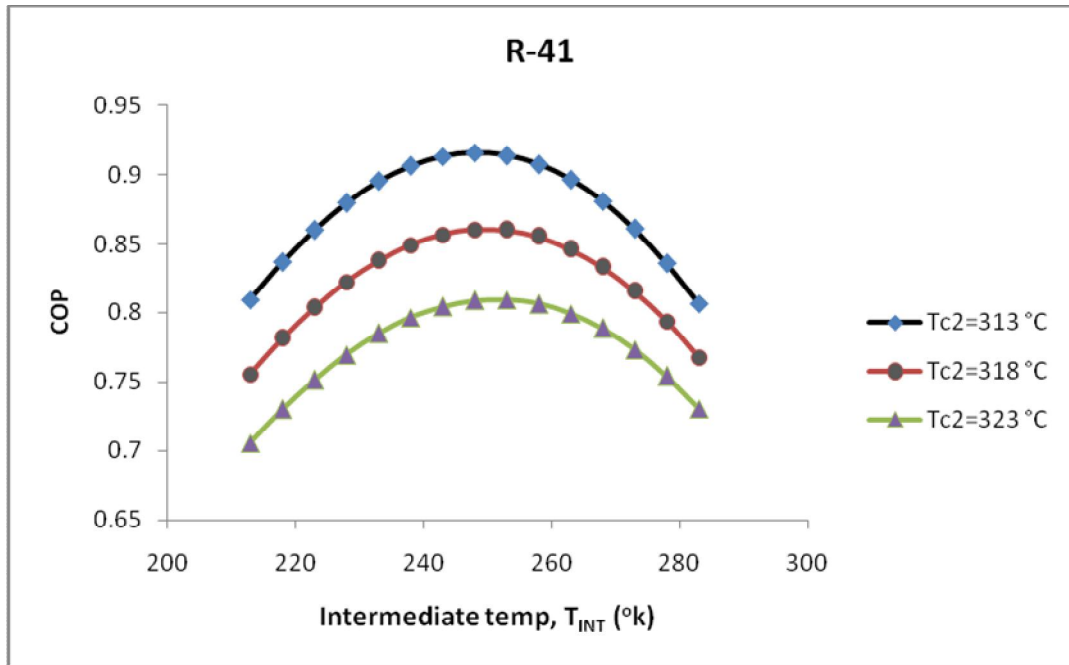


Fig.82 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

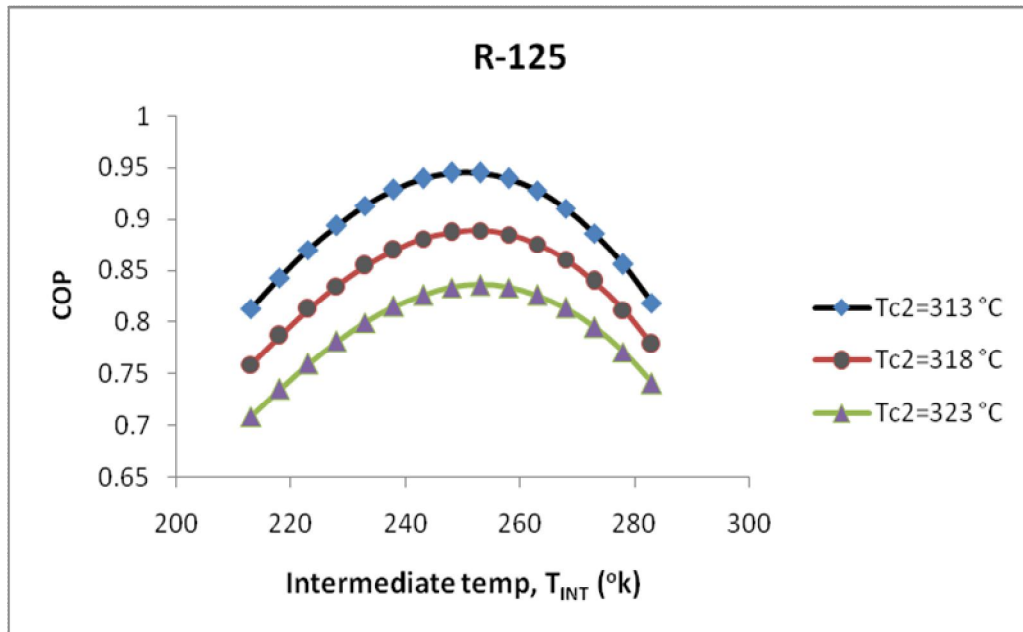


Fig.83 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

**Variation in Coefficient of Performance with superheating 10°C and subcooling 5°C for cascade system**

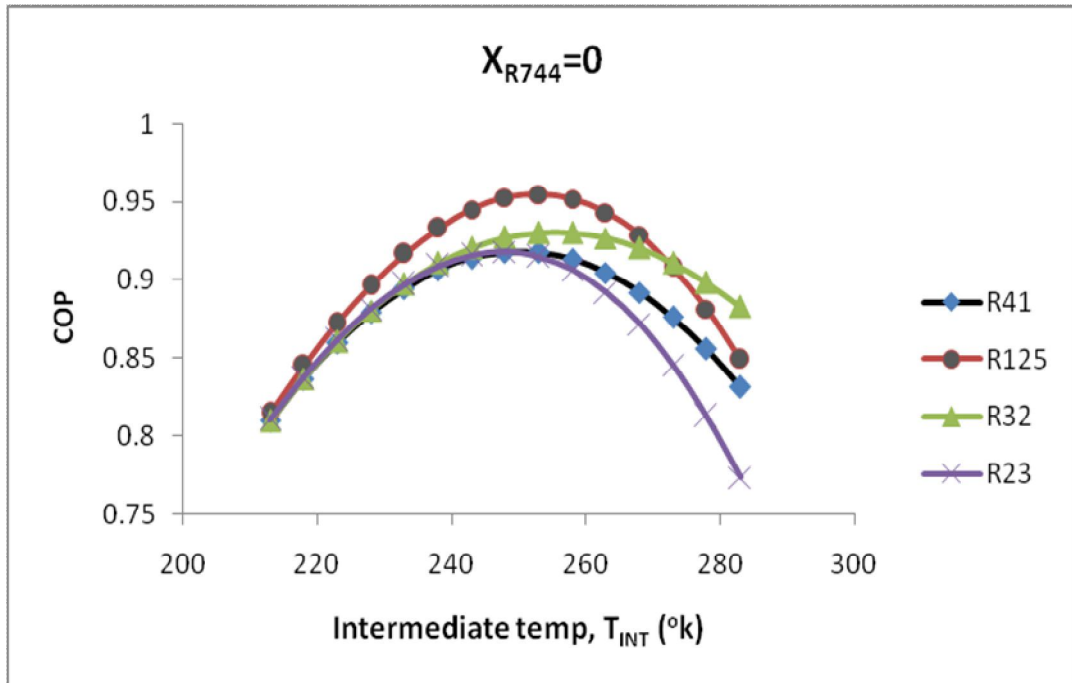


Fig.84 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 0°C.

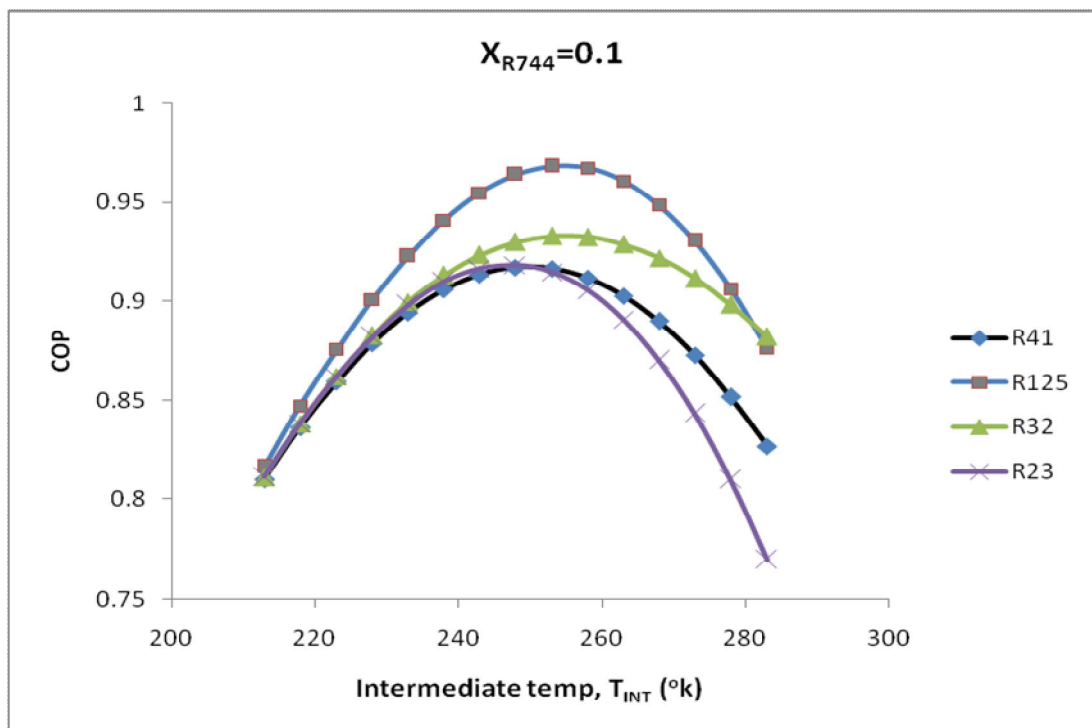


Fig.85 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

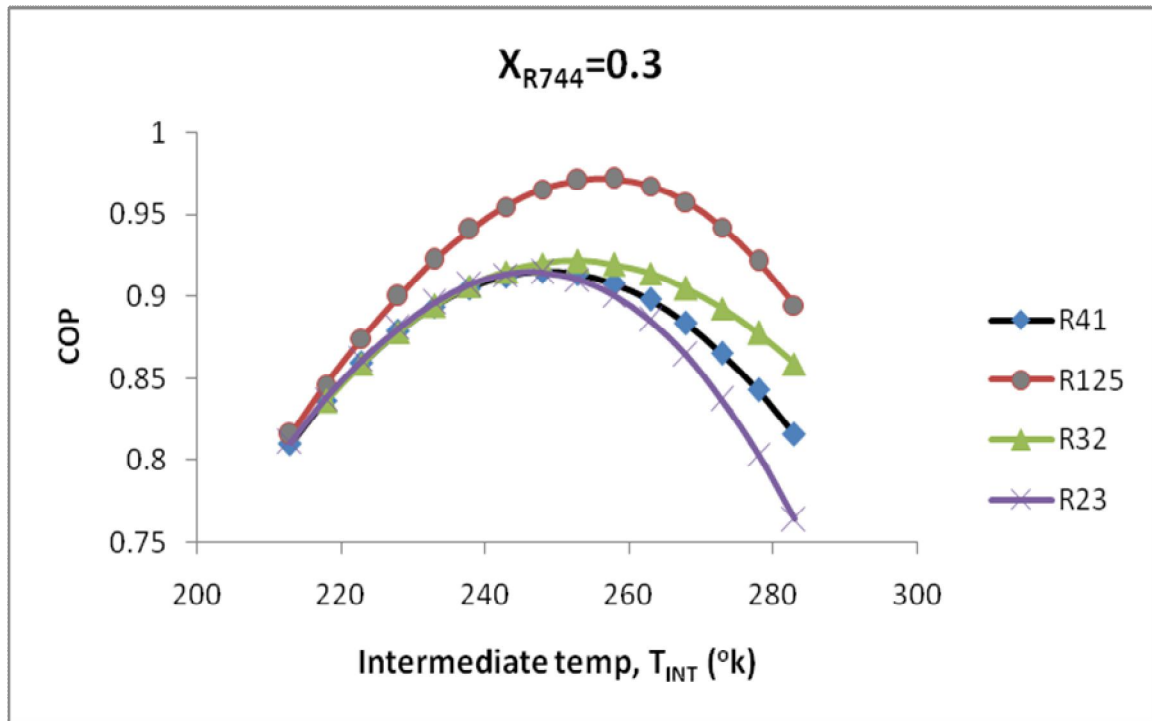


Fig.86 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

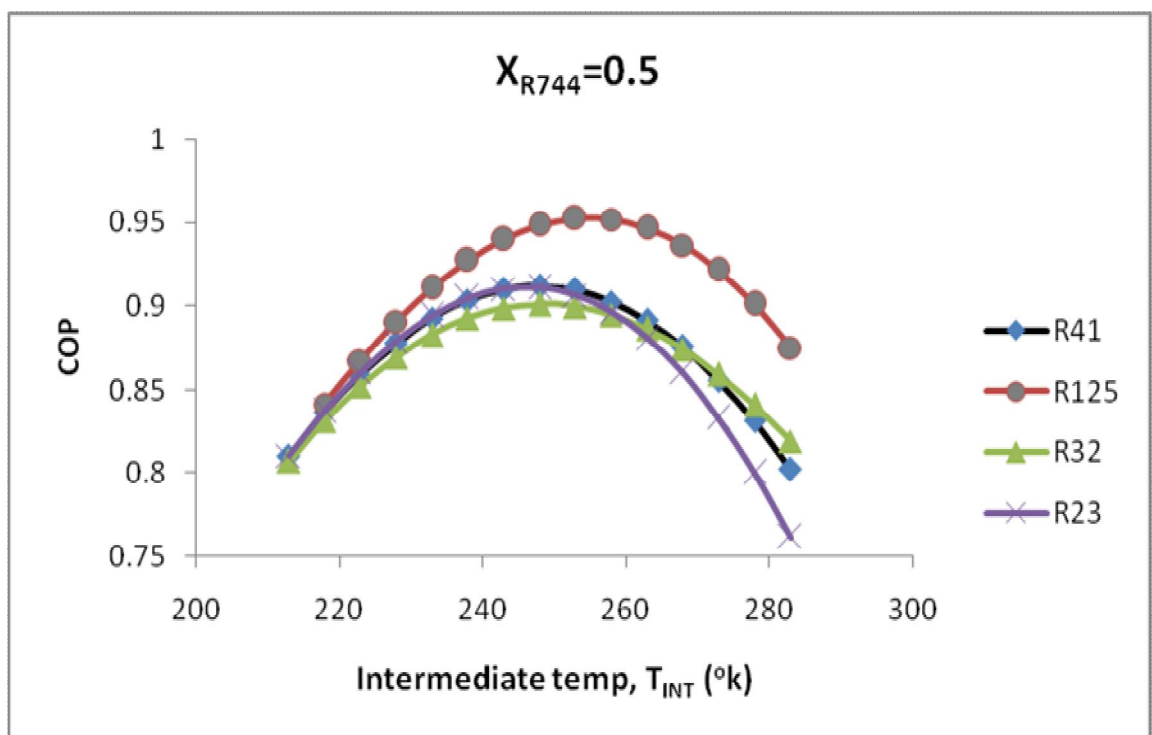


Fig.87 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

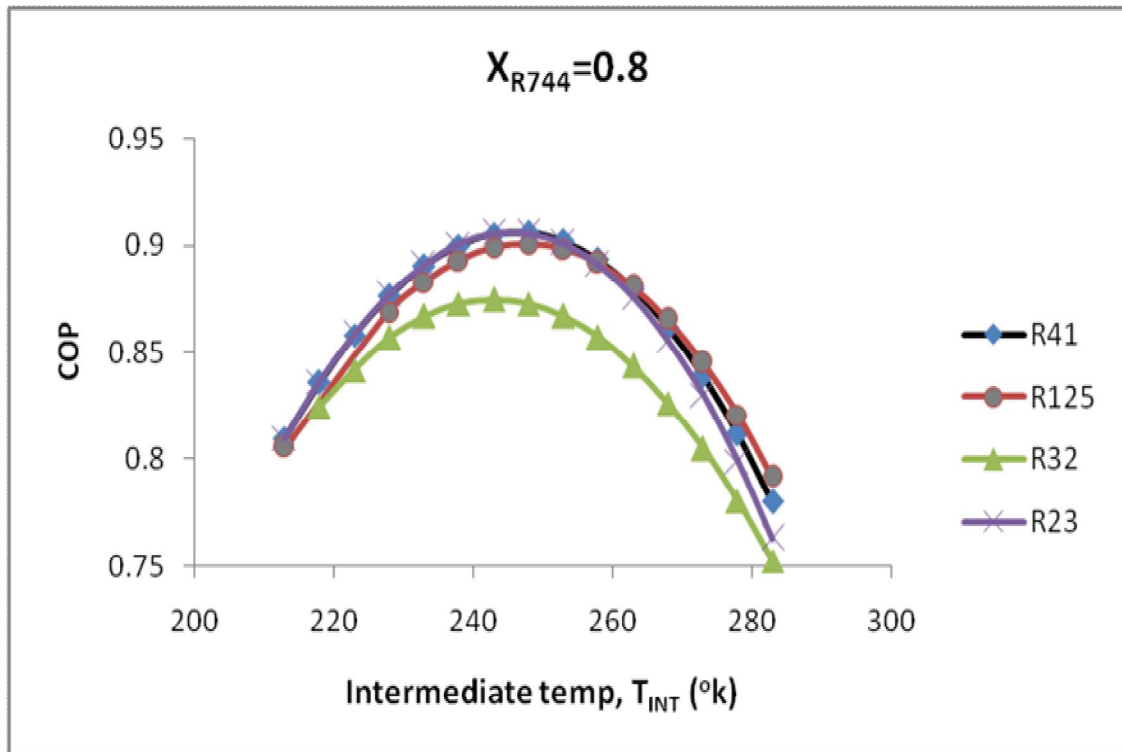


Fig.88 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

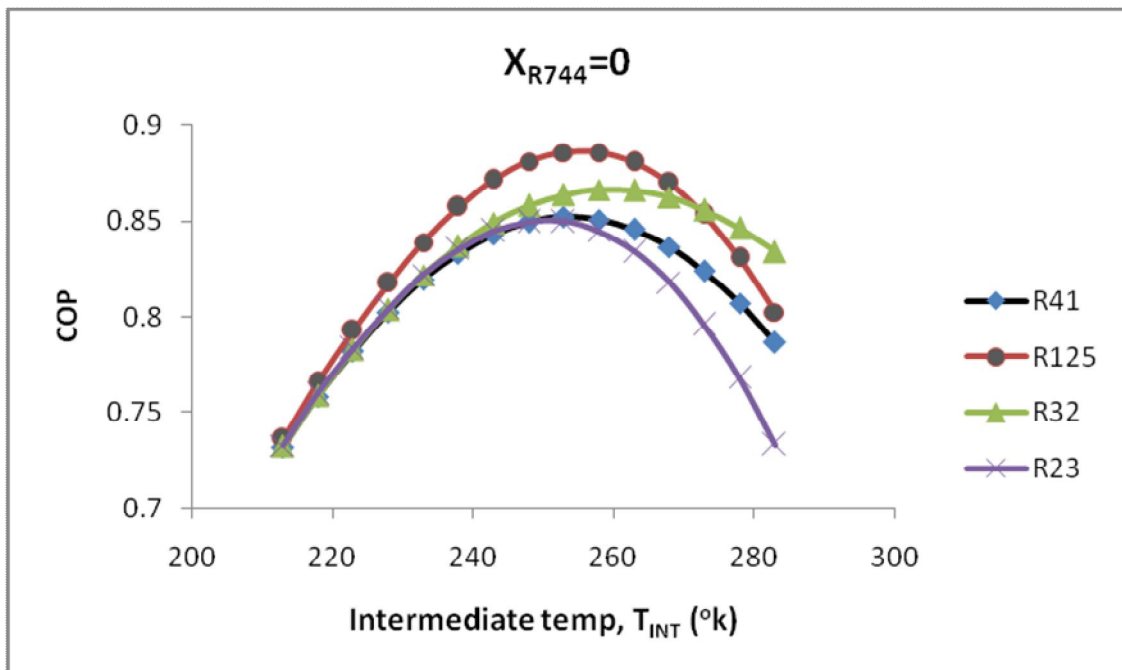


Fig.89 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

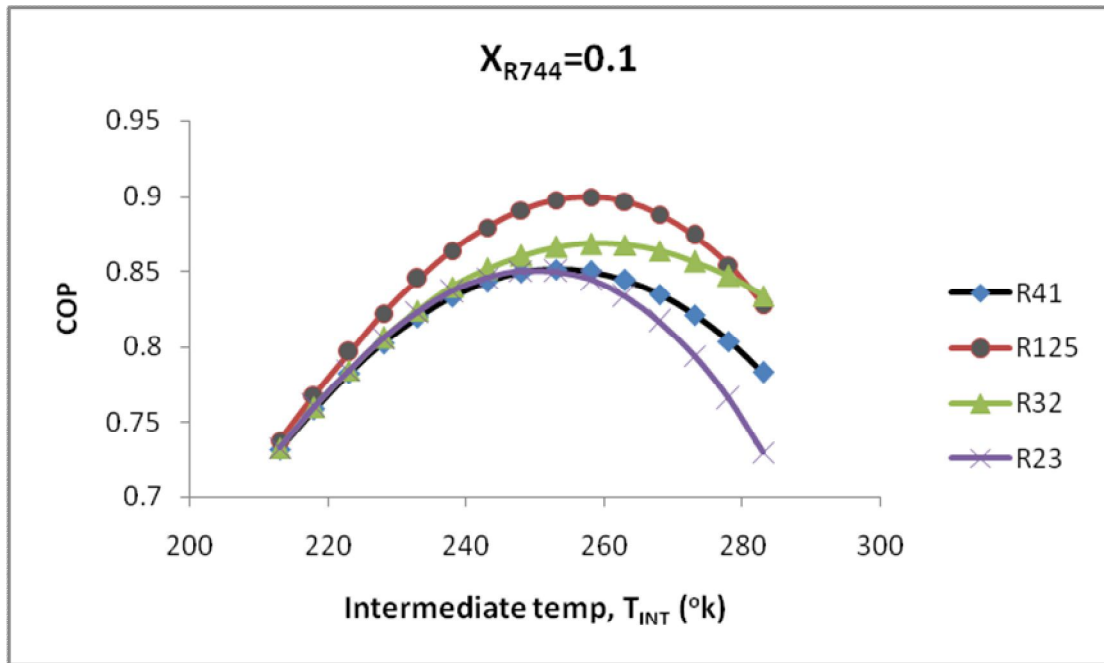


Fig.90 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

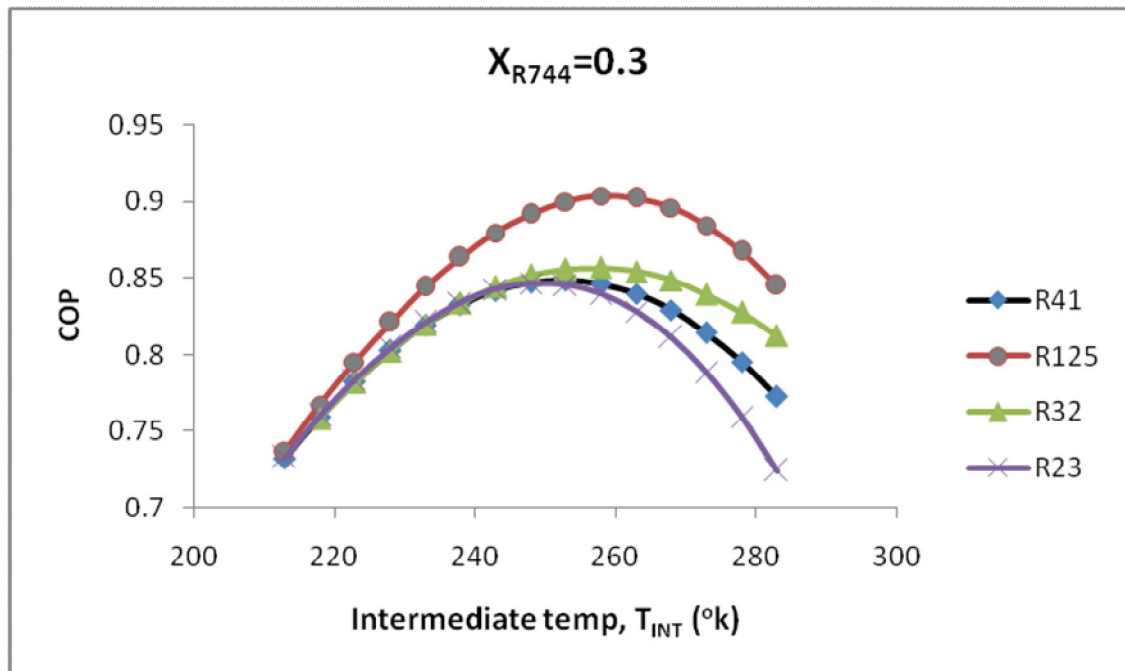


Fig.91 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.

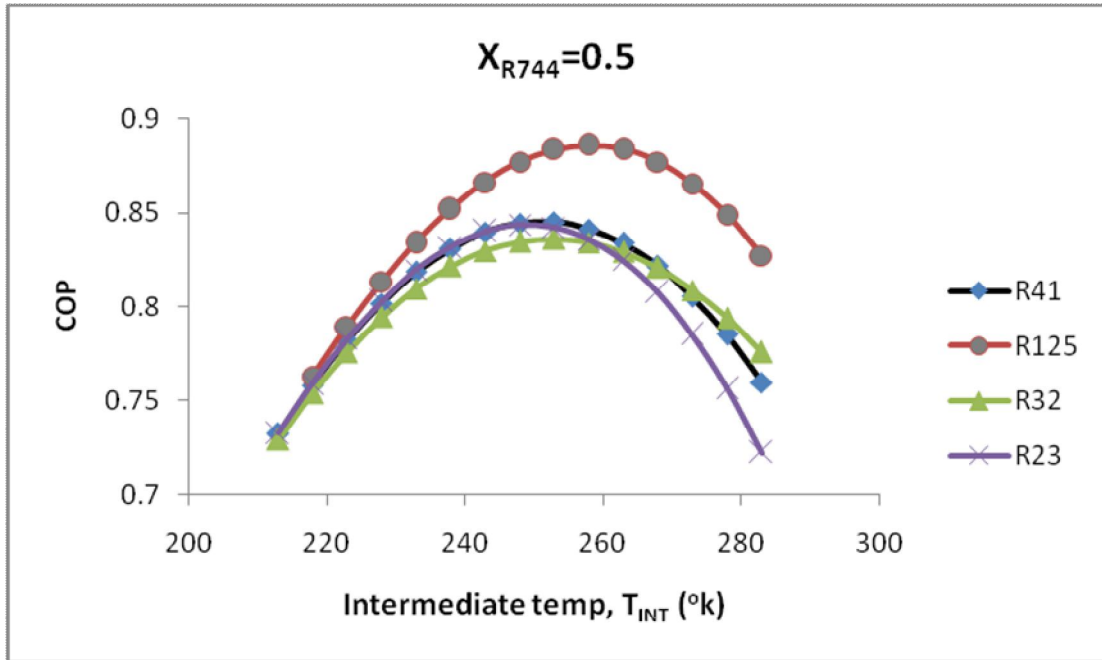


Fig.92 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

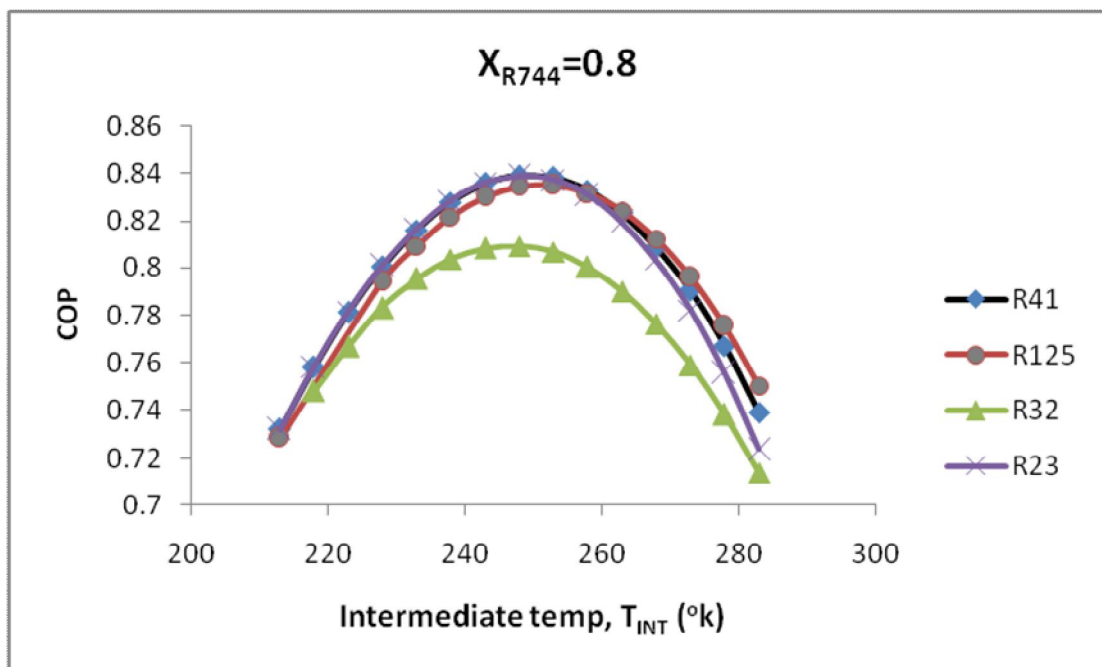


Fig.93 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.



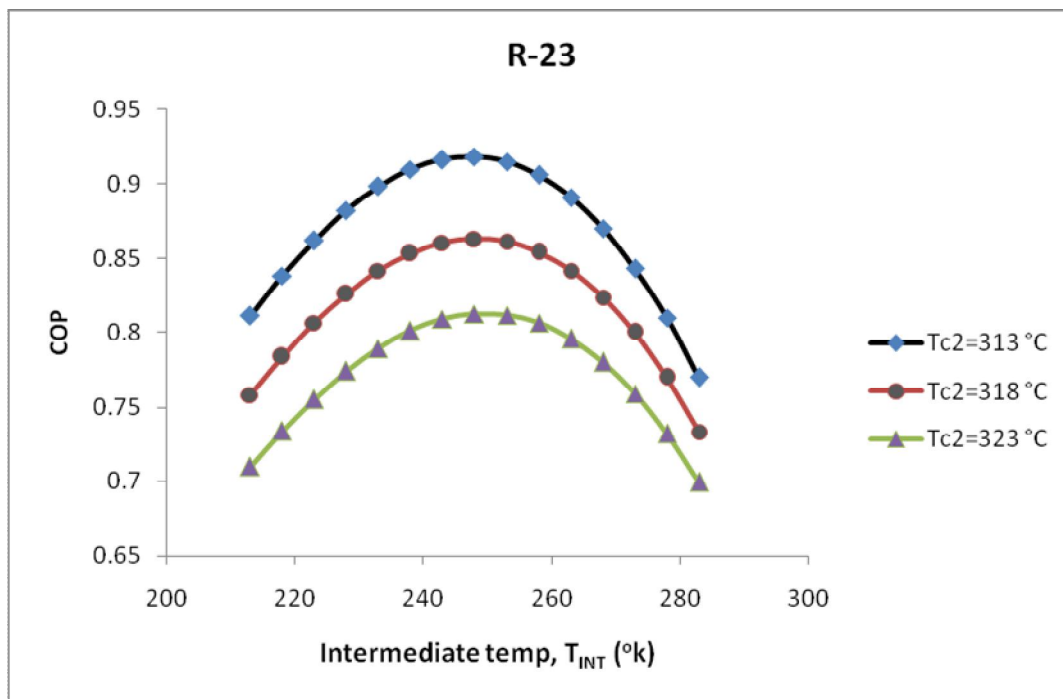


Fig.94 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

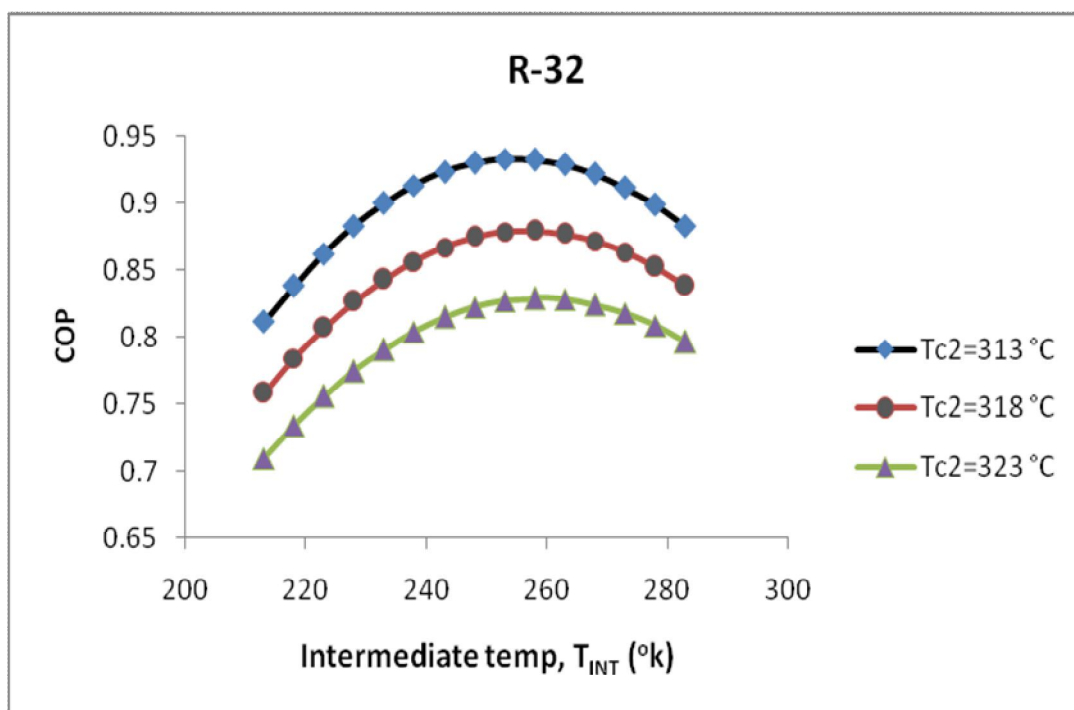


Fig.95 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

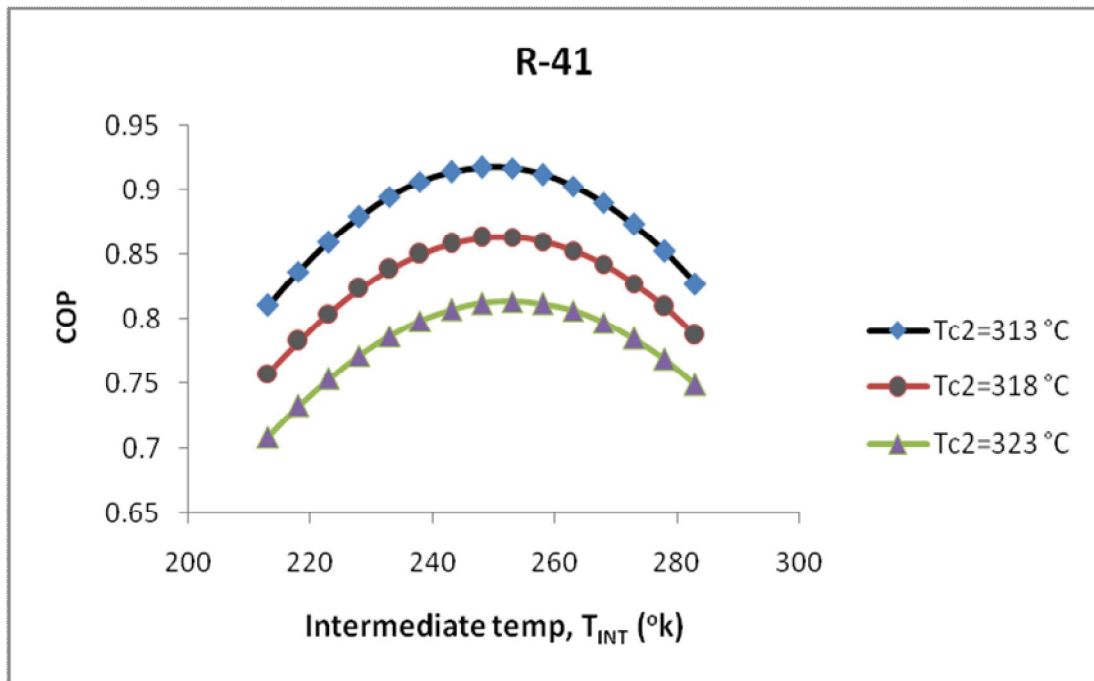


Fig.96 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

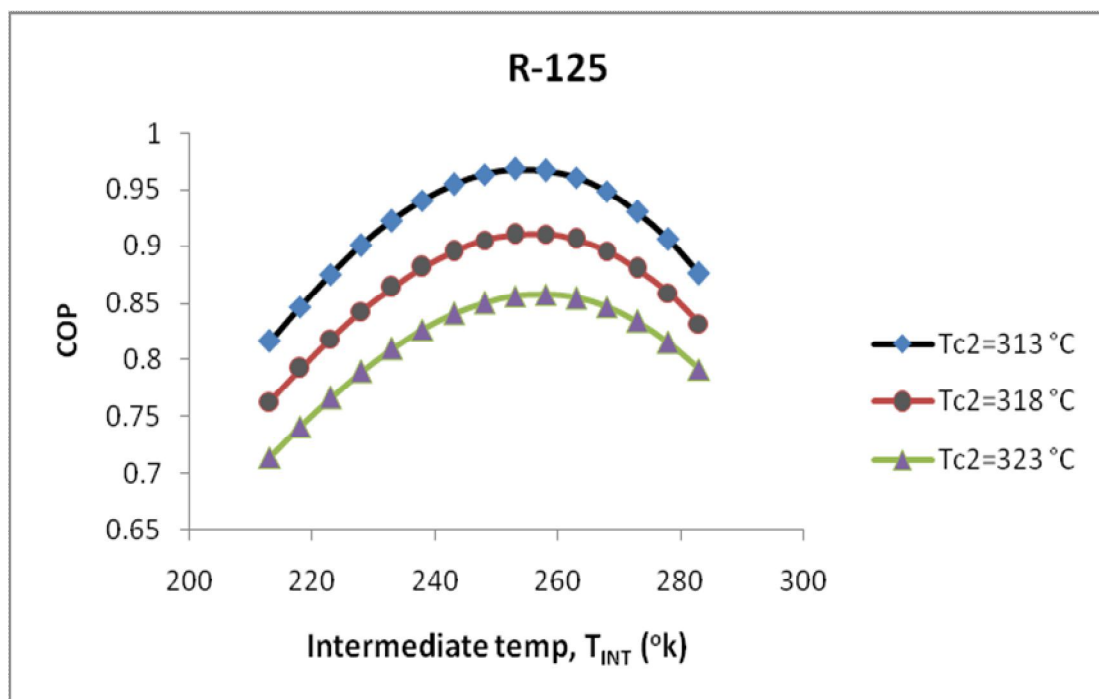


Fig.97 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

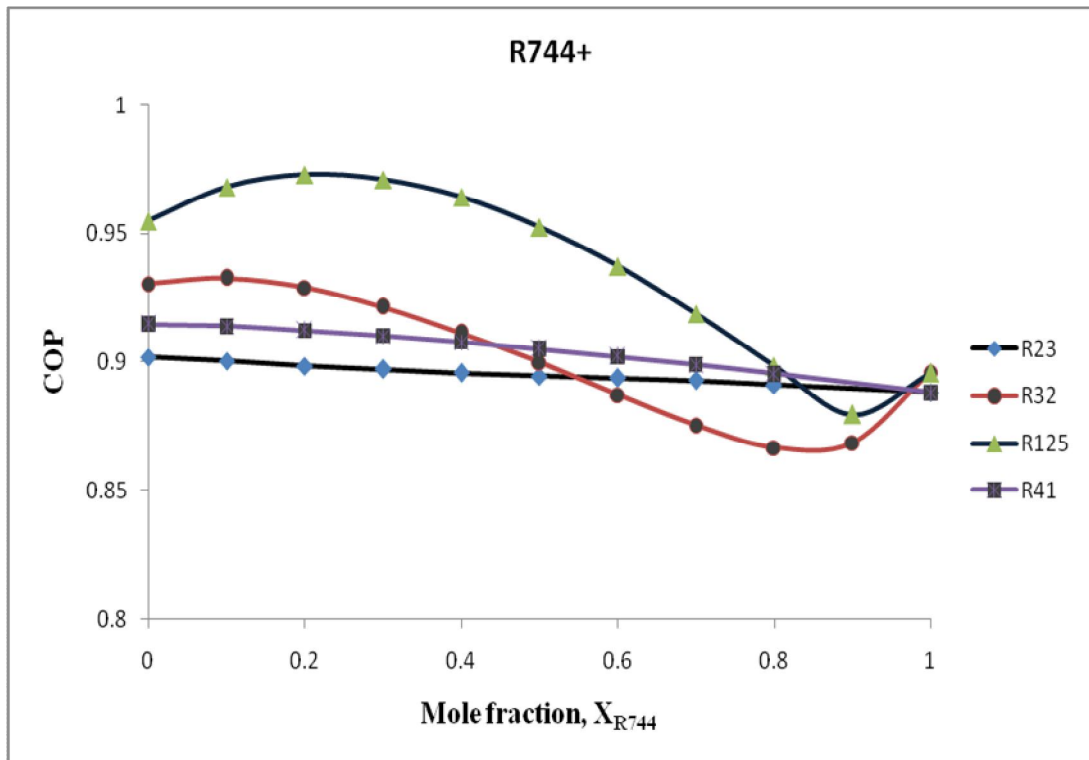


Fig.98 Variation in COP with CO<sub>2</sub> mole fraction for cascade system operating with R744 blends as low temperature working fluid.

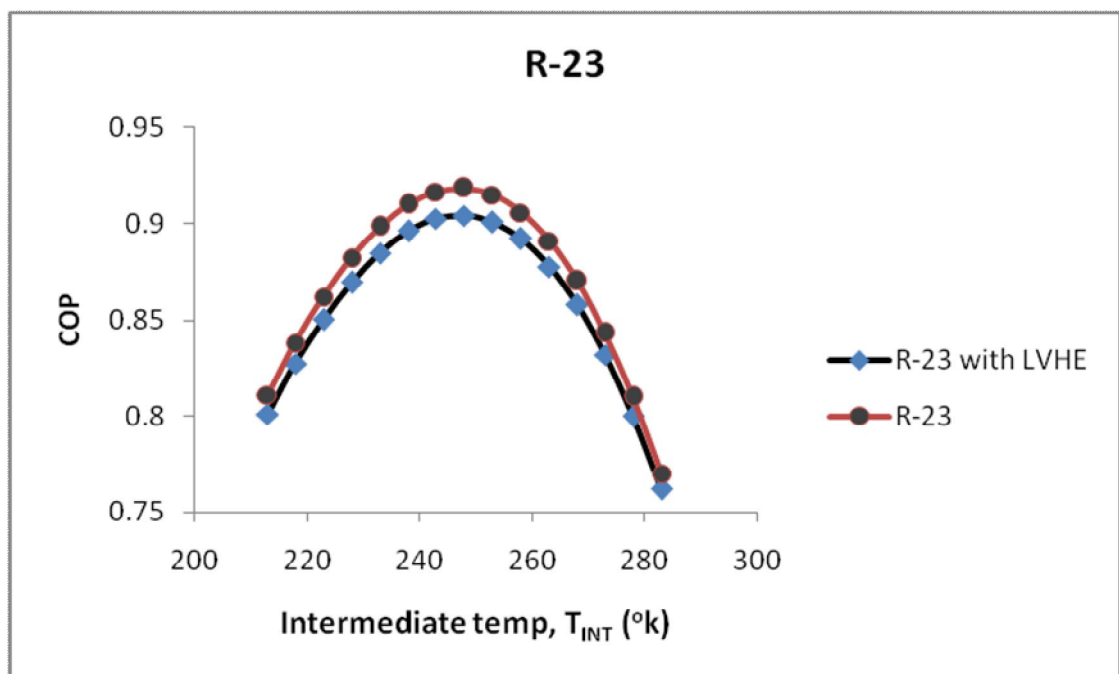


Fig.99 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 by taking LVHE effectiveness 1.

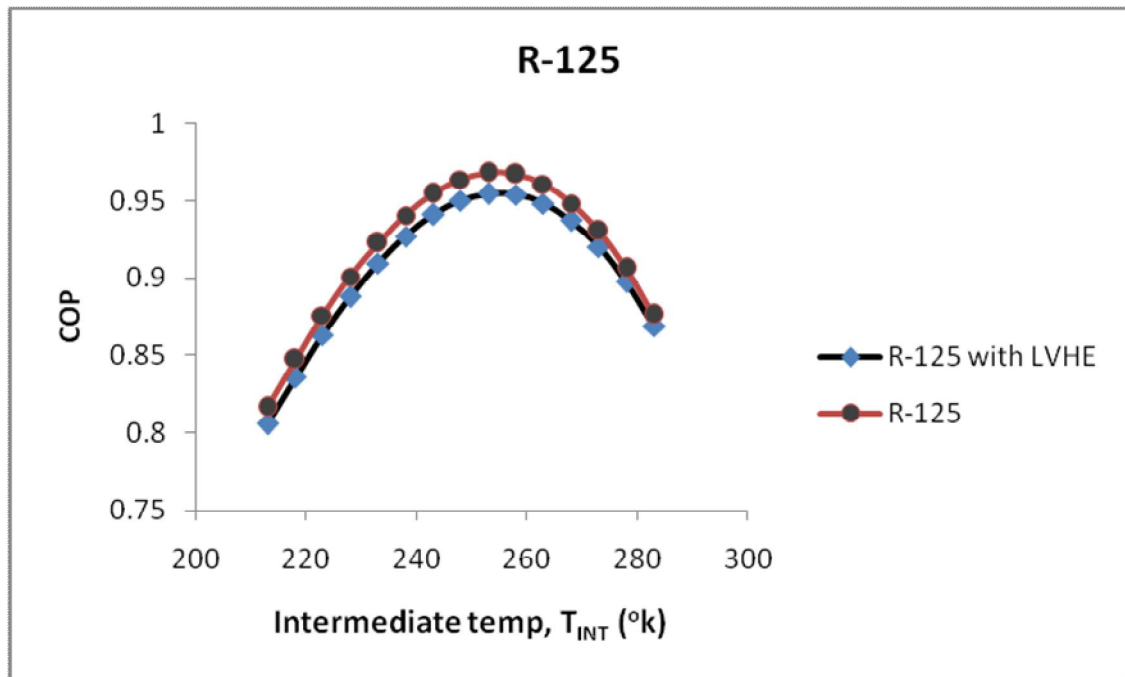


Fig.100 Variation in COP with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 by taking LVHE effectiveness 1.

## Variation in Volumetric Cooling Capacity without superheating and subcooling for cascade system

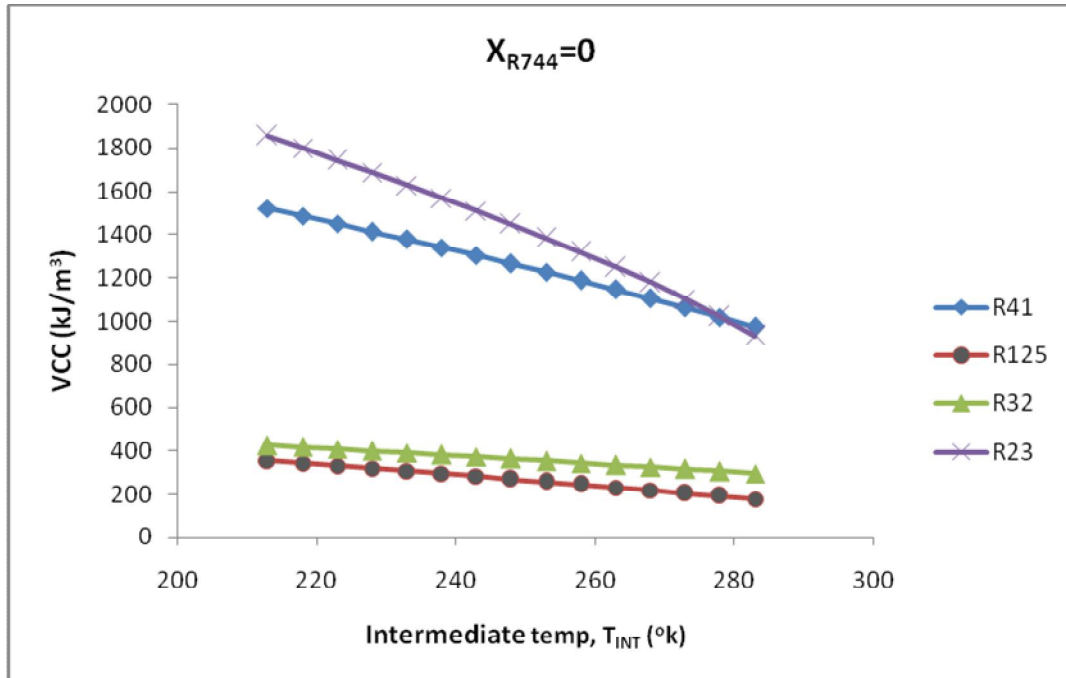


Fig.101 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.0 mole fraction as low temperature working fluid with approach 0°C.

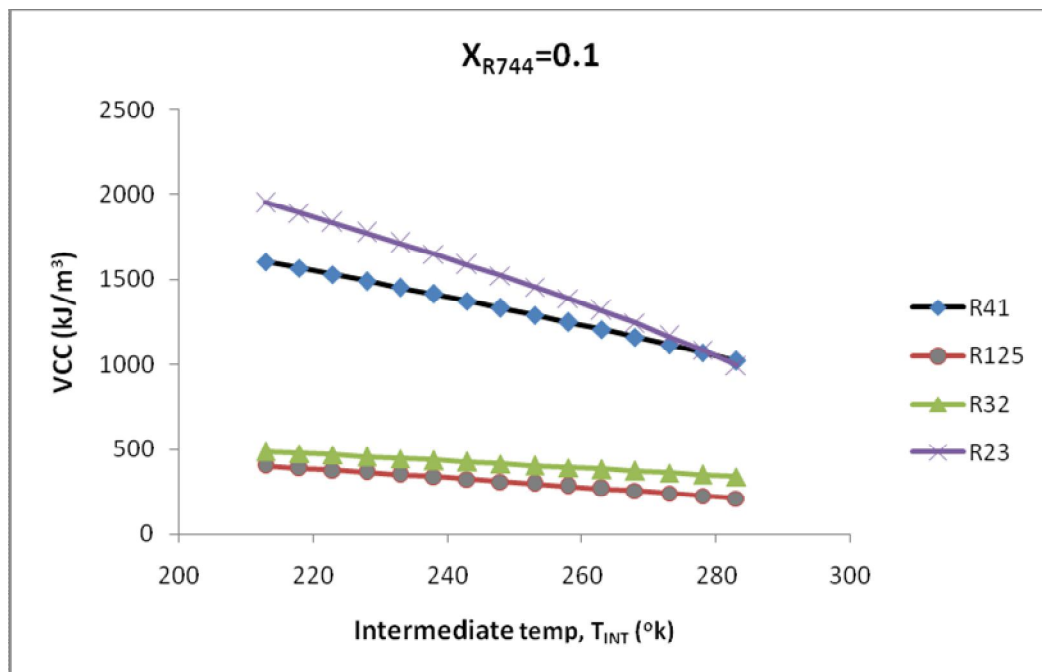


Fig.102 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

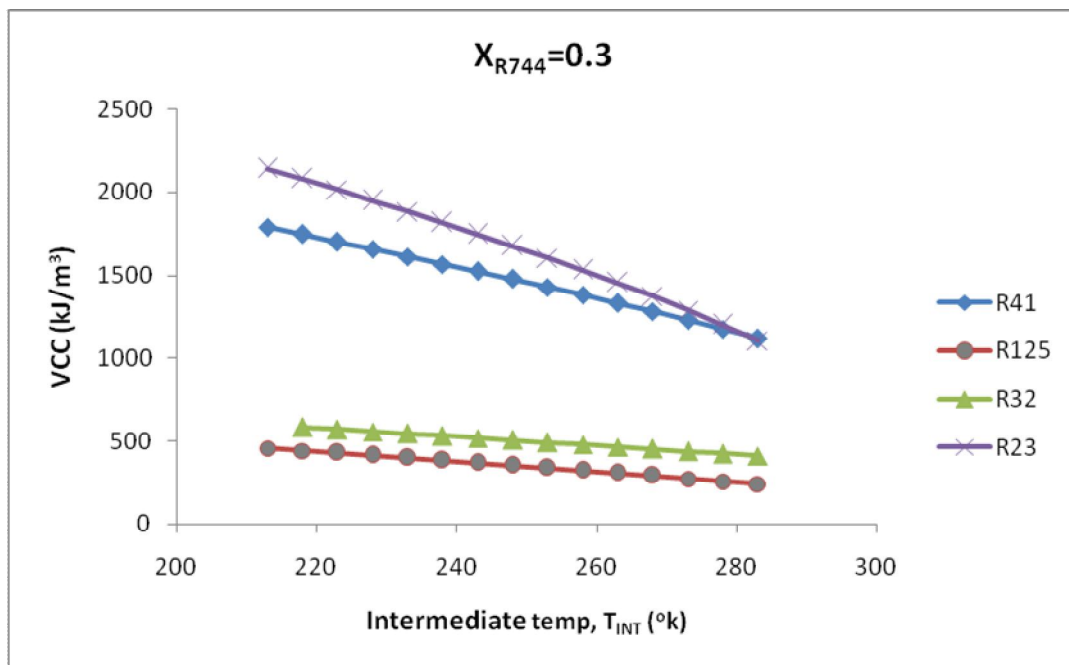


Fig.103 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

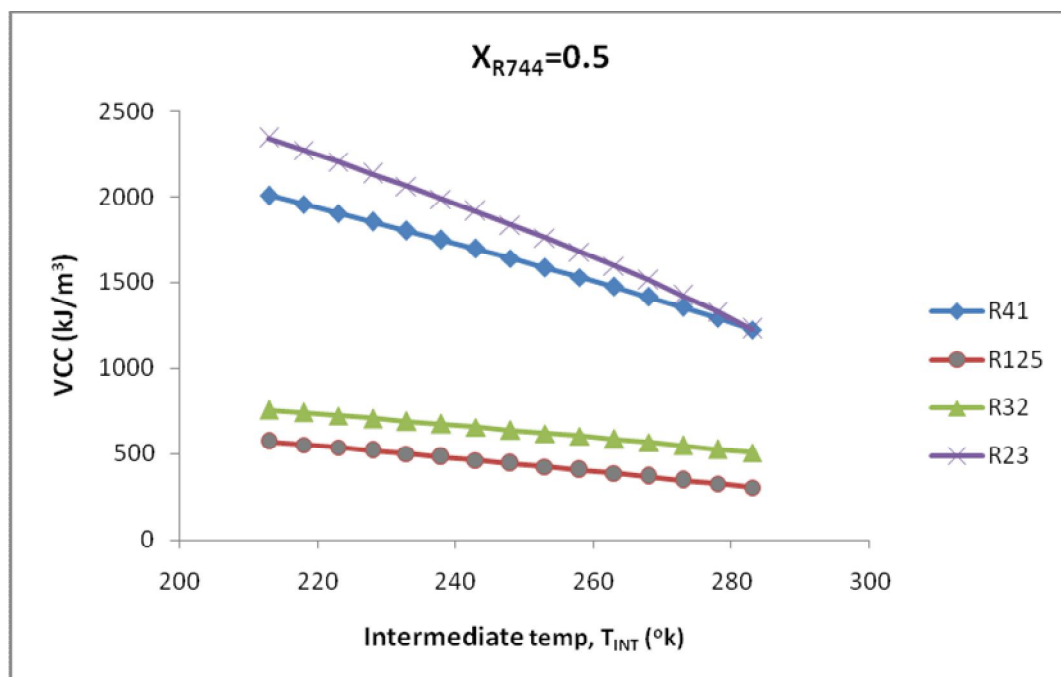


Fig.104 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

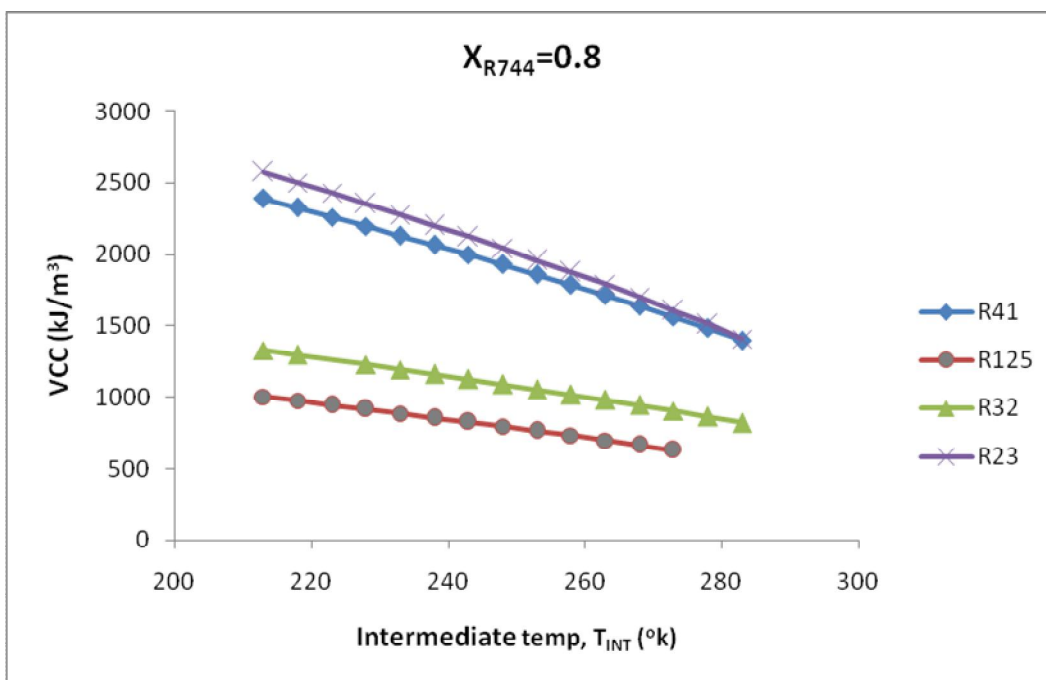


Fig.105 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

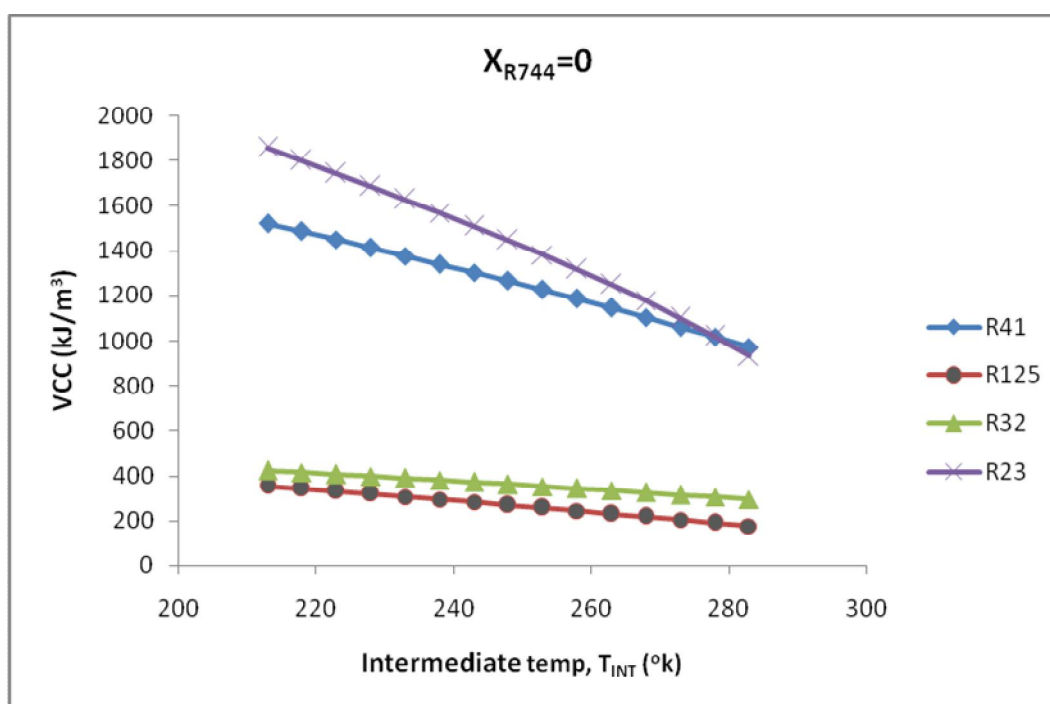


Fig.106 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 5°C.

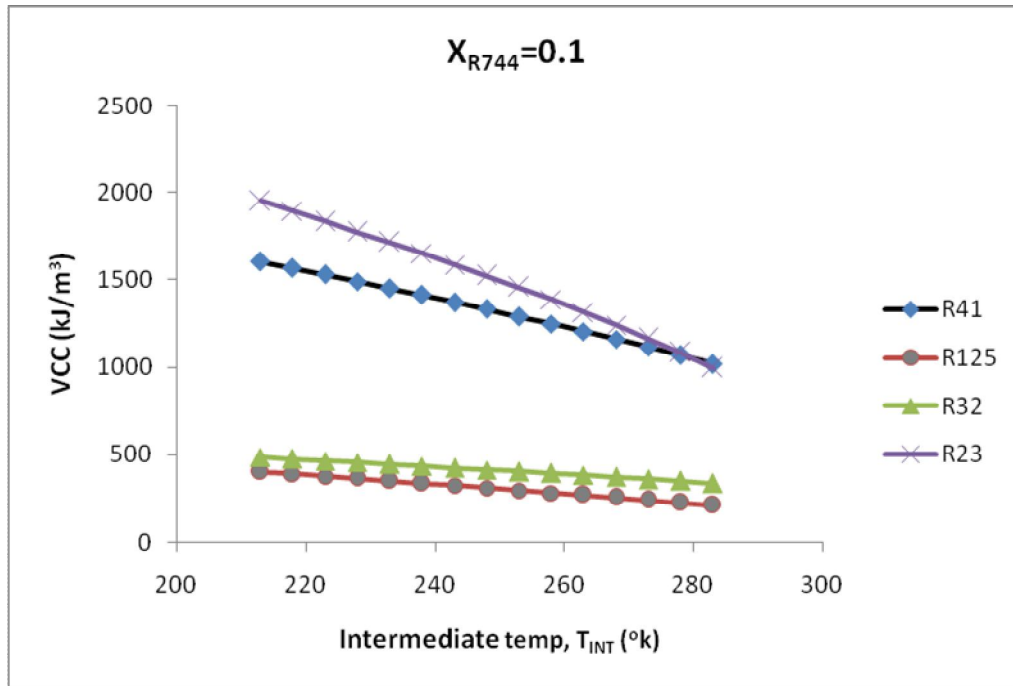


Fig.107 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

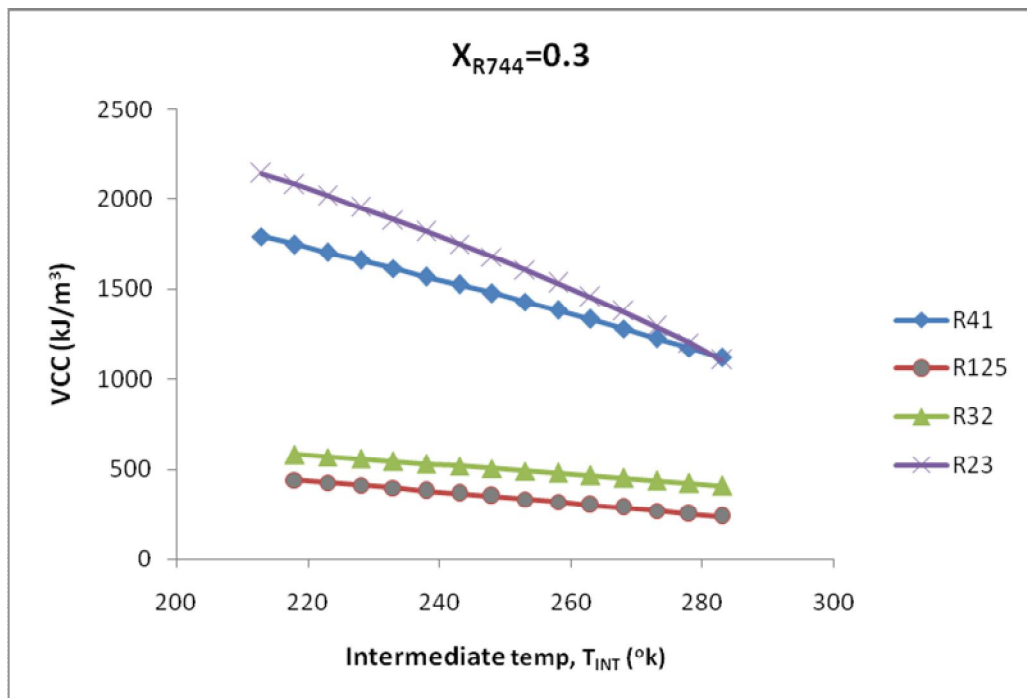


Fig.108 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.



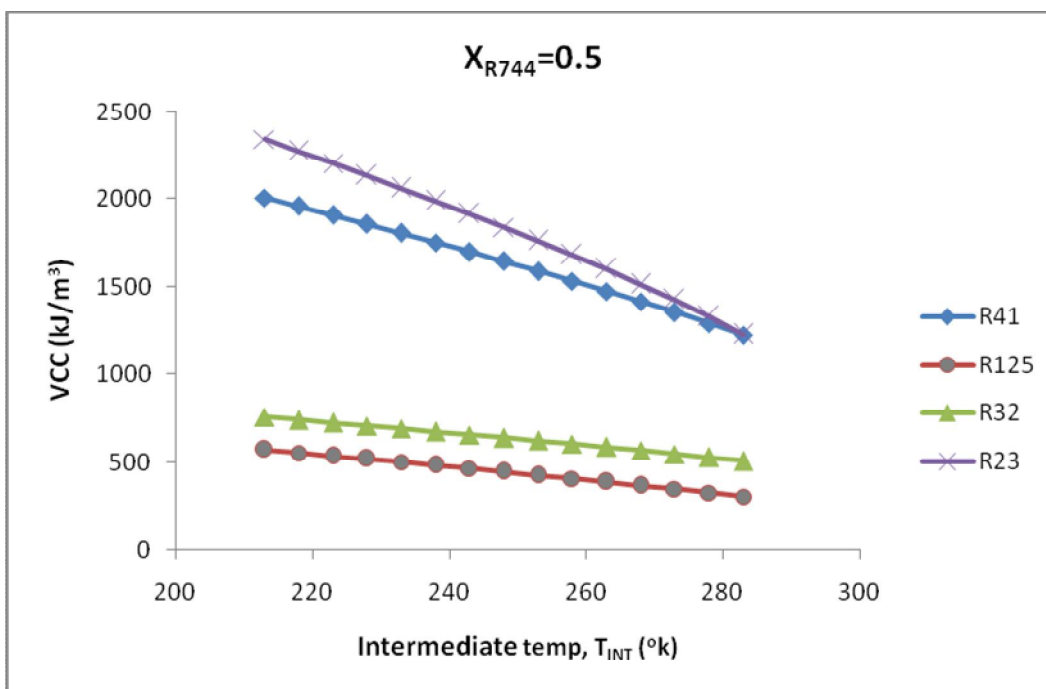


Fig.109 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

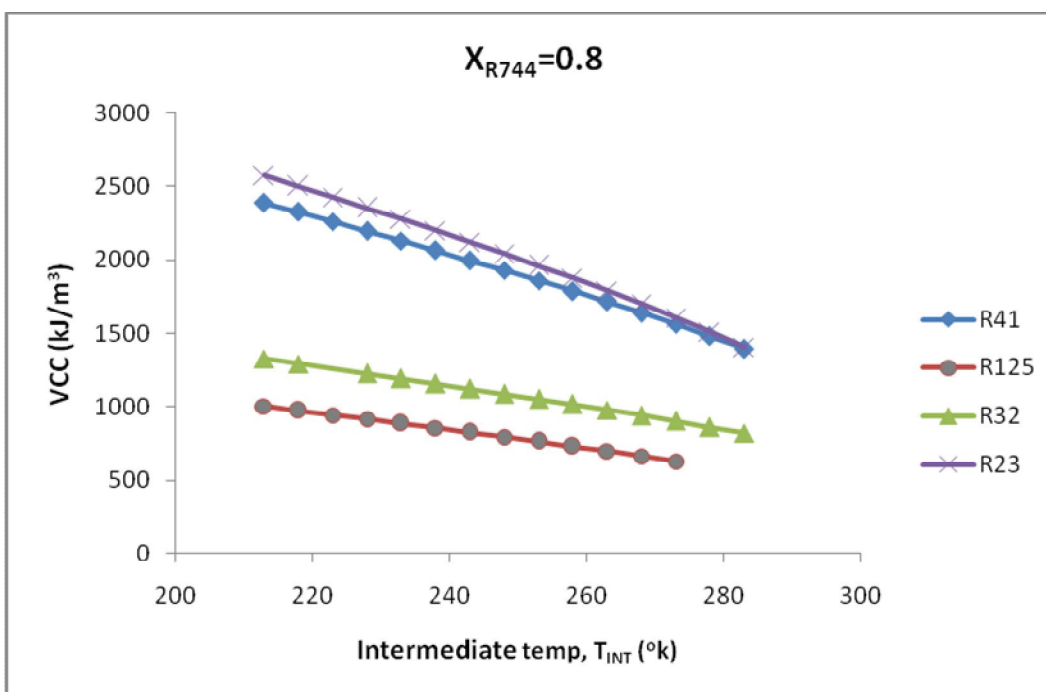


Fig.110 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.

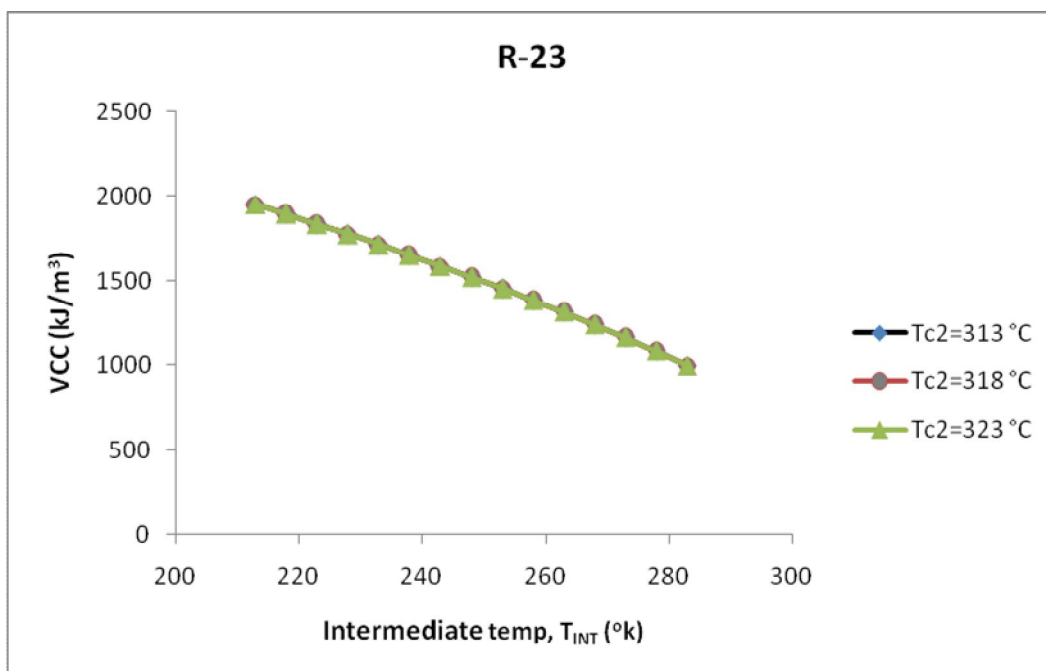


Fig.111 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

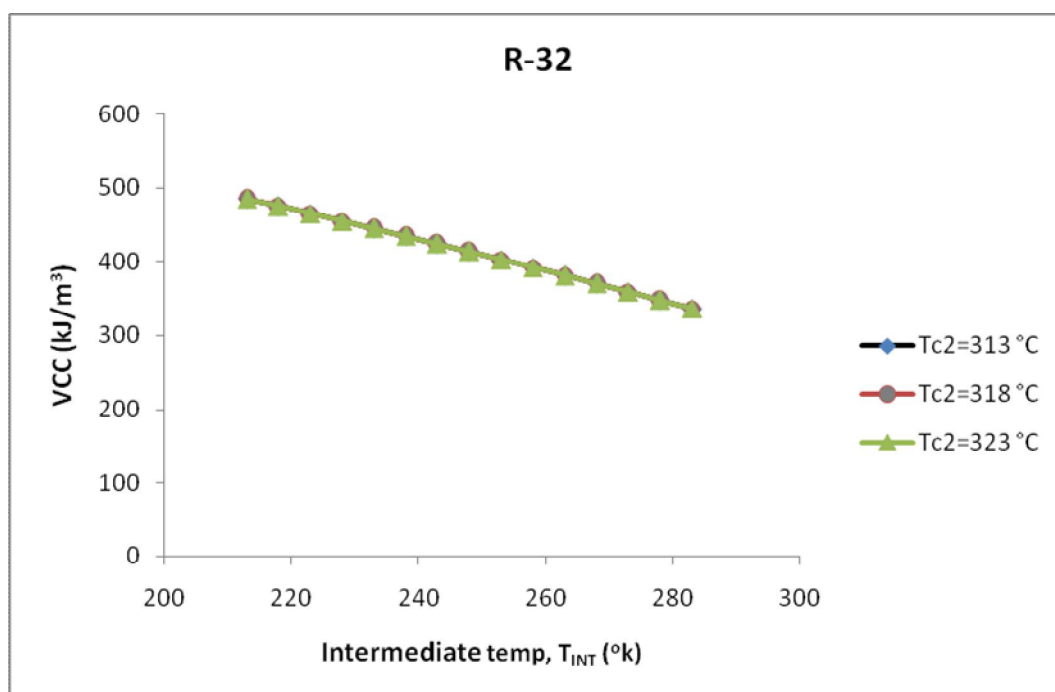


Fig.112 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

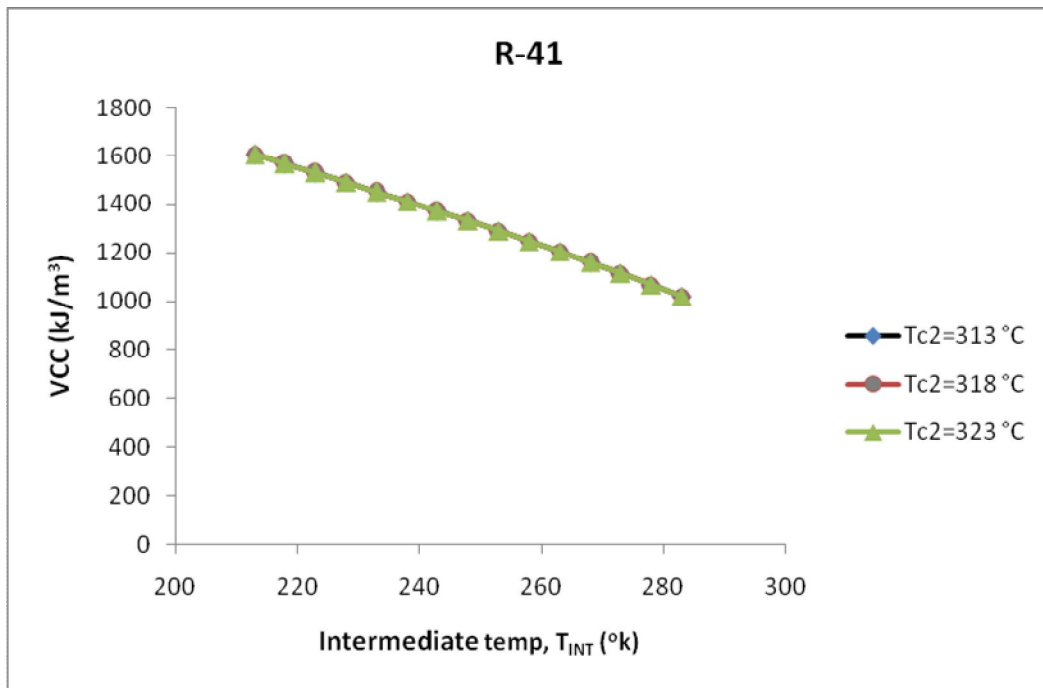


Fig.113 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

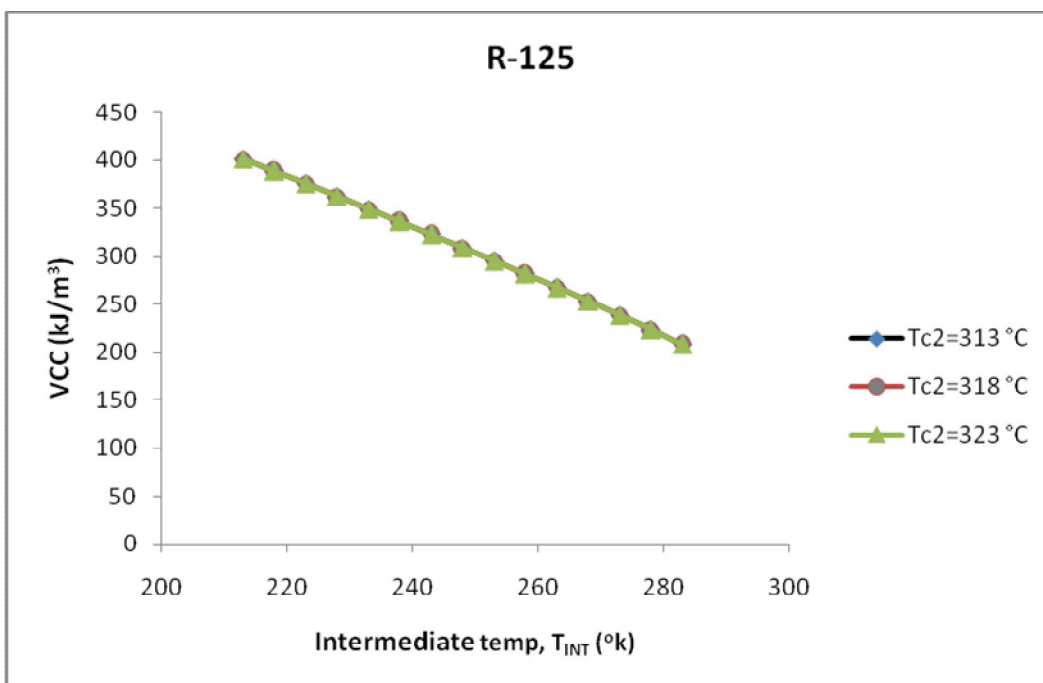


Fig.114 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

**Variation in Volumetric Cooling Capacity with superheating 10°C and subcooling 5°C for cascade system**

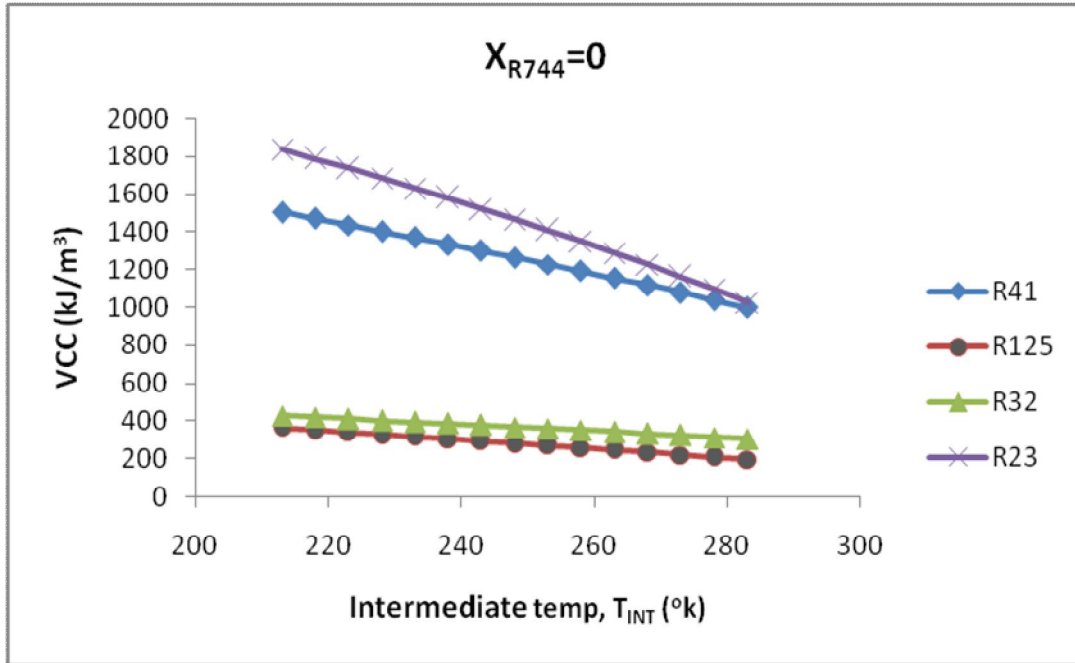


Fig.115 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0 mole fraction as low temperature working fluid with approach 0°C.

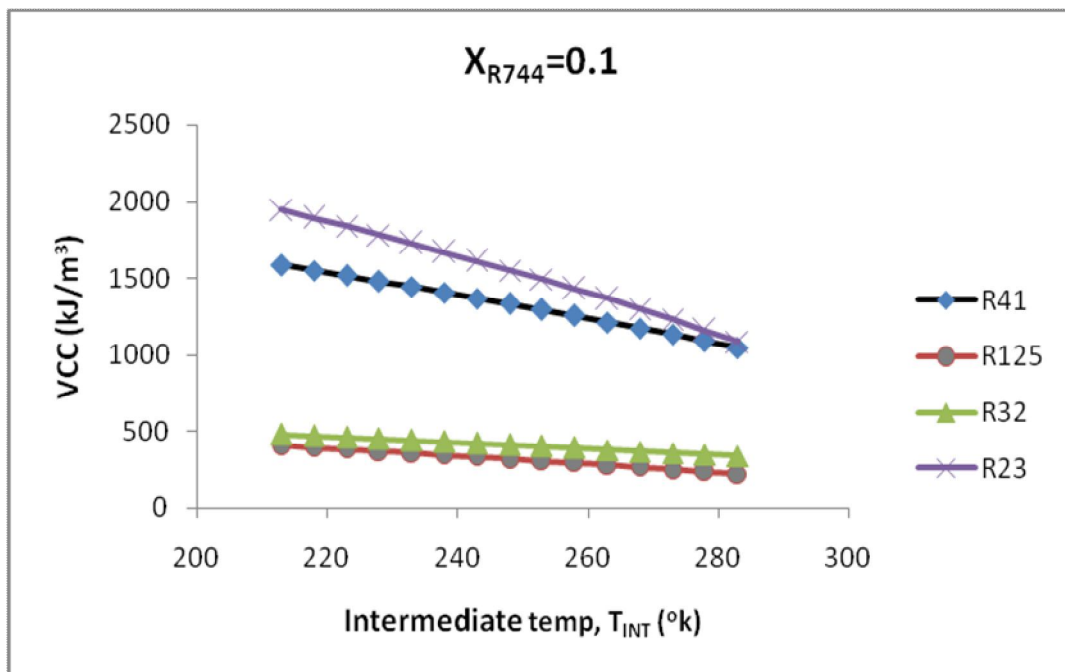


Fig.116 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 0°C.

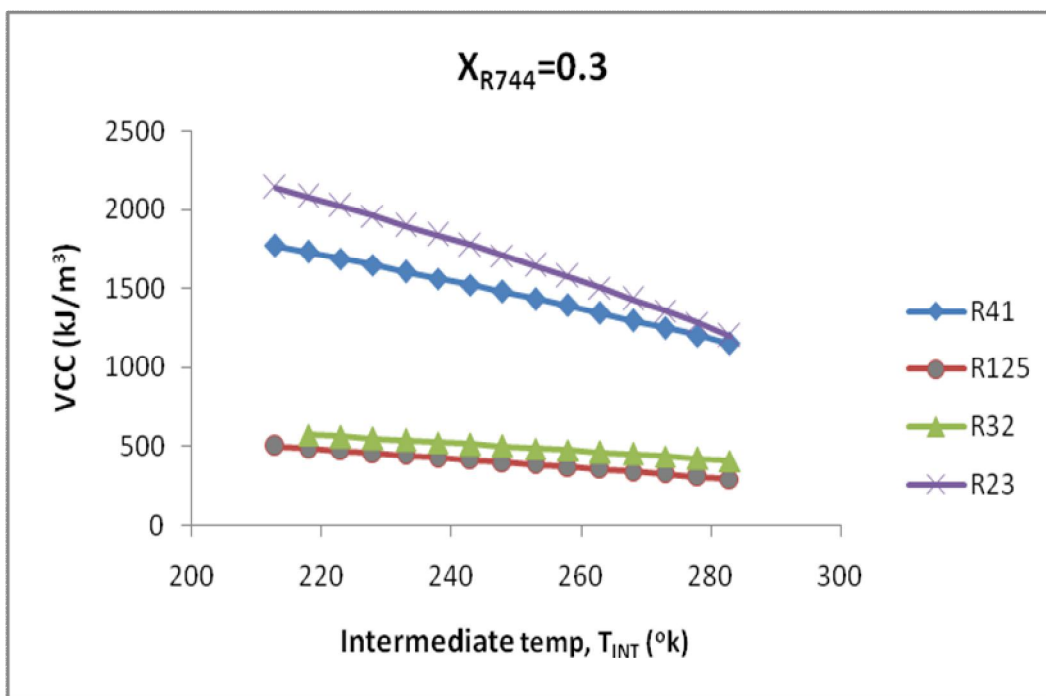


Fig.117 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 0°C.

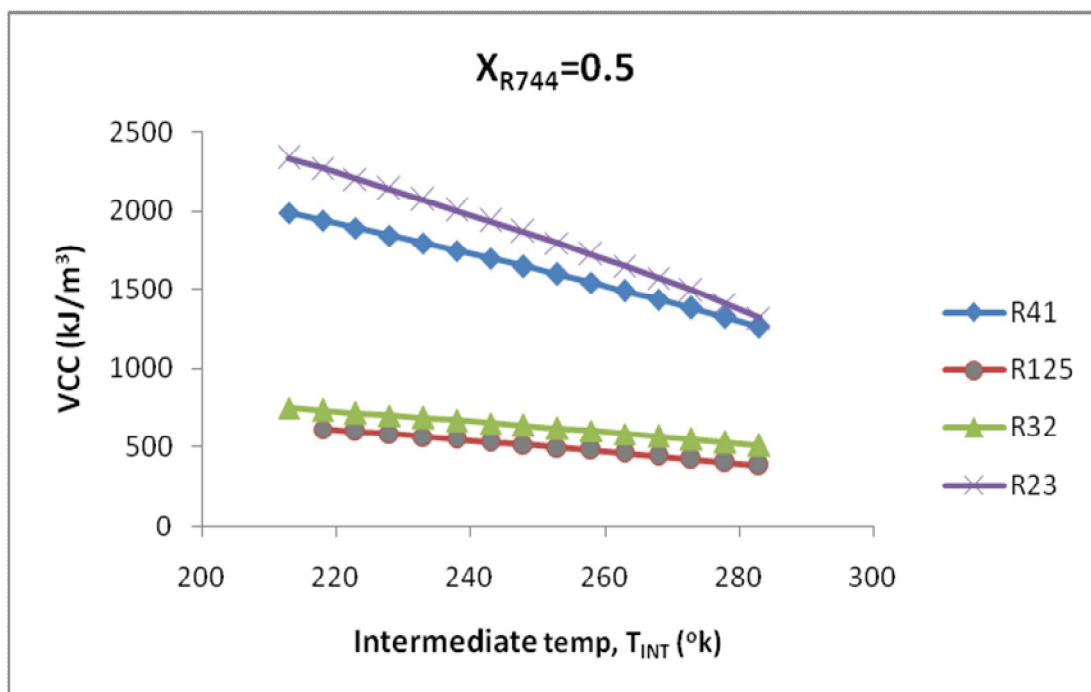


Fig.118 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 0°C.

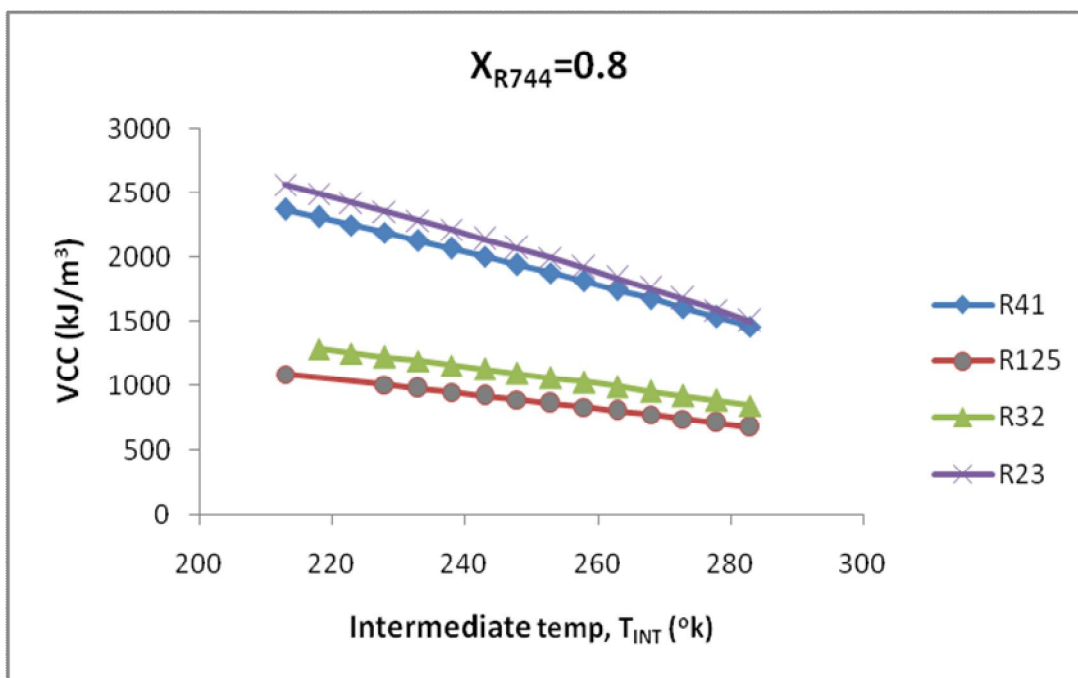


Fig.119 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 0°C.

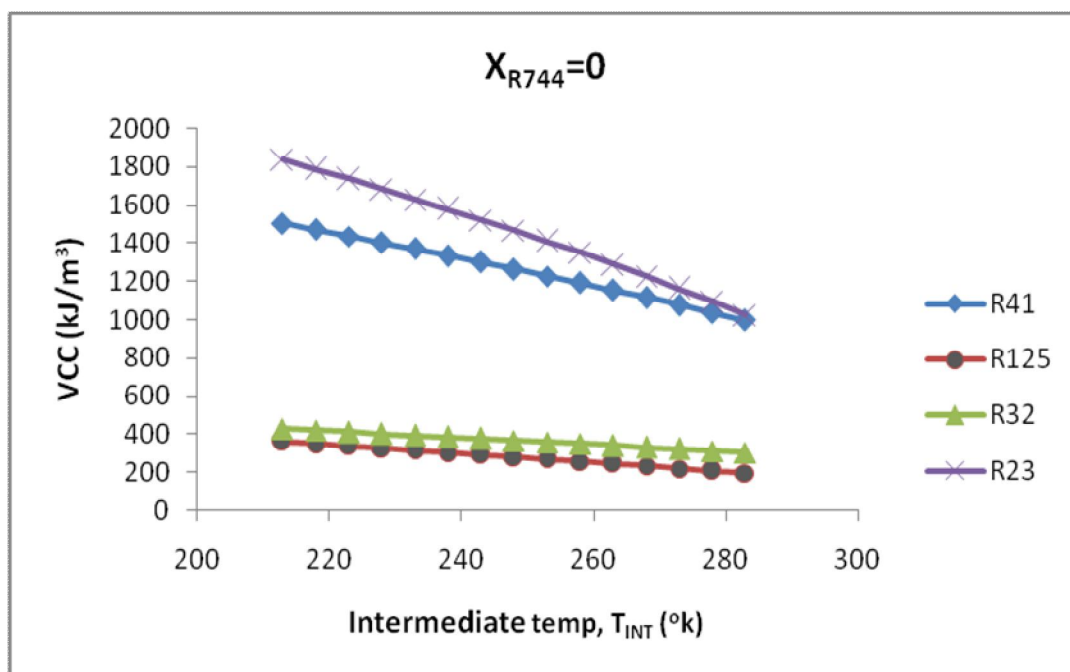


Fig.120 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.0 mole fraction as low temperature working fluid with approach 5°C.

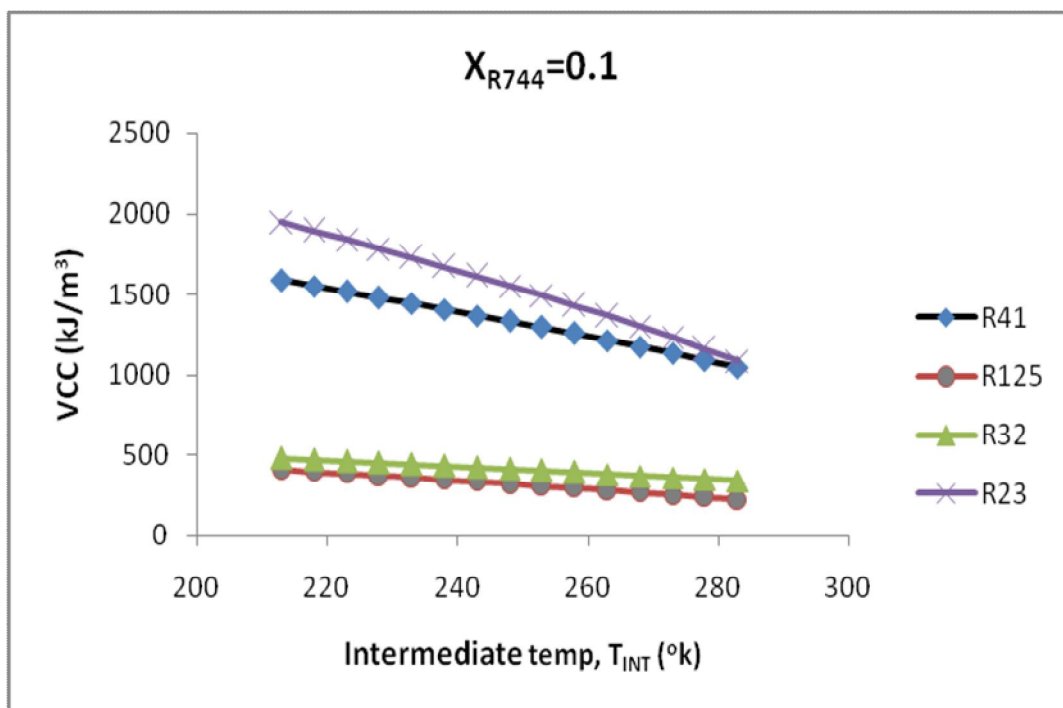


Fig.121 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid with approach 5°C.

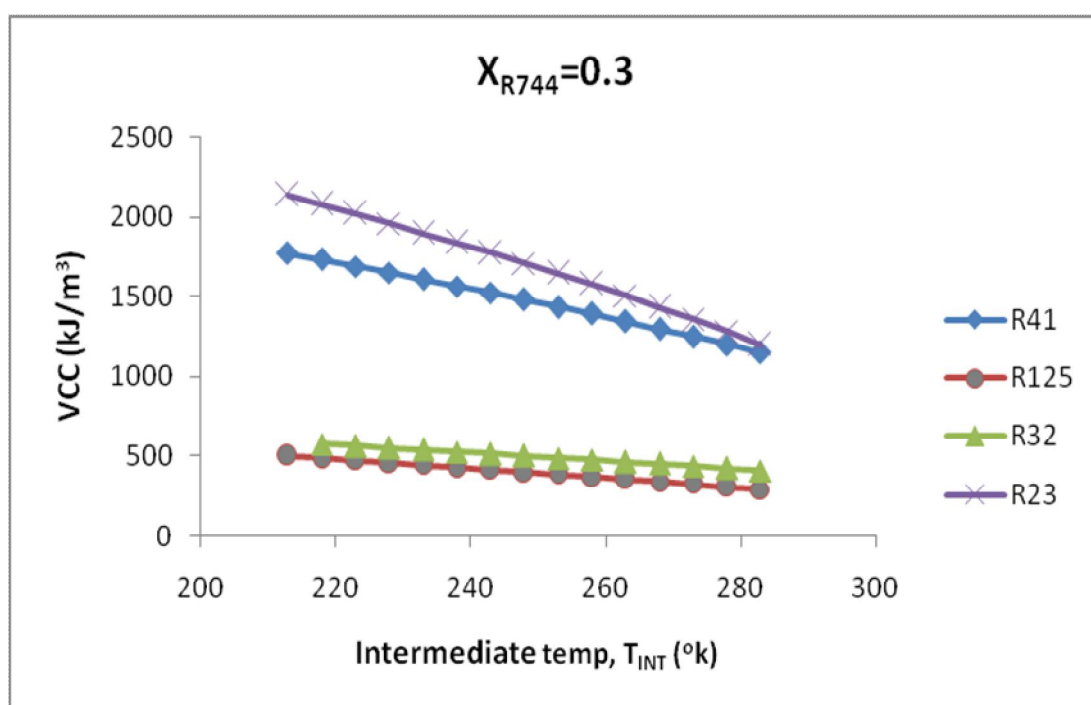


Fig.122 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.3 mole fraction as low temperature working fluid with approach 5°C.

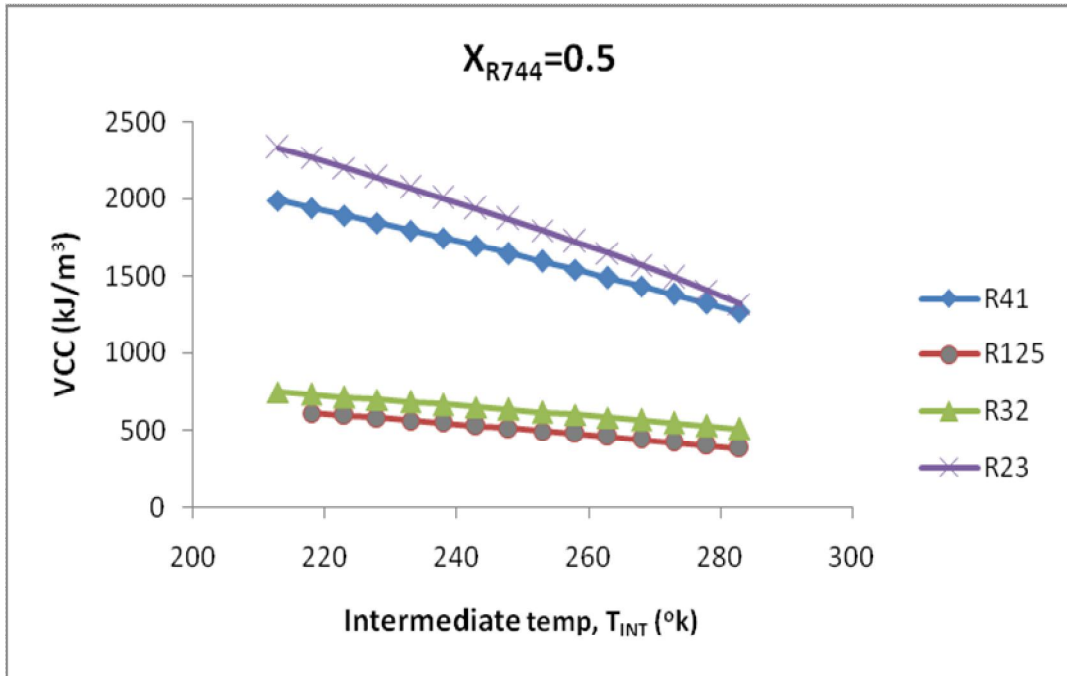


Fig.123 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.5 mole fraction as low temperature working fluid with approach 5°C.

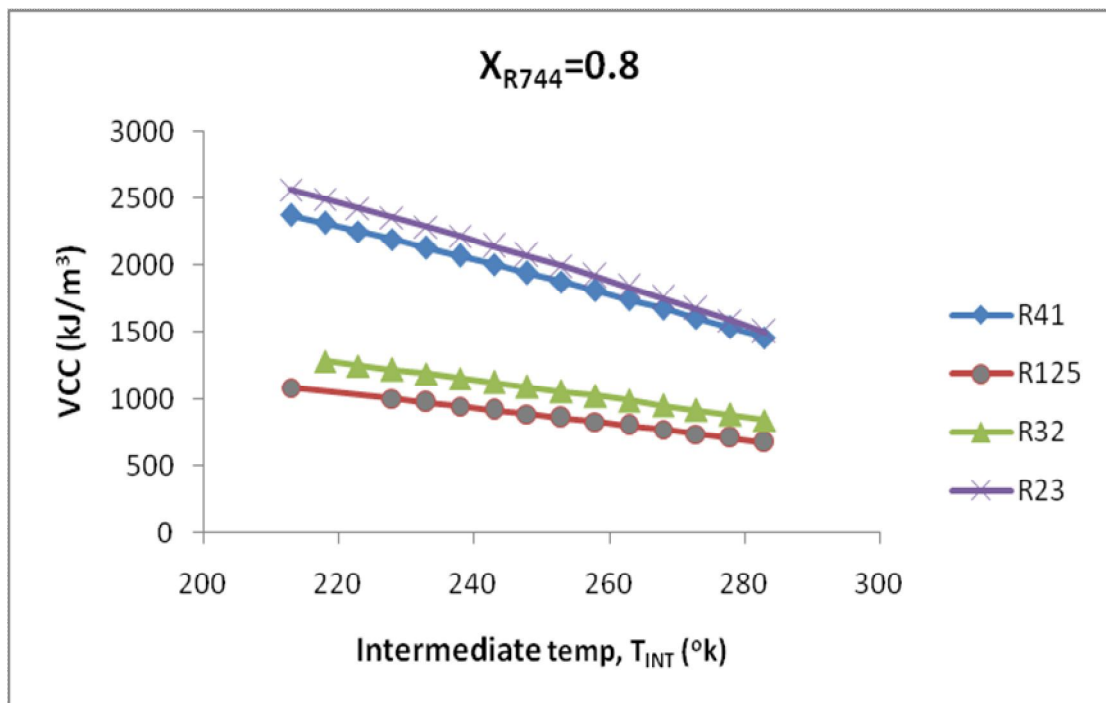


Fig.124 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.8 mole fraction as low temperature working fluid with approach 5°C.



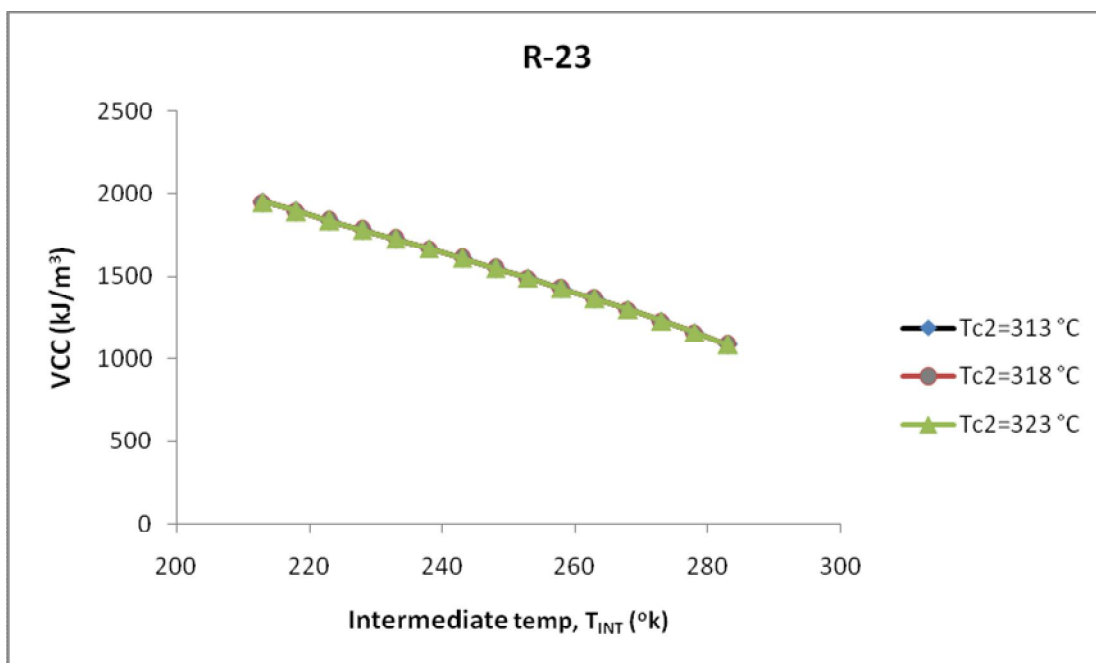


Fig.125 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-23 at different condenser temperature.

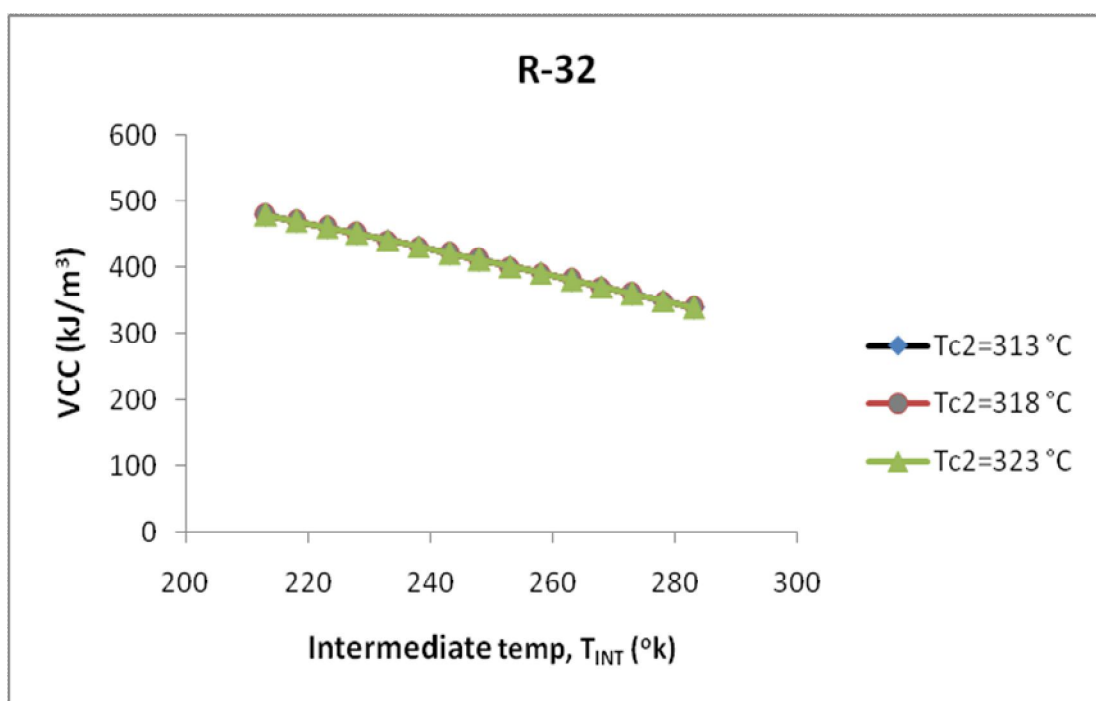


Fig.126 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-32 at different condenser temperature.

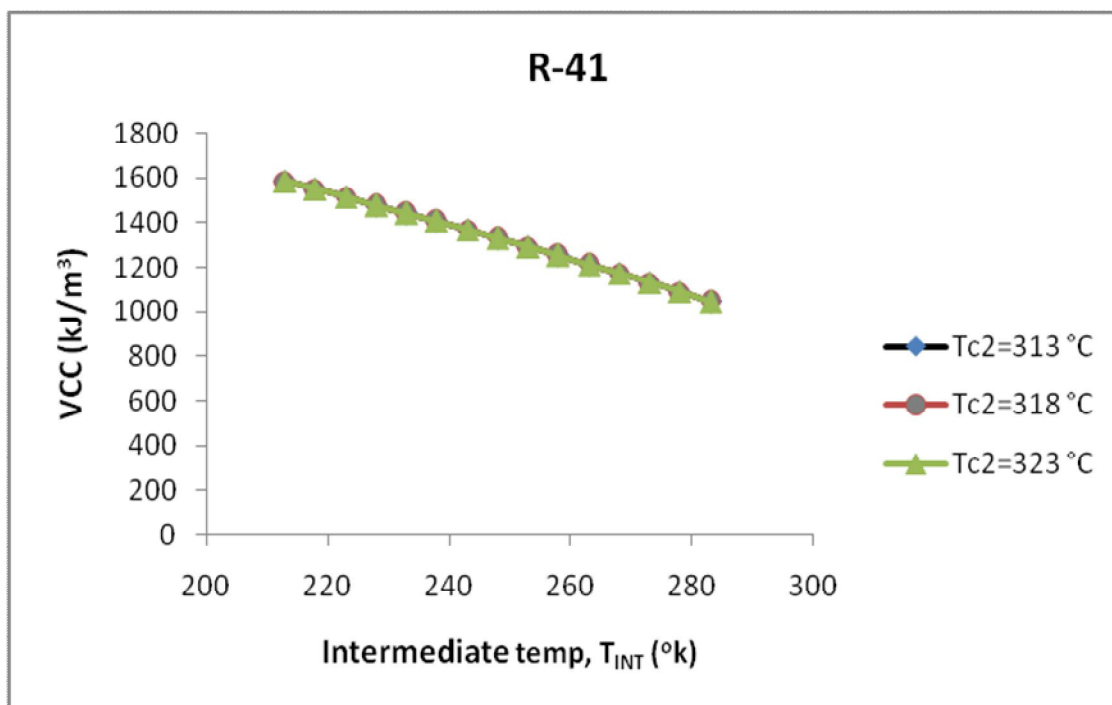


Fig.127 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-41 at different condenser temperature.

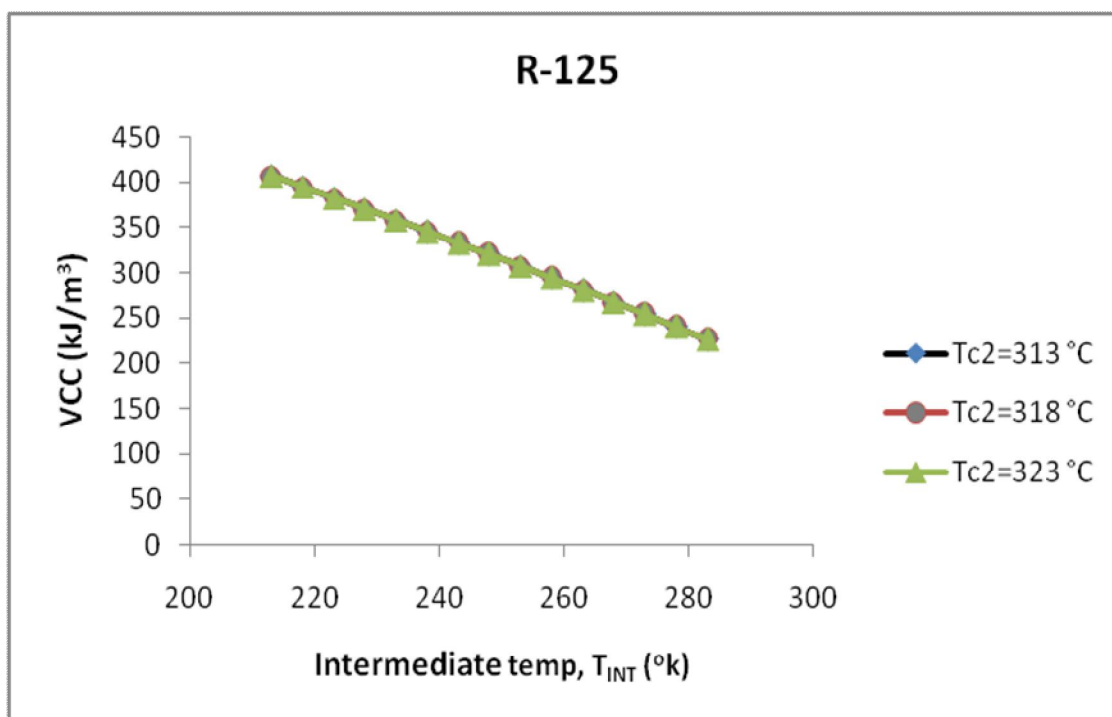


Fig.128 Variation in volumetric cooling capacity with intermediate temperature for cascade system operating with R744 blend at 0.1 mole fraction as low temperature working fluid for R-125 at different condenser temperature.

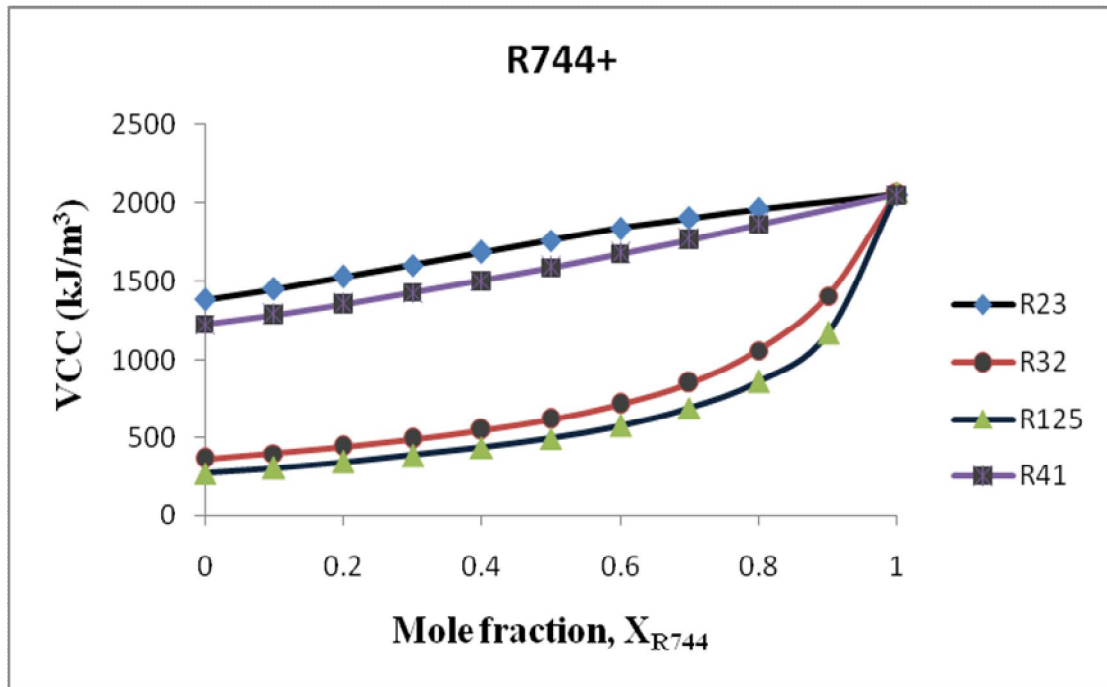


Fig.129 Variation in volumetric cooling capacity with CO<sub>2</sub> mole fraction for cascade system operating with R744 blends as low temperature working fluid.

In the present study, thermodynamic analysis have been carried out for cascade refrigeration cycle using CO<sub>2</sub>/HFC blends as the low-temperature fluid and ammonia as the high- temperature fluid with a view to extending the applicability of carbon dioxide in such systems below its triple point (216.58 K).

The results obtained permit the following remarks:

1. Mass flow rate in high temperature circuit decreases with increase in intermediate temperature for R-125 and R-23.
2. Mass flow rate in high temperature circuit increases slightly with increase in intermediate temperature for R-41 and R-32.
3. The total compressor work decreases with increase in intermediate temperature.
4. The total compressor work for R-41 mixture is highest among all mixtures followed by R-32, R-23 and R-125 respectively.
5. COP increases with increase in intermediate temperature up to a temperature (optimum temperature) after this COP decreases with increase in intermediate temperature.
6. COP for R-125 mixture is highest among all mixtures followed by R-32, R-41 and R-23 respectively.
7. The volumetric cooling capacity decreases with increase in intermediate temperature.
8. The volumetric cooling capacity for R-23 mixture is highest among all mixtures followed by R-41, R-32 and R-125 respectively.
9. By using liquid vapour heat exchanger on the low-temperature circuit, COP decreases by 1%.
10. Optimum temperature range for cascade refrigeration system is 245°K to 260°K without superheating and subcooling and 250°K to 265°K, with superheating and subcooling.

R744 blends can be considered an attractive option for the low-temperature-circuit in cascade refrigeration cycle operating at temperatures approaching 200 °K due to its low cost, easy availability and favorable properties.

1. Further investigating should be carried out for use of different hydrocarbons (HFCs) with carbon dioxide.
2. Exergy analysis should be carried out for this cascade refrigeration system using carbon dioxide blend with HFCs in low temperature circuit.
3. Exergo economic analysis should be carried out for this cascade refrigeration system using carbon dioxide blend with HFCs in low temperature circuit.

## APPENDIX A

### Computer program

```
t1=te1+10
h1=Enthalpy(r23,t=t1,p=pe1)
s1=Entropy(r23,T=T1,p=pe1)
v1=Volume(R23,T=t1,P=Pe1)
Pc1=P_sat(r23,T=tc1)
s2s=s1
h2s=Enthalpy(r23,s=s2s,p=pc1)
h2=h1+((h2s-h1)/nc1)
s2=Entropy(r23,P=Pc1,h=h2)
t3=tc1-5
h3=Enthalpy(r23,T=T3,p=pc1)
s3=Entropy(r23,T=T3,p=pc1)
h3=h4
Pe1=P_sat(r23,T=Te1)
s4=Entropy(r23,P=Pe1,h=h4)
wc1=mr1*(h2-h1)

t2=te2+10
h5=Enthalpy(r717,T=T2,p=pe2)
s5=Entropy(r717,T=T2,p=pe2)
Pc2=P_sat(r717,T=tc2)
s6s=s5
h6s=Enthalpy(r717,s=s6s,p=pc2)
h6=h5+((h6s-h5)/nc2)
s6=Entropy(r717,P=Pc2,h=h6)
t7=tc2-5
h7=Enthalpy(r717,T=T7,p=pc2)
s7=Entropy(r717,T=T7,p=pc2)
h7=h8
Pe2=P_sat(r717,T=Te2)
```

$$s8=\text{Entropy}(r717,P=\text{Pe}2,h=h8)$$

$$wc2=mr2*(h6-h5)$$

$$wc=wc1+wc2$$

$$Qe=mr1*(h1-h4)$$

$$mr1*(h2-h3)=mr2*(h5-h8)$$

$$cop=Qe/wc$$

$$vcc=Qe/(mr1*v1)$$

$$te2=tc1-\text{approach}$$

$$tc1=250$$

$$tc2=313$$

$$te1=203$$

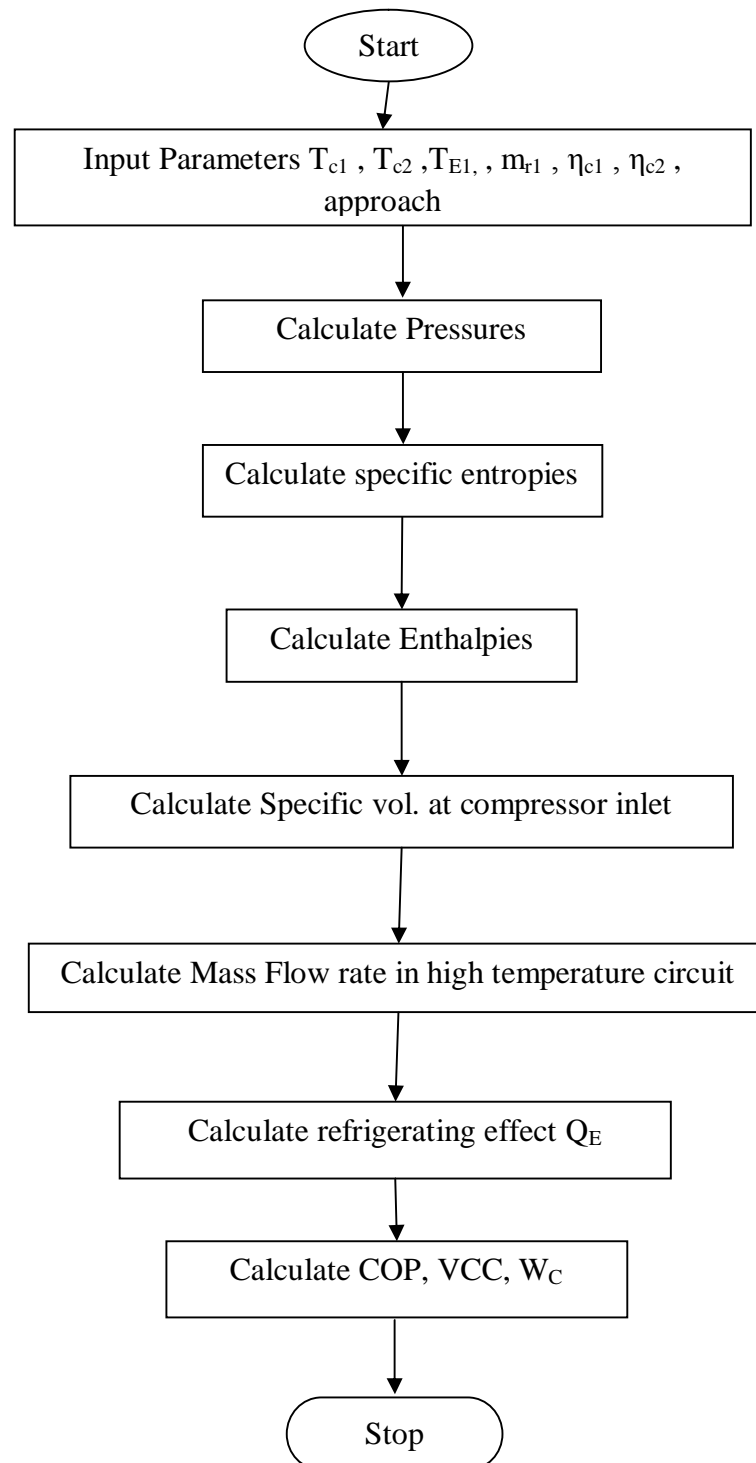
$$mr1=1$$

$$nc1=0.7$$

$$nc2=0.7$$

$$\text{approach}=5$$

## FLOW DIAGRAM





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